## IGCSE

## Edexcel IGCSE

Mathematics - Higher (4400)

November 2006

Mark Scheme

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## IGCSE Maths November 2006 - Paper 3H Final Mark Scheme

| Question <br> No. | Working | Answer | Mark | Notes |
| :---: | :--- | :--- | :--- | :--- |
| 1 | a |  | $290 \pm 2$ | 2 |
| b | $226-180$ |  | 2 | M1 |
|  |  | 046 |  | A1 for $290 \pm 5$ or $360-70$ |
|  |  |  |  |  |



| 3 | $100 \times 1.80$ or 180 |  | 6 | M1 |
| :--- | :--- | :--- | :--- | :--- |
|  | $60 \times 4.00$ or 240 |  |  | M1 |
|  | $4.00 \div 5$ or $0.8(0)$ or $3.2(0)$ |  |  | M1 may be part of an expression |
|  | $35 \times 3.20$ or 112 |  |  | M1 |
|  | "240" + " 112 " - " 180 " |  | M1 dep on at least 2 of previous 4 M marks |  |
|  |  | 172 |  | A1 cao |
|  |  |  |  | Total 6 marks |


| 4 | a | $\frac{150 \pm 2}{360}$ oe inc $\frac{5}{12}, 0.42,0.416,0.417$ | 2 | B1 <br> B1 | numerator $=150 \pm 2$ <br> denominator $=360$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| b | $10 \times 30+12 \times 12+14 \times 18+17 \times 60$ <br> or $300+144+252+1020$ or 1716 |  | 4 | M1finds products $f \times x$ consistently within intervals (inc <br> end points) $\&$ sums them |  |
|  | use of at least 3 midpoints |  |  | M1 |  |
|  | $\frac{\text { " } 1716 "}{120}$ |  |  | M1 $\quad$ (dep on 1 st M1) for division by $\Sigma \mathrm{f}$ |  |
|  |  | 14.3 |  | A1 | Accept 14 if all M marks scored |
|  |  |  |  |  | Total 6 marks |


| 5 | $\frac{48}{60}$ or $60-48$ |  | 3 | M1 |
| :--- | :--- | :--- | :--- | :--- |
|  | 80 or ' $\frac{12 "}{60}$ |  |  | M1 |
|  |  | 20 |  | A1 $\quad$ cao |
|  |  |  |  |  |


| 6 | $240 \times \frac{5}{2}$ |  | 2 | M1 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 600 |  | A1 $\quad$ cao SC B1 for $240 \times \frac{2}{5}$ or 96 |  |
|  |  |  |  |  | Total 2 marks |


| 7 | $4 x<6$ or $-6<-4 \mathrm{x}$ |  | 3 | M1 | correctly collects x terms |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | M1 | correctly collects constants |
|  |  | $\mathrm{x}<1.5$ oe |  | A1 |  |
|  |  |  |  |  | Total $\mathbf{3}$ marks |


| 8 | $0.5+0.1$ or $0.5+0.1+0.3$ <br> or table completed with 0.1 |  | 3 | M1 |
| :--- | :--- | :--- | :--- | :--- |
|  | $1-(0.5+0.1)$ or1 $-(0.5+0.1+0.3)+0.3$ |  |  | M1 |
|  |  | 0.4 |  | A1 |
|  |  |  |  |  |


| 9 a | $\mathrm{BM}=5$ seen or implied |  | 4 | B1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $13^{2}-5^{2}$ or 144 |  |  | M1 for squaring and subtracting |  |
|  | $\sqrt{13^{2}-5^{2}}$ |  |  | M1 for $\sqrt{13^{2}-5^{2}}$ only |  |
|  |  | 12 |  | A1 cao |  |
| b | $\frac{1}{2} \times 10 \times 112$ " |  | 4 | M1 for $\frac{1}{2} \times 10 \times$ their (a) |  |
|  | $\times 4$ |  |  | M1 dep on first M1 |  |
|  | $10 \times 10$ or 100 |  |  | M1 indep |  |
|  |  | 340 |  | A1 ft from "12" |  |
|  |  |  |  |  | Total 8 marks |


