FOR EDEXCEL

## GCE Examinations Advanced Subsidiary

# **Core Mathematics C4**

Paper J

### Time: 1 hour 30 minutes

### Instructions and Information

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.

Full marks may be obtained for answers to ALL questions.

Mathematical formulae and statistical tables are available.

This paper has eight questions.

#### Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.

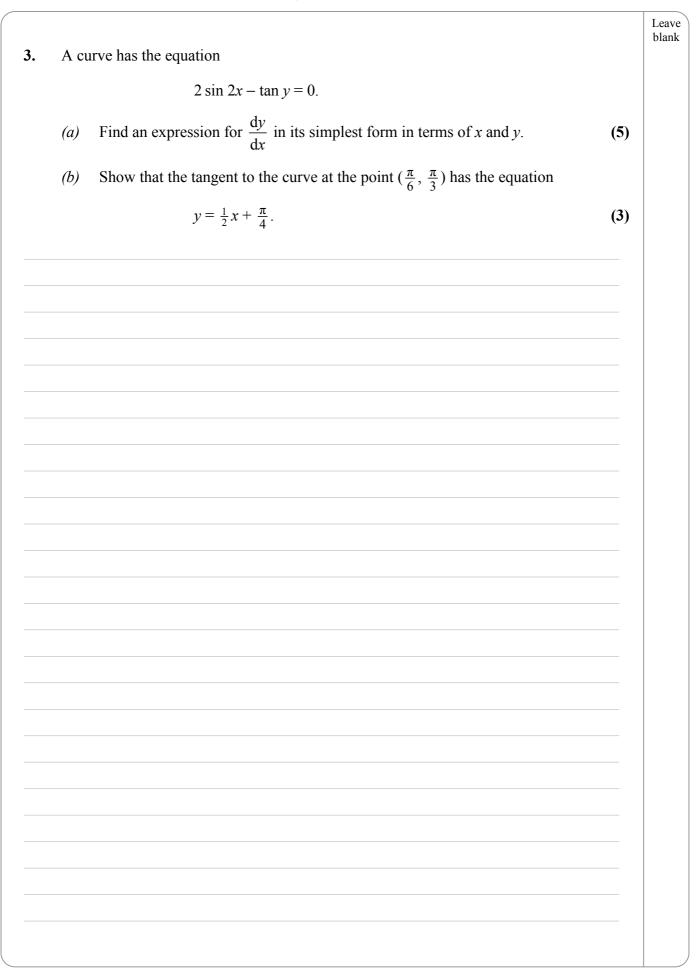


Written by Shaun Armstrong © Solomon Press

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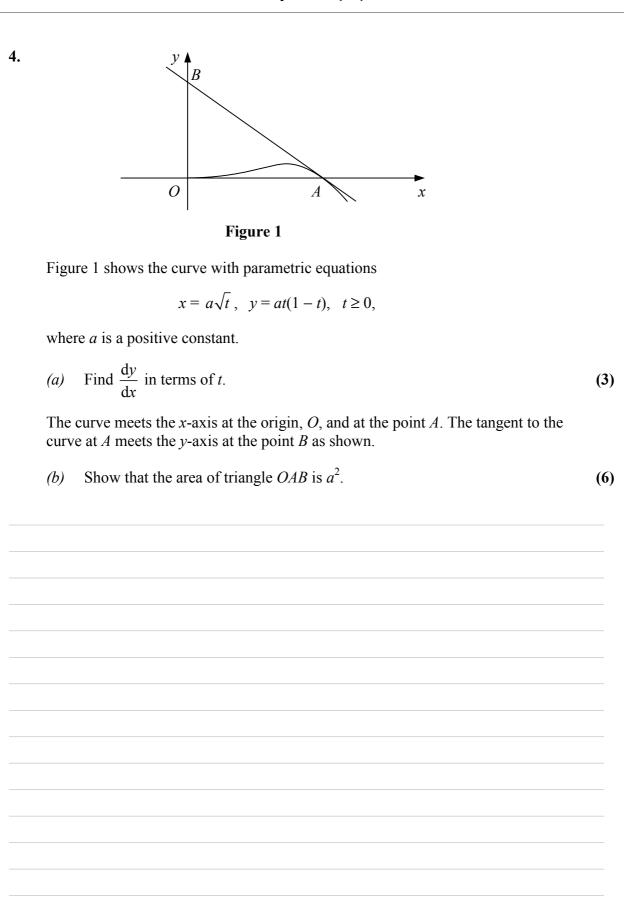
1.	The region bounded by the curve $y = x^2 - 2x$ and the <i>x</i> -axis is rotated through $2\pi$ radians about the <i>x</i> -axis.		Lea blai
	Find the volume of the solid formed, giving your answer in terms of $\pi$ .	(6)	
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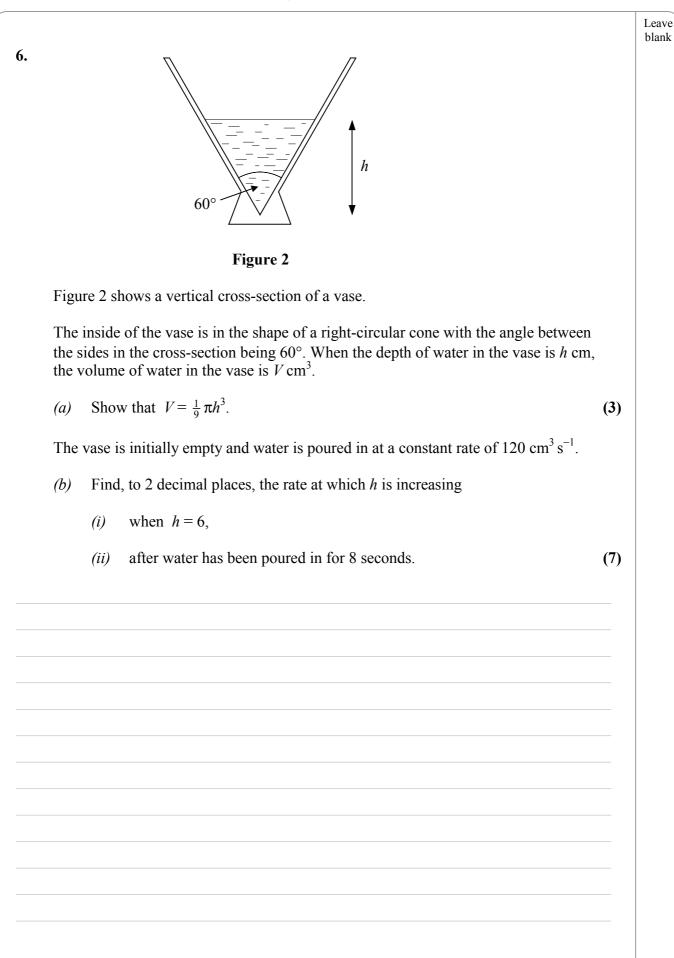
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Leave blank The gradient at any point (x, y) on a curve is proportional to  $\sqrt{y}$ . 5. Given that the curve passes through the point with coordinates (0, 4), show that the equation of the curve can be written in the form *(a)*  $2\sqrt{y} = kx + 4,$ where *k* is a positive constant. (5) Given also that the curve passes through the point with coordinates (2, 9), find the equation of the curve in the form y = f(x). *(b)* (4)

