

Mark Scheme (Results) Summer 2010

IGCSE

IGCSE Mathematics (4400) Paper 3H Higher Tier



Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.

For further information please call our Customer Services on + 44 1204 770 696, or visit our website at www.edexcel.com.

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our Ask The Expert email service helpful.

Ask The Expert can be accessed online at the following link:

http://www.edexcel.com/Aboutus/contact-us/

Summer 2010 Publications Code UG024290 All the material in this publication is copyright © Edexcel Ltd 2010

Summer 2010 IGCSE Mathematics (4400) Mark Scheme - Paper 3H

Apart from Questions 4(c), 16 and 21 (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Q	Working	Answer	Mark	Notes
1 a	$\frac{15}{6}$ oe or $\frac{100}{6}$ oe inc value rounded or truncated to at least 1 dp eg 16.6, 16.7		2	M1
		250		A1 cao
b	$\frac{900}{6}$ or $\frac{5}{6}$ oe inc value rounded or truncated to at least 2 dp eg 0.83		2	M1
		750		A1 cao
				Total 4 marks

2 ai	62	2	B1	cao
ii	alternate		B1	Accept 'opposite and corresponding' (need both)
				or 'opposite, angle sum of triangle = 180° and
				sum of angles on a line = 180°' (need all three)
bi	71	2	B1	cao
ii	corresponding		B1	Accept 'opposite and alternate' (need both)
				or 'opposite, angle sum of triangle = 180° and
				sum of angles on a line = 180°' (need all three)
				Total 4 marks

3 a	6	1	B1	cao
b	7	1	B1	cao
				Total 2 marks

	Q	Working	Answer	Mark		Not	tes
4	а		5 <i>n</i> + 30	1	B1		
	b		y ⁶	1	B1	cao	
	С	4x - 8 = 3		3	M1	for correct expansion of $4(x-2)$ or for either 4x = 3 + 2 or $4x = 5following 4x - 2 = 3$	M2 for $x - 2 = \frac{3}{4}$
		4x = 8 + 3 or 4x = 11			M1	for $4x = 8 + 3$ or $4x = 11$	
			$2\frac{3}{4}$ oe		A1	dep on 2 method ma	rks
							Total 5 marks

5 a	$\frac{3}{10} \times \frac{5}{6}$		2	M1	
		$\frac{15}{60}$ or $\frac{1}{4}$		A1	Accept $\frac{3}{12}$, $\frac{5}{20}$
b		24	2	B2	B1 for multiple of 24
					Total 4 marks

	Q	Working	Answer	Mark		Notes
6	а		400 < <i>V</i> ≤ 500	1	B1	Accept 400-500
	b	50 × 2 + 150 × 4 + 250 × 6 + 350 × 18		4	M1	for finding at least 4 products
		+ 450 × 44 + 550 × 6				$m \times f$ consistently within
		= 100+600+1500+6300+19 800+3300				intervals (inc end points)
		= 31 600			M1	(dep) for use of at least 4 correct halfway values
		31 600 ÷ 80			M1	(dep on 1st M1) for adding and ÷ by 80
			395		A1	
	С		2 6 12 30 74 80	1	B1	cao
	d		Points correct	2	B1	<u>+</u> ½ sq ft from sensible table
			Curve or line segments		B1	ft from points if 4 or 5 correct
						or if points are plotted
						consistently within each interval
		_				at the correct heights
	е	Use of 40 (or 40.5) on graph or 40		2	M1	for use of 40 (or 40.5) on cf graph
		(or 40.5) stated				or for 40 (or 40.5) stated
			approx 420		A1	If M1 scored, ft from cf graph
						If no indication of method, ft
						only from correct curve & if
						answer is correct
						(<u>+</u> ½ sq tolerance) award M1 A1
						Total 10 marks

Q	Working	Answer	Mark			Notes
7	cos and 41		3	M1	or M1 for	or M1 for correct
	6.8 cos 41°			M1	6.8sin41°	statement of
					(4.461) and	Sine Rule eg
					6.8^2 –	6.8 <i>x</i>
					"4.461" ²	$\frac{1}{\sin 90^{\circ}} = \frac{1}{\sin 49^{\circ}}$
					(26.337)	M1 for correct
					M1 for	expression for x
					√"26.337"	eg
						$X = \frac{6.8 \sin 49^{\circ}}{\sin 90^{\circ}}$
		5.13		A1	for ans rounding	to 5.13 (5.132025)
						Total 3 marks

