

## IGCSE Edexcel IGCSE Mathematics - Higher (4400)

November 2006

Mark Scheme

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	estion No.	Working	Answer	Mark		Notes
1	а		$290 \pm 2$	2	B2	B1 for $290 \pm 5$ or $360 - 70$
	b	226 - 180		2	M1	
			046		A1	Condone omission of 0
						Total 4 mark

2	a	x + x + x +	x + x + x or $6x$	2	B1	
		x + 7 + x + 7 + x + 7 + x + 7 or $4(x + 7)$ or $4x + 28$			B1	
	bi	6x'' = 4(x + 7)''		4	M1	
	ii	6x = 4x + 28			M1	
		6x - 4x = 28 oe			M1	
			14		A1 cao	
					Total 6 mark	٢S

3	$100 \times 1.80 \text{ or } 180$		6	M1
	$60 \times 4.00 \text{ or } 240$			M1
	4.00 ÷ 5 or 0.8(0) or 3.2(0)			M1 may be part of an expression
	35 × 3.20 or 112			M1
	"240" + "112" – "180"			M1 dep on at least 2 of previous 4 M marks
		172		A1 cao
				Total 6 marks

4 a	$\frac{150 \pm 2}{360} \text{ oe inc } \frac{5}{12}, 0.42, 0.41\dot{6}, 0.417$		2	B1 B1	numerator = $150 \pm 2$ denominator = $360$
b	10×30+12×12+14×18+17×60 or 300+144+252+1020 or 1716		4	M1	finds products $f \times x$ consistently within intervals (inc end points) & sums them
	use of at least 3 midpoints			M1	
	<u>"1716"</u> <u>120</u>			M1	(dep on 1st M1) for division by $\Sigma f$
		14.3		A1	Accept 14 if all M marks scored
					Total 6 marks

5	$\frac{48}{60}$ or $60 - 48$		3	M1
	80 or $\frac{"12"}{60}$			M1
		20		A1 cao
				Total 3 marks

6	$240 \times \frac{5}{2}$		2	M1
		600		A1 cao SC B1 for $240 \times \frac{2}{5}$ or 96
				Total 2 marks

7	4x < 6 or $-6 < -4x$		3	M1 correctly collects x terms
				M1 correctly collects constants
		x < 1.5 oe		A1
				Total 3 marks

8	0.5 + 0.1 or $0.5 + 0.1 + 0.3or table completed with 0.1$		3	M1
	1-(0.5+0.1)  or 1-(0.5+0.1+0.3) + 0.3			M1
		0.4		A1
				Total 3 marks

9 a	BM = 5 seen or implied		4	B1
	$13^2 - 5^2$ or 144			M1 for squaring and subtracting Accept $13^2 - 10^2$ or 69
	$\sqrt{13^2-5^2}$			M1 for $\sqrt{13^2 - 5^2}$ only
		12		A1 cao
b	$\frac{1}{2} \times 10 \times "12"$		4	M1 for $\frac{1}{2} \times 10 \times$ their (a)
	× 4			M1 dep on first M1
	$10 \times 10$ or 100			M1 indep
		340		A1 ft from "12"
				Total 8 marks

10	Q correct		4	B1		
	R correct			B1	ft from Q	
		Reflection		B1		ft from <b>R</b> if at least
		y = x		B1	Accept eg in dotted line but, if stated, equation must be correct	one transformation correct
						Total 4 marks

11 a	1 2 2 2 5 5 5 5 5 6 6 6 6 7 9		3	M1
	Attempt to find 4th (or 3 <sup>3</sup> / <sub>4</sub> th)			M1
	& 12th (or 11 <sup>1</sup> / <sub>4</sub> th) values			
		4		A1 cao
bi	eg B had higher marks than A		2	B1 B0 if median for A seen and $\neq 5$
ii	eg B less spread or more consistent			B1
				Total 5 marks

12	а	Attempt to find $\frac{\text{vert}}{\text{horiz}}$ for line PQ		4	M1	
		(gradient =) 2			A1	$(y =) 2x \Rightarrow M1A1$
			y = 2x - 4		B2	ft from "2" B1 for $2x - 4$ B1 for $y = mx - 4$ where $m \neq 2$
	b	Line through (0, 1)		3	M1	
		Attempts grad $-\frac{1}{2}$ or correctly finds			M1	
		coordinates of another point				
			Correct line		A1	Passes within 1mm of $(-2, 2)$ and $(2, 0)$
						Total 7 marks