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- 7. Relative to a fixed origin, the points A and B have position vectors  $\begin{pmatrix} -4\\1\\3 \end{pmatrix}$  and  $\begin{pmatrix} -3\\6\\1 \end{pmatrix}$  respectively.
  - (a) Find a vector equation for the line  $l_1$  which passes through A and B.

The line  $l_2$  has vector equation

$$\mathbf{r} = \begin{pmatrix} 3\\ -7\\ 9 \end{pmatrix} + \mu \begin{pmatrix} 2\\ -3\\ 1 \end{pmatrix}.$$

(b) Show that lines  $l_1$  and  $l_2$  do not intersect.

(5)

(2)

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(c) Find the position vector of the point C on  $l_2$  such that  $\angle ABC = 90^{\circ}$ . (6)

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$$f(x) = \frac{x(3x-7)}{(1-x)(1-3x)}, |x| < \frac{1}{3}.$$

*(a)* Find the values of the constants A, B and C such that

$$f(x) = A + \frac{B}{1-x} + \frac{C}{1-3x}.$$
 (4)

*(b)* Evaluate

$$\int_0^{\frac{1}{4}} f(x) dx,$$

giving your answer in the form  $p + \ln q$ , where p and q are rational. (5) Find the series expansion of f(x) in ascending powers of x up to and (5)

(c) including the term in  $x^3$ , simplifying each coefficient.

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