



Pearson

Mark Scheme (Results)

Summer 2017

Pearson Edexcel International GCSE
In Mathematics B (4MB0) Paper 01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- **Types of mark**
 - M marks: method marks
 - A marks: accuracy marks
 - B marks: unconditional accuracy marks (independent of M marks)
- **Abbreviations**
 - cao – correct answer only
 - ft – follow through
 - isw – ignore subsequent working
 - SC - special case
 - oe – or equivalent (and appropriate)
 - dep – dependent
 - indep – independent
 - eeoo – each error or omission

- **No working**

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

- **With working**

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

- **Ignoring subsequent work**

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

- **Parts of questions**

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another

1	1		B1	
	0.25 or $\frac{1}{4}$ or 4^{-1}		B1	2

Total 2 marks

2	$\frac{6+20-15}{5 \times 3 \times 2}$ or $\frac{26-15}{30}$ after $\frac{3+10}{15}$ or $\frac{6+5}{30}$ after $\frac{4-3}{6}$ (oe)	M1		
	$\frac{11}{30}$		A1	2

NB: M0 A0 if no working seen.

NB: Allow M1 for $\frac{6+20+15}{30}$ oe

Total 2 marks

3 (a)	12		B1	1
	(b) $g(x) \leq 12$		B1 ft	1 2

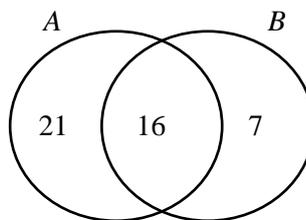
NB: (1) ft on (a)

(2) Allow $y \leq "12"$ and $g \leq "12"$ or $(-\infty, 12]$ or or $]-\infty, 12]$

Total 2 marks

4 $n(A \cup B) = n(A) + n(B) - n(A \cap B) = 37 + 23 - 16$ M1

NB: M1 for diagram oe



Or $21 + 16 + 7$

44		A1	2
Total 2 marks			

5	$\frac{40}{30}$ or $1\frac{1}{3}$ or 1 h 20 mins or 1.33 or better	M1		
	16 05 or 4.05 pm (allow 4.05 but not 4.05am)		A1	2

Total 2 marks

6 labelled diagram showing correct angle at A or B with $180 \leq \text{angle at B} \leq 270$

OR $235^\circ - 180^\circ$

OR $180^\circ - 125^\circ$

M1

55, 055, N55E, N55°E

A1

2

Total 2 marks

7 $2(-3)^3 + 7(-3)^2 + k(-3) - 30 = 0$ ($-54 + 63 - 3k - 30 = 0$)

M1

(OR method leading to a correct linear equation in k , e.g.

$$x+3 \overline{) 2x^2 + x + (k-3)}$$

requires $-30 - 3(k-3) = 0$ oe (M1)

(OR comparing coefficients: $(x+3)(ax^2 + bx + c) = 2x^3 + 7x^2 + kx + c$

with $a = 2$, $3a + b = 7$ ($b = 1$), $3c = -30$ ($c = -10$), $k = 3b + c$ oe (M1))

$k = -7$

A1

2

Total 2 marks

8 (a) 2

B1

1

(b) 2

B1

1

2

Total 2 marks

9 Probability = $((1 \times) \frac{9}{39} \times \frac{8}{38}$ oe or $\left(\frac{10}{40} \times \frac{9}{39} \times \frac{8}{38}\right)$ ($\times n$) [n is an integer] M1

$\frac{72}{1482}$, $\frac{12}{247}$, oe or awrt 0.049, awrt 4.9%

A1

2

SC: $4\left(\frac{1}{4}\right)^3$ oe or $1 \times \frac{1}{4} \times \frac{1}{4}$ ($= \frac{1}{16}$ [must see working]) scores M1 A0

Total 2 marks

10 Breaking 432 into $(144) \times 3$ or $(16) \times 27$ AND 243 into $(81) \times 3$ or $(9) \times 27$ where bracketed number may be written as a product

