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Please check the examination d	letails below before entering	your candidate information			
Candidate surname	0	ther names			
Pearson Edexcel International GCSE	Centre Number	Candidate Number			
Monday 21 January 2019					
Morning (Time: 2 hours)	Paper Refe	rence 4PM0/02			
Further Pure N	<b>Nathemati</b>	CS			
Paper 2					

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
  - there may be more space than you need.

#### Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

### Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ▶





### Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Solve the equation 
$$3\log_3 x - 8\log_x 3 = 10$$

(6)

**Question 1 continued** 

(Total for Question 1 is 6 marks)



(a) Using the axes below, sketch the line with equation

(i) 
$$y + 2x = -5$$

(ii) 
$$y = x + 4$$

Show the coordinates of the points where each line crosses the coordinate axes.

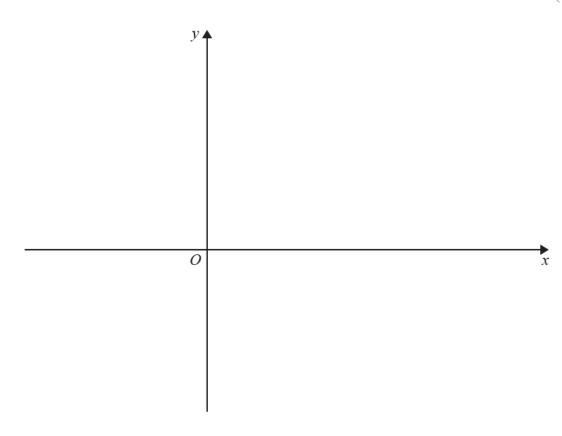
(2)

(b) Show, by shading, the region R defined by the inequalities

$$y + 2x > -5 \qquad \qquad y < x + 4$$

$$y < x + 4$$

(1)



Question 2 continued

(Total for Question 2 is 3 marks)



- Referred to a fixed origin O, the position vectors of the points P and Q are  $(5\mathbf{i} + 6\mathbf{j})$  and  $(3\mathbf{i} 4\mathbf{j})$  respectively.
  - (a) Find, as a simplified expression in terms of **i** and **j**,  $\overrightarrow{PQ}$ .

(2)

(b) Find a unit vector parallel to  $\overrightarrow{PQ}$ .

**(2)** 

The position vector of the fixed point R is  $(13\mathbf{i} + a\mathbf{j})$ , where a is a constant.

Given that  $\overrightarrow{QR} = 5\overrightarrow{QP}$ 

(c) find the value of a.

(2)

Question 3 continued

(Total for Question 3 is 6 marks)



- 4 A particle P is moving along the x-axis. At time t seconds  $(t \ge 0)$  the velocity, v m/s, of P is given by  $v = 4 \sin 2t$ 
  - (a) Find the least value of t for which the velocity of P is 2 m/s.

(2)

(b) Find the magnitude of the acceleration of P when its velocity is  $2 \,\mathrm{m/s}$ .

(3)

The particle *P* is at the point with coordinates (3, 0) when  $t = \frac{\pi}{4}$ 

(c) Find the distance of P from the origin when t = 0

**(4)** 

**Question 4 continued** 

(Total for Question 4 is 9 marks)



5

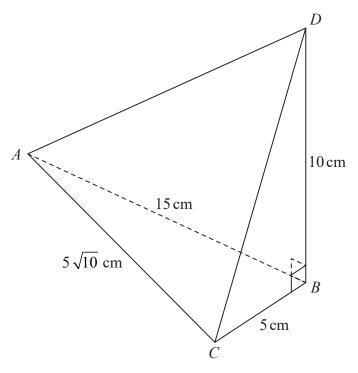


Diagram **NOT** accurately drawn

Figure 1

Figure 1 shows a triangular pyramid ABCD where triangle ABC is the base and BD is perpendicular to the base.

$$AB = 15 \text{ cm}$$
  $AC = 5\sqrt{10} \text{ cm}$   $BC = 5 \text{ cm}$   $BD = 10 \text{ cm}$ 

(a) Show that  $\angle ABC = 90^{\circ}$ 

(2)

(b) Find, in degrees to 1 decimal place, the size of  $\angle DAC$ .

**(4)** 

The point X on AC is such that BX is perpendicular to AC.

(c) Find, in degrees to 1 decimal place, the size of  $\angle DXB$ .

(4)

**Question 5 continued** 



Question 5 continued

**Question 5 continued** 

(Total for Question 5 is 10 marks)



6

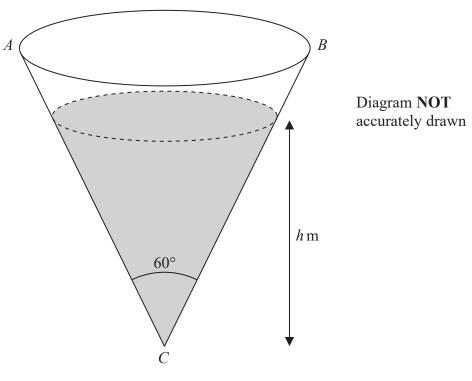


Figure 2

Figure 2 shows a water tank in the shape of a hollow right circular cone fixed with its axis of symmetry vertical. A diameter of the circular rim of the cone is AB. The vertex, C, of the cone is below AB such that  $\angle ACB = 60^{\circ}$ 

Initially, the tank is empty and water flows into the tank at a constant rate of  $0.03 \,\mathrm{m}^3/\mathrm{s}$ . At time t seconds after the water starts to flow into the tank, the height of the surface of the water in the tank above C is h metres.