8	$\frac{1786}{0.76}$ or $1786 \times \frac{100}{76}$ oe		3		for $\frac{1786}{0.76}$ or $1786 \times \frac{100}{76}$ oe M1 for $\frac{1786}{76}$, $76\% = 1786$, $\frac{1786}{x} = 0.76$, $1786 = 0.76x$ or 23.5 seen	
		2350		A1	cao	
					Tot	al 3 marks

Q	Working	Answer	Mark		Notes	
9 a		reflection in the line $y = -x$	2	B2	B1 for reflection	These marks are
					B1 for $y = -x$ oe	independent
					[accept eg	but award no marks
					"in dotted line"	if the answer is not a
					or "in line through	single transformation
					(-5,5) and (5, -5)"]	
b		R correct	2	B2	B1 for 2 vertices correct	
	\	/ertices are (2,-1)(3,-1)(3,-3)			or for a translation of ${f R}$	
					or for a 90° clockwise ro	tation of Q about (-1,1)
С		reflection in the line $y = 1$	2	B2	B1 for reflection	As in (a)
					B1 for $y = 1$ oe	
					[accept eg "in a	
					horizontal line	
					through (0,1)]	
					ft from (b),	
					if B1 scored in (b)	
			·			Total 6 marks

10 a		-4 ≤ <i>x</i> < 3	2	B2	Also accept ' $x < 3$ and $x > -4$ '
					B1 for $-4 \le x \le 3$, $-4 < x < 3$,
					$-4 < x \le 3$, a double-ended inequality
					which is correct at one end
					(ignore the other end)
					Also award B1 for $x \ge -4$, $x < 3$,
					' <i>x</i> < 3 <u>or</u> <i>x</i> ≥ −4'
bi	2x > - 8		4	M1	for $2x > -8$ or $x + 4.5 > 0.5$
		x > -4		A1	for $x > -4$ as final answer
ii		-3 -2 -1	2	B2	B1 for 3 correct and 1 wrong
					or for 2 correct and none wrong
					Total 6 marks

Q	Working	Answer	Mark		Notes
11 a	$\pi \times 8^2$		2	M1	
		201		A1	for ans rounding to 201
					$(\pi \to 201.061 \ 3.14 \to 200.96)$
b	eg 8.5870 × 587.71		2	M1	for correct evaluation of
					at least 2 of the terms inside
					the brackets (126.75, 192, 268.96
					accept if rounded or truncated to at least 3sf)
					or for correct evaluation of brackets
					(587.71 - accept 587, 588 or 587.7)
		5050		A1	Accept any answer
				in the range 5040-5050 inclusive.	
					$(\pi \to 5046.677\ 3.14 \to 5044.119)$
					Total 4 marks

12 a		18 13 2 -9 -14	2	B2	for all correct
					B1 for 3 or 4 correct
b		Points	2	B1	<u>+</u> ½ sq ft from (a) if at least B1 in (a)
		Curve		B1	ft if B1 awarded for points or if
					there is not more than
					one point incorrectly plotted and
					at least B1 scored in (a)
					Award for single curve (not line segments)
					which does not miss.
					more than one plotted point
					by more than ½ square
ci		$3x^2 - 12$	4	B2	B2 for $3x^2 - 12$
					B1 for two of three terms
					differentiated correctly
ii	$3 \times 5^2 - 12$			M1	for substn $x = 5$ in their (c)(i) if at least B1
					scored in (c)(i)
		63		A1	cao cao
					Total 8 marks