OR 432 AND 243 as a product of prime factors ($432 = 2^4 \times 3^3$, $243 = 3^5$) M1

$$\sqrt{(3 \times 2^2)^2 \times 3} - \sqrt{9^2 \times 3} \text{ or } (3 \times 2^2)\sqrt{3} - 9\sqrt{3} \text{ or } 4\sqrt{27} - 3\sqrt{27}$$

oe, e.g. (from working) $12\sqrt{3} - 9\sqrt{3} (= 3\sqrt{3})$ [manipulating both surds correctly]

NB: $12\sqrt{3} - 9\sqrt{3}$ or $3\sqrt{3}$ with no working gains M0M0A0 M1 (DEP)

$$\sqrt{27} \text{ or } n = 27 \quad \text{A1} \quad \mathbf{3}$$

Total 3 marks

11 $AP \times 9 = 6 \times 3$ or $AP = 2$ or $9 + 2 (= 11)$ M1

$$r = \frac{9 + "AP"}{2} \quad \text{M1 (DEP)}$$

$$r = 5.5, \quad 5\frac{1}{2}, \quad \frac{11}{2} \quad \text{A1} \quad \mathbf{3}$$

Total 3 marks

12 $x^2 - 4x - x + 4 (= -2)$ or $x^2 - 5x + 4 (= -2)$ or $x^2 - 5x + 6 (= 0)$

(oe, expanding with at least three terms from $x^2, -4x, -x, +4$ correct) M1

(Factorising any 3 term quadratic)

$$(x-2)(x-3)(=0) \text{ or } \frac{5 \pm \sqrt{25 - 4 \times 1 \times 6}}{2} \text{ oe} \quad \text{M1}$$

Or factorising which when expanded, the result must give at least 2 of their 3 terms from their trinomial, e.g. $(x-6)(x-1)(=0)$ will give x^2 and $+6$ terms

$$x = 2, 3 \quad (\text{cao dependent on M1 earned earlier}) \quad \text{A1} \quad \text{cao} \quad \mathbf{3}$$

Total 3 marks

13 $\frac{\sin \angle ACB}{5} = \frac{\sin 40}{6}$ oe M1

$$\angle ACB = \sin^{-1}\left(\frac{5 \times \sin 40}{6}\right) (\sin^{-1}((0.535)656341..)) \quad \text{M1 (DEP)}$$

$$\angle ACB = 32.3 - 32.4 \quad (32.3884...) \quad \text{A1} \quad \mathbf{3}$$

Total 3 marks

14 $(9-5):(x-5) = 2:5$ oe or $2:5 = 4:10$ or car B was 10 (yrs) M1

$$\frac{9-5}{x-5} = \frac{2}{5} \text{ oe, e.g. } 2x - 10 = 20 \text{ or } 10 + 5 \quad \text{M1}$$

$$x = 15 \quad \text{A1} \quad \mathbf{3}$$

SC B1 for $5 \times 14 = 10 + 2x$, $x = 30$ (5 yrs time)[working needed]

Total 3 marks

$$15 \quad \overline{AP} = \frac{1}{2} \begin{pmatrix} 6 \\ 2 \end{pmatrix} (= \begin{pmatrix} 3 \\ 1 \end{pmatrix}) \quad \text{M1}$$

$$\overline{OP} = \overline{OA} + \overline{AP} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 3 \\ 1 \end{pmatrix} \quad \text{M1(DEP)}$$

OR C is the point $(6 + 1, 2 + 1) [= (7, 3)]$ or $OC = \begin{pmatrix} 7 \\ 3 \end{pmatrix}$ (M1)

P is the mid-point of AC so P is $\left(\frac{7+1}{2}, \frac{3+1}{2}\right)$ (M1)