Find, in m/s to 3 significant figures, the rate of change of the height of the surface of the water above C at the instant when h = 1.5

**(6)** 

Question 6 continued

(Total for Question 6 is 6 marks)



7 (a) Complete the table of values for  $y = \ln(3x + 1) + 2$ , giving your answers to 2 decimal places.

х	0	1	2	3	4	5	6	
у	2		3.95	4.30			4.94	

**(2)** 

(b) On the grid opposite, draw the graph of  $y = \ln(3x + 1) + 2$  for  $0 \le x \le 6$ 

(2)

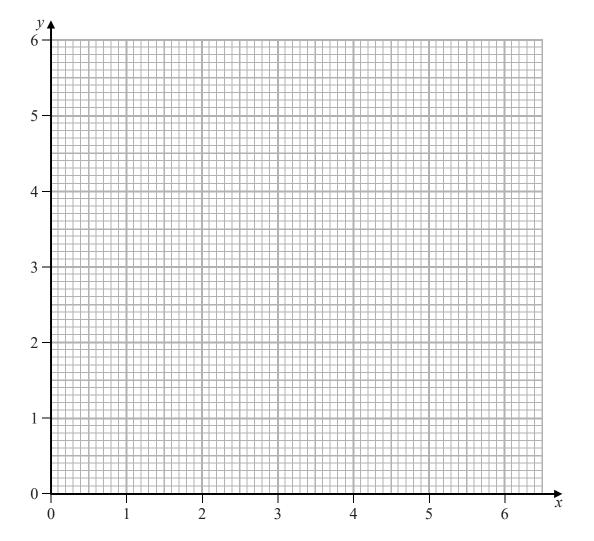
(c) Use your graph to obtain an estimate, to 1 decimal place, for the value of ln 10.6 You **must** show clearly how you have used your graph.

(3)

(d) By drawing a straight line on the grid, obtain estimates, to 1 decimal place, for the roots of the equation  $(3x+1)^2 = e^{(x+1)}$  in the interval  $0 \le x \le 6$ 

(5)

# Question 7 continued



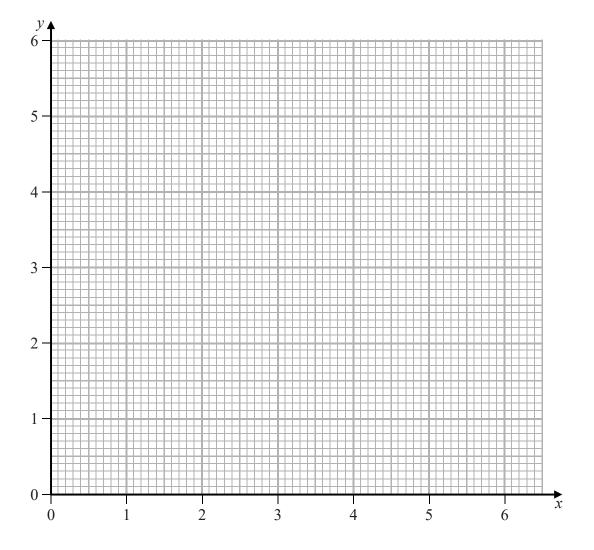
Turn over for a spare grid if you need to redraw your graph.



Question 7 continued

## **Question 7 continued**

Only use this grid if you need to redraw your graph.



(Total for Question 7 is 12 marks)



8 The roots of the equation  $3x^2 - 2x - 1 = 0$  are  $\alpha$  and  $\beta$ , where  $\alpha > \beta$ 

Without solving the equation,

(a) find the value of  $\alpha^2 + \beta^2$ 

(3)

(b) show that  $\alpha - \beta = \frac{4}{3}$ 

**(2)** 

(c) form a quadratic equation, with integer coefficients, that has roots  $\frac{\alpha + \beta}{\alpha}$  and  $\frac{\alpha - \beta}{\beta}$ 

**(6)** 

**Question 8 continued** 

Question	8	continued

**Question 8 continued** 

(Total for Question 8 is 11 marks)





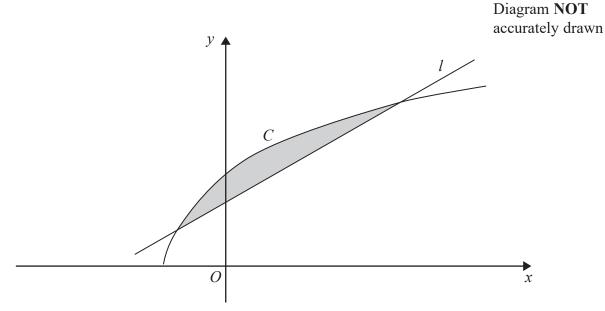


Figure 3

Figure 3 shows part of the curve C with equation  $y = (2x + 3)^{\frac{1}{2}}$  and the line l with equation 2y = x + 3The line l crosses C at two points.