Q	Working	Answer	Mark		Notes		
13	There are 4 independent requirements to consider when marking this question but the order in which						
	they are satisfied wi	II vary. Focus on these 4 key po	oints, igno	oring irre	elevant or incorrect statements.		
	$\angle PQS = 36^{\circ} \text{ or } \angle SPR = 54^{\circ}$		4	B1	May be stated or marked on diagram		
	angles in the same segment			B1	Award if 'same segment', 'same arc', or 'same chord'		
	$\angle PQR = 90^{\circ} \text{ or } \angle PSR = 90^{\circ}$ and angle in a semicircle is a right angle			B1	Angle may be stated or marked on diagram. Condone omission of 'is a right angle' oe.		
		54		B1	Ca0		
					Total 4 marks		

14 ai		15	2	B1	Cao Cao
ii	i	8.25		B1	cao
b	$\frac{1}{2}$ ×"15"×"8.25"		2	M1	
		61.875		A1	Also accept 61.88
С	"8.25"		3	M1	numerator "8.25"
	25			M1	denominator 25
		0.33		A1	cao
					Total 7 marks

Q	Working	Answer	Mark		Notes
15 a	$E = \frac{k}{r^2}$		3	M1	for $E = \frac{k}{r^2}$
					but not for $E = \frac{1}{r^2}$
	$4 = \frac{k}{50^2}$			M1	
		$\frac{10000}{r^2}$		A1	Award 3 marks if answer is $E = \frac{k}{r^2}$
					but <i>k</i> is evaluated as 10 000 in <i>any</i> part
b		25	1	B1	ft from $\frac{"10000"}{400}$ except for $k = 1$,
					if at least M1 scored in (a)
С	$r^2 = \frac{10000}{1600}$ oe		2	M1	for substitution and rearrangement into form
					$r^2 = \frac{k}{1600}$ or $r = \frac{\sqrt{k}}{40}$ with their value of k
					except for <i>k</i> = 1
		2.5 oe		A1	Cao
					Total 6 marks

16	eg $9 - 3\sqrt{5} - 3\sqrt{5} + \sqrt{5}^2$	2	B2	B1 for $9 + \sqrt{5}^2$ or $9 + \sqrt{5}\sqrt{5}$
	$9-2\times3\sqrt{5}+\sqrt{5}^2$			or $9 + \sqrt{25}$ or $3^2 + \sqrt{5}^2$
				or $3^2 + \sqrt{5}\sqrt{5}$ or $3^2 + \sqrt{25}$
				B1 for $-3\sqrt{5} - 3\sqrt{5}$
				or for $-2 \times 3\sqrt{5}$
				Total 2 marks

Q	Working	Answer	Mark	Notes
17	$\frac{18}{12}$ or 1.5 oe or 18 : 12 oe		3	M1 for $\frac{18}{12}$ or 1.5 oe or 18 : 12 oe
				Also award for $\frac{12}{18}$ or $\frac{2}{3}$
				or 12 : 18 oe
	544 × 1.5 ²			M ₁ for 1.5^2 or 2.25 or $\frac{9}{4}$ or $9:4$ oe
				Also award for $\left(\frac{2}{3}\right)^2$ or $\frac{4}{9}$
				or 4 : 9 oe
		1224		A1 cao
				Total 3 marks

18	<i>X</i> (<i>X</i> + 6)		3	B1	for $x(x + 6)$
	$\frac{x(x+6)}{(x+6)(x-6)}$				Accept (x + 0)(x + 6)
	$(\lambda + 0)(\lambda - 0)$			B1	for $(x + 6)(x - 6)$
		Х		B1	cao
		${x-6}$			
					Total 3 marks