$(4, 2)$ A1 **3**

Total 3 marks

$$16 \quad \frac{1}{b} = \frac{2}{c} - \frac{1}{a} \text{ or } -\frac{1}{b} = \frac{1}{a} - \frac{2}{c} \quad \text{M1}$$

$$\frac{1}{b} = \frac{2a-c}{ac} \text{ or } b = \frac{1}{\left(\frac{2a-c}{ca}\right)} \text{ or } b = \frac{1}{\left(\frac{2}{c} - \frac{1}{a}\right)} \text{ oe (positive } b) \quad \text{M1}$$

[OR $ca = 2ab - bc$ oe (remove denominators and collect terms in b) (M1)

$ca = b(2a - c)$ (factorises) (M1)]

NB: Allow a maximum of 1 sign slip in the 2 M marks

$$b = \frac{ac}{2a-c} \text{ or } b = \frac{-ac}{c-2a} \quad \text{A1 **3**}$$

Total 3 marks

$$17 \text{ (i)} \quad \left. \begin{array}{l} 84 = 2^2 \times 3 \times 7 \\ 126 = 2 \times 3^2 \times 7 \\ 294 = 2 \times 3 \times 7^2 \end{array} \right\} \text{(prime factors of at least 2 of 84, 126 and 294)}$$

OR $84 = 42 \times 2$
 $126 = 42 \times 3$
 $294 = 42 \times 7$ M1

OR $2^2 \times 3^2 \times 7^2$ or $2 \times 3 \times 7$

LCM = 1764	A1	2	
(ii) HCF = 42	B1	1	3

NB: The M mark can be awarded in either (i) or (ii), so if one is correct M1A1B0 or M1A0B1

Special Case: If LCM & HCF are correct but wrong way round award M1A0B1.

One correct in wrong place is M1A0B0 **Total 3 marks**

18 Numerator: $y(2w+x) - 3x(x+2w)$ OR $2w(y-3x) + x(y-3x)$ (oe) M1

Denominator: $2y(y-3x)$ M1 (INDEP)

$\frac{(2w+x)(y-3x)}{2y(y-3x)}$ A1

$\frac{2w+x}{2y}$ A1 **4**

Total 4 marks

19 (a) (i) 0.048 B1

(ii) 0.05 B1 2

(b) 1.8×10^n or $0.18 \left(\frac{9}{50}\right)$ or their attempt at $9 \div 50 \times 10^{-148}$
 or $m \times 10^{-149}$ where $0 < m \leq 10$ M1

1.8×10^{-149} A1 2 **4**

Total 4 marks

20 $6-4 < x-2x$ (oe, e.g. $2 < -x$) or for an answer of $x = -2$ or x and -2 written with wrong inequality sign M1

$4-28 \leq 2x+2x$ (oe) or for an answer of $x = -6$ or x and -6 written with wrong inequality sign M1

$x < -2$ and $x \geq -6$ oe, e.g. $-6 \leq x < -2$ A1

$-6, -5, -4, -3$ A1 **4**

Total 4 marks

21 (a) $\angle CAD = 34^\circ$	B1	1	
(b) $\angle CBD = "34"$ clearly defined (could be on diagram)	B1ft		
$\angle ABC = 124^\circ$	B1		
Angle in semicircle and Angles in the same segment (oe wording)	B1	3	4

[OR $\angle ODC = 56^\circ$ clearly defined (B1)			
$\angle ABC = 124^\circ$ (B1)			
Isosceles triangle ($\triangle OCD$) or right angled triangle (ACD) or angles in a triangle and Cyclic Quad (B1)]			
[OR $\angle AOC = 180 + 68 (= 248)$ clearly defined (B1)			
$\angle ABC = 124$ (B1)			

Straight line & angle at centre double angle at circumference (oe wording) B1]

NB: Accept angles on their diagram
 Other methods are acceptable, but reasons must be relevant to method used – at least 2 relevant correct reasons needed.