| 10 | Q correct |  | 4 | B1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | R correct |  |  | B1 | ft from Q |  |
|  |  | Reflection |  | B1 |  | ft from $\mathbf{R}$ if at least one transformation correct |
|  |  | $y=x$ |  | B1 | Accept eg in dotted line but, if stated, equation must be correct |  |
|  |  |  |  | Total 4 marks |  |  |


| $11 \quad$ a | 122255555666679 |  | 3 | M1 |
| ---: | :--- | :--- | :--- | :--- |
|  | Attempt to find 4th (or 33/th) <br> \& 12th (or 111⁄4th) values |  | M1 |  |
|  |  | 4 |  | A1 $\quad$ cao |
| bi | eg B had higher marks than A |  | 2 | B1 $\quad$ B0 if median for A seen and $\neq 5$ |
| ii | eg B less spread or more consistent |  |  | B1 |
|  |  |  |  | Total 5 marks |


| 12 a | Attempt to find $\frac{\text { vert }}{\text { horiz }}$ for line PQ |  | 4 | M1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (gradient =) 2 |  |  | A1 | ( $\mathrm{y}=$ ) $2 \mathrm{x} \Rightarrow \mathrm{M} 1 \mathrm{~A} 1$ |
|  |  | $y=2 x-4$ |  | B2 | $\begin{aligned} & \text { ft from " } 2 \text { " B1 for } 2 \mathrm{x}-4 \\ & \text { B1 for } \mathrm{y}=\mathrm{mx}-4 \text { where } \mathrm{m} \neq 2 \\ & \hline \end{aligned}$ |
| b | Line through (0, 1) |  | 3 | M1 |  |
|  | Attempts grad $-1 / 2$ or correctly finds coordinates of another point |  |  | M1 |  |
|  |  | Correct line |  | A1 | Passes within 1 mm of $(-2,2)$ and ( 2,0 ) |
|  |  |  |  |  | Total 7 marks |


| 13 | a |  | $\frac{1}{8}$ | 1 | B1 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| b |  | $\frac{3}{7}$ | 1 | B1 | Accept <br> equivalent <br> fractions |
| c |  | $\frac{9}{64}$ | 1 | B1 | Total 3 marks |
|  |  |  |  |  |  |


| 14 a | 5000-1250x | 2 | B2 | B1 for 5000 B1 for $-1250 x$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| b | $5000-1250 x=0$ | 3 | M1 | ft from a <br> if at least B1 scored and a is linear |  |
|  | $\mathrm{x}=4$ |  | M1 |  |  |
|  | 410000 |  | A1 |  |  |
| ci | max | 2 | B1 | independent |  |
| ii | coeff of $x^{2}<0$ or $\frac{d y}{d x}>0$ for $x$ value $<4$ and $\frac{d y}{d x}>0$ for $x$ value $>4$ or $y<10000$ for $x$ value $<4$ and for $x$ value $>4$ or $\frac{d^{2} y}{d x^{2}}=-1250<0$ |  | B1 |  |  |
| di | 4 | 2 | B1 | ft from b if at least 1 scored |  |
| ii | max profit oe |  | B1 | Accept eg largest profit |  |
|  |  |  |  |  | Total 9 marks |


| 15 | $\frac{4}{3} \pi \times 3^{3} \div 2+\frac{1}{3} \pi \times 3^{2} \times 10$ |  | 4 | M1for $\frac{4}{3} \pi \times 3^{3} \div 2$ <br> or value rounding to 56.5 or 56.6 |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | M1for $\frac{1}{3} \pi \times 3^{2} \times 10$ <br> or value rounding to 94.2 or 94.3 |
|  |  |  |  | M1for sum (dep on first two M marks) |
|  |  | 151 |  | A1for 151 or better $(150.796 \ldots)$ <br> $(3.14 \rightarrow 56.52+94.2=150.72)$ |
|  |  |  |  |  |