13 a	$\frac{1}{8}$	1	B1	
b	$\frac{3}{7}$	1	B1	Accept equivalent
с	<del>9</del> 64	1	B1	fractions
				Total 3 marks

14	а		5000 -1250x	2	B2	B1 for 5000 B1 for -1250x
	b	5000 - 1250x = 0		3	M1	
		x = 4			M1	ft from a if at least B1 scored
			4 10 000		A1	and a is linear
	ci		max	2	B1	independent
	ii	coeff of $x^2 < 0$ or $\frac{dy}{dx} > 0$ for x value < 4 and $\frac{dy}{dx} > 0$ for x value > 4 or y < 10 000 for x value < 4 and for x value > 4 or $\frac{d^2y}{dx^2} = -1250 < 0$	d alue		B1	
	di		4	2	B1	ft from b if at least 1 scored
	ii		max profit oe		B1	Accept eg largest profit
						Total 9 marks

15	$\frac{4}{3}\pi\times3^3\div2\ +\ \frac{1}{3}\pi\times3^2\times10$		4	M1	for $\frac{4}{3}\pi \times 3^3 \div 2$ or value rounding to 56.5 or 56.6
				M1	for $\frac{1}{3}\pi \times 3^2 \times 10$ or value rounding to 94.2 or 94.3
				M1	for sum (dep on first two M marks)
		151		A1	for 151 or better (150.796) ( $3.14 \rightarrow 56.52 + 94.2 = 150.72$ )
					Total 4 marks

16 i	$B \subset A$	2	B1	cao
ii	$A \cap B = \emptyset$		B1	cao
				Total 2 marks

		$\frac{x-(x-1)}{x-1}$ $x-(x-1)$ $x-(x-1)$				сао	evaluated correctly for two values of x and an answer of x
		$\frac{\frac{x}{x-1}}{\frac{x-(x-1)}{x-1}}  \text{or } \frac{x}{x-(x-1)}  \text{oe}$			M1		SC B1 for ff(x)
	ci	$\frac{\frac{x}{x-1}}{\frac{x}{x-1}-1}$		4	M1		
	b		1	1	B1	cao	
	ii		$\frac{3}{4}$ oe		B1	Don't accept $\frac{-3}{-4}$	
17	ai		$1\frac{1}{2}$ oe	2	B1		

18	$x^2 = 2x + 15$		5	$M1 \qquad \left(\frac{y-15}{2}\right)^2 = y$
	$x^2 - 2x - 15 = 0$			M1 $y^2 - 34y + 225 = 0$
	$(x+3)(x-5) = 0 \ x = \frac{2\pm 8}{2}$			M1 $(y-25)(y-9) = 0$
	x = -3  or  x = 5			A1 $y = 9 \text{ or } y = 25$
		-3, 9 and 5,25		A1
				Total 5 marks

19	а		7 – x	1	B1
	b	8 - x seen or 9, 13, 6 marked correctly on diagram or $50 - (10 + 9 + 13 + 6) = 50 - 38 = 12$ and $8 + 7 = 15$		3	M1
		10+13+9+6+(7-x)+(8-x)+x=50 oe inc $7-x+8-x+x=12$ or $15-12$			M1 equation must be correct
			3		A1
					Total 3 marks

20	a		1: √ <i>k</i>	1	B1 Accept $\sqrt{k}$
	b	$\sqrt{2}$ or $\sqrt{\frac{1}{2}}$ seen		2	M1
			7.1		A1 $\begin{array}{c} \text{for 7.1 or better (7.071)} \\ \text{Accept } \sqrt{50} \end{array}$
					Total 3 marks

21	а		3n oe	1	B1	Accept eg n + 2n
	b	n - 1, 3n - 1 seen		5	B2	B1 for each
		$\frac{1}{3} \times \frac{n-1}{3n-1} = \frac{1}{10} \text{ oe inc } \frac{n}{3n} \times \frac{n-1}{3n-1} = \frac{1}{10}$			M1	for correct equation
		10(n-1) = 3(3n-1) oe inc $10n(n-1) = 3n(3n-1)$			M1	for correctly removing fractions
		(n = 7)	21		A1	cao
						Total 6 marks
						Total 100 marks

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