Total 4 marks

22 (a) $\begin{pmatrix} 7 & 17 \\ -15 & 14 \end{pmatrix}$	B1, B1 (-1eeoo)	2	
(b) $\begin{pmatrix} 26 & -38 \\ -38 & 31 \end{pmatrix}$	B1 (1 st row)		
	B1 (2 nd row)	2	4

Total 4 marks

23 $900 = k \times 2^2$	M1		
$k = \frac{900}{2^2}, 225$	M1 (DEP)		
[OR $k = \frac{900}{4} = \frac{36}{x^2}$ (M1)			

$x^2 = \frac{36 \times 4}{900}$	(oe)	(M1 (DEP))	
<hr/>			
$x = \sqrt{\frac{36}{225}}$ oe, e.g. $\sqrt{\frac{4}{25}}$ or $\sqrt{0.16}$ or $x = 0.4$ or $\frac{2}{5}$ oe e.g. $\frac{6}{15}$			M1 (DEP)
<hr/>			
$x = \pm \frac{2}{5}, \pm \frac{6}{15}, \pm 0.4$		A1	4

Total 4 marks

24 (a) $\frac{-2+14+18+2x+3x}{5} = \frac{5x+2}{4}$ oe e.g. $\frac{30+5x}{5} = \frac{5x+2}{4}$		M1	
<hr/>			
e.g. $4(30+5x) = 5(5x+2)$ or $24+4x = 5x+2$ oe			
i.e. correct rearrangement with no denominators		M1	
<hr/>			
$x = 22$		A1	3
<hr/>			
(b) 18		B1ft	1 4

NB: ft on “ $x = 22$ ”**Total 4 marks**

25 (a) $v = -12t + 57$	(one term correct)	M1	
<hr/>			
Correct		A1	2
<hr/>			
(b) “ $-12t + 57 = 0$ ” ft their (a) [but not displacement]		M1	
<hr/>			
$t = \frac{57}{12}, 4.75$ (s) oe, e.g. $\frac{19}{4}$		A1	2
<hr/>			
(c) $x = -6 \times \left(\frac{57}{12}\right)^2 + 57 \times \left(\frac{57}{12}\right) + 27$		M1	
<hr/>			
$x = 162.375$ accept answers in range 162 – 162.4		A1	2 6

Total 6 marks

26 (a) Triangle ABC drawn correctly.		B1	1
<hr/>			
(b)(i) Arc, radius 4 cm, centre B , drawn within triangle ABC		B1ft	
<hr/>			
(ii) Three sets of arcs of correct radii, one of which is centred at B , one centred on correct point on BC and ditto on AB		M1ft	

Angle bisector drawn so that it intersects AC	A1	3
(c) Correct region shaded or clearly indicated on correct diagram. [bordered by 3 straight lines and 1 curve]	B1ft	1 5
		Total 5 marks

27 Cosine Rule: $(x+9)^2 = 7^2 + (2x)^2 - 2 \times 7 \times (2x) \times \cos 65$

[Or $\cos 65 = \frac{(2x)^2 + 7^2 - (x+9)^2}{2 \times 7 \times 2x}$]

(Condone lack of brackets but other than this, cosine rule must be correctly stated)

B1

$x^2 + 18x + 81 = 49 + 4x^2 - 11.8x$ (expanding $(x+9)^2$ and $(2x)^2$ condone 1 error only in cosine rule for this mark

or

$$x^2 + 18x + 81 = 49 + 4x^2 - 28x \cos(65^\circ)$$

or

$$\cos 65 = \frac{4x^2 + 49 - (x^2 + 18x + 81)}{28x}$$

or

$$\cos 65 \times 28x = 4x^2 + 49 - (x^2 + 18x + 81) \text{ oe } \quad \text{M1}$$

NB: 11.8 or better can be used throughout (11.83331133...)

$$3x^2 - 29.8x - 32 (= 0) \text{ (or better ie } 29.83331\dots) \quad \text{A1}$$

$$x = \frac{-(-29.8) \pm \sqrt{(-29.8)^2 - 4 \times 3 \times (-32)}}{2 \times 3}$$