| 16 | i |  | $\mathrm{B} \subset \mathrm{A}$ | 2 |
| ---: | ---: | ---: | ---: | ---: |
| B 1 | cao |  |  |  |
| ii |  | $\mathrm{A} \cap \mathrm{B}=\varnothing$ |  | B 1 |
|  |  |  |  |  |


| 17 ai |  | $1 \frac{1}{2}$ oe | 2 | B1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ii |  | $\frac{3}{4} \text { oe }$ |  | B1 | Don't accept $\frac{-3}{-4}$ |  |
| b |  | 1 | 1 | B1 | cao |  |
| ci | $\frac{\frac{x}{x-1}}{\frac{x}{x-1}-1}$ |  | 4 | M1 |  |  |
|  | $\frac{\frac{x}{x-1}}{\frac{x-(x-1)}{x-1}} \text { or } \frac{x}{x-(x-1)} \text { oe }$ |  |  | M1 |  | SC B1 for $\mathrm{ff}(\mathrm{x})$ evaluated correctly for two values of $x$ and an answer of x |
|  |  | X |  | A1 | cao |  |
| ii | eg $f$ is its own inverse, $\mathrm{f}^{-1}=\mathrm{f}$ |  |  | B1 dep on correct ci | dep on correct ci |  |


| 18 | $x^{2}=2 x+15$ |  | 5 | M1 $\left(\frac{y-15}{2}\right)^{2}=y$ |
| :--- | :--- | :--- | :--- | :--- |
|  | $x^{2}-2 x-15=0$ |  |  | M1 $y^{2}-34 y+225=0$ |
|  | $(x+3)(x-5)=0 x=\frac{2 \pm 8}{2}$ |  |  | A1 $\quad y=9$ or $y=25$ |
|  | $x=-3$ or $x=5$ | $-3,9$ and 5,25 |  | A1 |
|  |  |  |  | Total 5 marks |


| 19 | a |  | $7-\mathrm{x}$ | 1 |
| :--- | :--- | :--- | :--- | :--- |
|  | $8-\mathrm{x}$ seen or $9,13,6$ marked correctly on diagram <br> or $50-(10+9+13+6)=50-38=12$ and $8+7$ <br> $=15$ |  | 3 | M1 |
|  | $10+13+9+6+(7-\mathrm{x})+(8-\mathrm{x})+\mathrm{x}=50$ oe <br> inc $7-\mathrm{x}+8-\mathrm{x}+\mathrm{x}=12$ <br> or $15-12$ |  |  | M1 $\quad$ equation must be correct |
|  |  | 3 |  | A1 |
|  |  |  |  |  |


| $20 \quad$ a |  | $1: \sqrt{k}$ | 1 | B1 |
| :---: | :--- | :--- | :--- | :--- |
|  | Accept $\sqrt{k}$ |  |  |  |
| b | $\sqrt{2}$ or $\sqrt{\frac{1}{2}}$ seen |  | 2 | M1 |
|  |  | 7.1 |  | A1for 7.1 or better (7.071...) <br> Accept $\sqrt{50}$ |
|  |  |  |  | Total 3 marks |


| 21 a |  | 3 n oe | 1 | B1 | Accept eg $\mathrm{n}+2 \mathrm{n}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| b | $n-1,3 n-1$ seen |  | 5 | B2 | B1 for each |  |
|  | $\frac{1}{3} \times \frac{n-1}{3 n-1}=\frac{1}{10} \text { oe inc } \frac{n}{3 n} \times \frac{n-1}{3 n-1}=\frac{1}{10}$ |  |  | M1 | for correct equation |  |
|  | $10(n-1)=3(3 n-1) \text { oe }$ <br> inc $10 n(n-1)=3 n(3 n-1)$ |  |  | M1 | for correctly removing fractions |  |
|  | ( $\mathrm{n}=7$ ) | 21 |  | A1 | cao |  |
|  |  |  |  |  |  | Total 6 marks |
|  |  |  |  |  |  | Total 100 marks |

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