(a) Find the coordinates of each of these points.

**(5)** 

The finite region bounded by C and l, shown shaded in Figure 3, is rotated through  $360^{\circ}$  about the x-axis.

(b) Use algebraic integration to find, in terms of  $\pi$ , the volume of the solid generated.

**(5)** 

Question 9 continued

Question 9 continued

Question 9 continued

(Total for Question 9 is 10 marks)



10 A geometric series has first term a and common ratio r (r > 0) The nth term of the series is  $U_n$ 

Given that  $U_1 + 3U_2 = 8$  and that  $U_2 \times U_3 = 4U_5$ 

- (a) find
  - (i) the value of r
  - (ii) the value of a

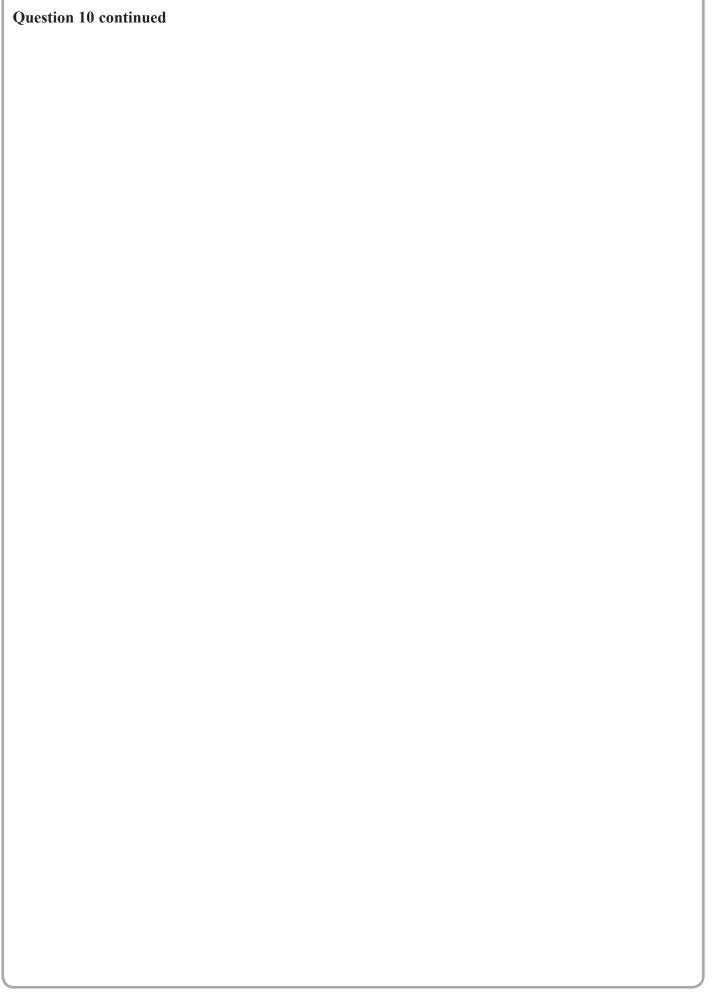
(5)

(b) Hence show that  $U_n = \frac{2^{n+2}}{3^n}$ 

(2)

(c) Find the least value of n such that  $U_n < 0.05$ 

(3)



**Question 10 continued** 

Question 10 continued

(Total for Question 10 is 10 marks)



 $\cos(A+B) = \cos A \cos B - \sin A \sin B$ 

(a) (i) Using the above identity, show that

$$\cos 2x = 1 - 2\sin^2 x$$

(ii) Hence show that

$$\frac{13\sin x - 2\cos 2x - 10}{4\sin x - 3} = 4 + \sin x \tag{7}$$

(b) Hence solve, in radians to 3 significant figures, the equation

$$10 + 2\cos\left(2\theta + \frac{\pi}{3}\right) - 13\sin\left(\theta + \frac{\pi}{6}\right) = 2\sin\left(\theta + \frac{\pi}{6}\right) + 8$$

for  $\pi \leqslant \theta \leqslant 2\pi$ 

(5)

(c) Find the exact value of

$$\int_0^{\frac{\pi}{2}} \left( \frac{13\sin x - 2\cos 2x - 10 + 4x\sin x - 3x}{4\sin x - 3} \right) dx \tag{5}$$

**32** 



Question 11 continued				
	J			

**Question 11 continued** 

Question 11 continued					

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**Question 11 continued** 

(Total for Question 11 is 17 marks)

**TOTAL FOR PAPER IS 100 MARKS** 