(solving a trinomial quadratic, values correctly subst'd)

M1 INDEP

$$(\sqrt{1272} \rightarrow \sqrt{1274}) (= 35.7)$$

B1

$$(x_+ = 10.9(2114), \quad x_- = -0.976(7))$$

$$x = 10.9 \text{ (given as the only answer) cao}$$

A1

6

Total 6 marks

28 (a) $\left(\frac{27}{729}\right)^{\frac{1}{3}}$ (oe, eg $\frac{1}{3}$) or as a ratio, e.g. $27^{\frac{1}{3}} : 729^{\frac{1}{3}}$ (o.e.eg 1 : 3) M1

$$\left(\frac{27}{729}\right)^{\frac{1}{3}} \times 15 \text{ oe}$$

M1 (DEP)

5 (cm)	A1	3
(b) [Finds height of C and then base area of C]		
$\left(\frac{1728}{729}\right)^{\frac{1}{3}} \times 15$	M1	
20 (cm)	A1	
Base area \times "20" = 1728 or $\pi r^2 \times 20 = 1728$ or $1728 \div 20$	M1 (DEP)	
OR [Finds radius of B, then radius of C and then base area of C]		
$(729 = \pi r_B^2 \times 15 \text{ gives } r_B = 3.93317435..)$	(M1)	
$r_C = \left(= "3.93292" \times \left(\frac{1728}{729}\right)^{\frac{1}{3}} \right) = 5.244$	(A1)	
Base area = $\pi \times r_C^2$	(M1(DEP))	
OR [Finds base area of B, then area SF (B to C) then uses these for base area of C]		
Base area of B = $\frac{729}{15} = 48.6$	(M1)	
Area scale factor = $\left(\frac{1728}{729}\right)^{\frac{2}{3}}$	(A1)	
Base area = $\frac{729}{15} \times \left(\frac{1728}{729}\right)^{\frac{2}{3}} (48.6 \times \frac{16}{9})$	(M1(DEP))	
Base area = 86.3 – 86.4 (cm ²)	A1	4 7
Total 7 marks		

NB: students who use height A can be awarded ft marks for an incorrect (a)

Volume A:C = 27:1728 (=1:64) (M1)

Height A:C = $1^{\frac{1}{3}} : 64^{\frac{1}{3}}$ (= 1: 4) (A1)

Height of C = 4 \times "5" (=20)

Base area of C = 1728 \div "20" (M1)

29 (a) Relating area to frequency e.g. by showing:

FD of 5 seen or written on top of FD axis oe

OR $2 \text{ cm} \times 2 \text{ cm square} = (\text{frequency}) 10$

OR $1 \text{ cm} \times 1 \text{ cm square} = (\text{frequency}) 2.5$

OR $10 \times 2 \text{ mm squares} = (\text{frequency}) 1$

OR $1 \times 2 \text{ mm square} = (\text{frequency}) 0.1$ B1

Passengers travelling $\leq 20 \text{ km}$: 2×20 (using FD \times width of bar)

$4 \times 10, 16 \times 2.5, 40 \times 1, 400 \times 0.1$

(i.e. method that follows from previous mark) M1

Number of passengers = 40 A1 3

(b) using FDs: number of passengers = "40" + 50 + 4 \times 15 + 3 \times 5

OR "40" + 50 + 6 \times 10 + 1.5 \times 10

OR "40" + 50 + 24 \times 2.5 + 6 \times 2.5

OR "40" + 50 + 60 \times 1 + 15 \times 1

OR "40" + 50 + 600 \times 0.1 + 150 \times 0.1

(i.e. 40 + 50 + 60 + 15) M1

Total number of passengers = 165 A1 2

(c) $\frac{75}{165}, \frac{15}{33}, \frac{5}{11}$ awrt 0.455 B1 1 6

Total 6 marks

TOTAL 100 MARKS