Q	Working	Answer	Mark		Notes	
19 a	$\frac{3}{6} \times \frac{3}{6}$		2	M1	for $\frac{3}{6} \times \frac{3}{6}$ oe	
		$\frac{9}{36}$ or $\frac{1}{4}$ oe		A1	Sample space method -	
		30 4			award 2 marks for a cor otherwise no marks	rect answer,
b			3	M1	for one of	SC
	$\frac{1}{6} \times \frac{5}{6} + \frac{2}{6} \times \frac{3}{6}$				$\frac{1}{6} \times \frac{5}{6}, \frac{2}{6} \times \frac{3}{6},$	M1 for one of
	or $\frac{1}{6} \times \frac{2}{6} + \frac{1}{6} \times \frac{3}{6} + \frac{2}{6} \times \frac{3}{6}$				$\frac{1}{6} \times \frac{2}{6}, \frac{1}{6} \times \frac{3}{6},$	$\frac{1}{6} \times \frac{2}{5}, \frac{1}{6} \times \frac{3}{5},$
	or $\frac{3}{6} \times \frac{3}{6} + \frac{1}{6} \times \frac{2}{6}$				$\frac{3}{6} \times \frac{3}{6}$	$\frac{2}{6} \times \frac{3}{5}$
				M1	for sum of 2 or	M1 for
					3 products which, evaluated accurately,	$\frac{1}{6} + \frac{2}{6} \times \frac{3}{5} \text{ or}$
					gives the correct answer	$\frac{1}{6} \times \frac{2}{5} + \frac{1}{6} \times \frac{3}{5}$
						$+\frac{2}{6} \times \frac{3}{5}$
		$\frac{11}{36}$		A1	Sample space method - award 3 marks for a cor otherwise no marks.	
					Accept 0.305, 0.30, 0.3 but not 0.3	31, 0.305, 0.306 etc
						Total 5 marks

Q	Working	Answer	Mark		Notes
20	13° or 19° angle of elevation identified		6	B1	On diagram or implied by working
				M1	for 40 tan 13° or 9.2347
					rounded or truncated to at least 2 sf
					or any complete, correct method of finding
					the height of the flagpole
	$tan 19^{\circ} = \frac{"9.2347"}{BC}$			M1	or for $\tan 71^\circ = \frac{BC}{"9.2347"}$
	(BC) "9.2347" 40 tan13°			M1	for correct expression for BC,
	$(BC =) \frac{"9.2347"}{\tan 19^{\circ}} \text{ or } \frac{40 \tan 13^{\circ}}{\tan 19^{\circ}}$				which need not be evaluated
	or 26.819				eg also accept 40 tan 13° tan 71°
					If evaluated, accept 26.7 or 26.8
					or any value which rounds to 26.7 or 26.8
					$(\frac{9.2}{\tan 19^{\circ}} \rightarrow 26.718$
					$(\frac{1}{\tan 19^{\circ}} \rightarrow 20.710$
					$\frac{9.23}{\text{tan19}^{\circ}} \rightarrow 26.805)$
	40 ² +"26.819" ²			M1	dep on first two M1s
					for 40 ² +"26.819" ²
					or for complete, correct method of
					finding length of AC
		48	2	A1	for ans rounding to 48.2
					(48.1590)
					Award 6 marks for an answer
					which rounds to 48.2,
					if it has been obtained
					by a mathematically correct method
					Total 6 marks

Q	Working	Answer	Mark	Notes
21	$2x^2 = 3x + 14$ May be implied by second M1		5	$M1 y = 2\left(\frac{y-14}{3}\right)^2$
	$2x^2 - 3x - 14 (= 0)$			$M1 2y^2 - 65y + 392 = 0$
	$(2x-7)(x+2)(=0)$ or $\frac{3\pm\sqrt{121}}{4}$			M1 $(2y-49)(y-8)(=0)$
	$(2x-7)(x+2)(=0)$ or $\frac{3\pm\sqrt{121}}{4}$ or $\frac{3}{4}\pm\frac{\sqrt{121}}{4}$			or $\frac{65 \pm \sqrt{1089}}{4}$
				or $\frac{65}{4} \pm \frac{\sqrt{1089}}{4}$
		$x = \frac{7}{2}, \ x = -2$		A1 dep on all method marks
		2		$y = \frac{49}{2}$, $y = 8$
				A1 dep on all method marks
		$x = \frac{7}{2}, \ y = \frac{49}{2}$ $x = -2, \ y = 8$		$X = \frac{7}{2}, \ \ Y = \frac{49}{2}$
		x = -2, y = 8		x = -2, y = 8
				Total 5 marks

Total 100 marks



Further copies of this publication are available from International Regional Offices at www.edexcel.com/international

For more information on Edexcel qualifications, please visit www.edexcel.com
Alternatively, you can contact Customer Services at www.edexcel.com/ask or on + 44 1204 770 696

Edexcel Limited. Registered in England and Wales no.4496750 Registered Office: One90 High Holborn, London, WC1V 7BH