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CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level Advanced International Certificate of Education

MARK SCHEME for the November 2003 question papers

	MATHEMATICS
9709/01	Paper 1 (Pure 1), maximum raw mark 75
9709/02	Paper 2 (Pure 2), maximum raw mark 50
9709/03, 8719/03	Paper 3 (Pure 3), maximum raw mark 75
9709/04	Paper 4 (Mechanics 1), maximum raw mark 50
9709/05, 8719/05	Paper 5 (Mechanics 2), maximum raw mark 50
9709/06, 0390/06	Paper 6 (Probability and Statistics 1), maximum raw mark 50
9709/07, 8719/07	Paper 7 (Probability and Statistics 2), maximum raw mark 50

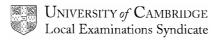
These mark schemes are published as an aid to teachers and students, to indicate the requirements of the examination. They show the basis on which Examiners were initially instructed to award marks. They do not indicate the details of the discussions that took place at an Examiners' meeting before marking began. Any substantial changes to the mark scheme that arose from these discussions will be recorded in the published *Report on the Examination*.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the *Report on the Examination*.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the November 2003 question papers for most IGCSE and GCE Advanced Level syllabuses.



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Mark Scheme Notes

- Marks are of the following three types:
 - M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
 - A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
 - B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol $\sqrt{}$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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• The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through \"marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.



GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 75

SYLLABUS/COMPONENT: 9709/01

MATHEMATICS Pure Mathematics : Paper One



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1	x(11-2x) = 12	M1	Complete elimination of x, or of y.
	$2x^{2}-11x+12=0$	A1	Correct quadratic. (or $y^2-11y+24=0$)
	Solution of quadratic	DM1	Correct method of solution \rightarrow 2values
	\rightarrow (1 ¹ / ₂ ,8) and (4,3)	A1	All correct
	(172,0) und (1,0)	[4]	(guesswork or TI B1 for one pair of
		[']	values, full marks for both)
		D1	
2	(i) $4s^4+5=7(1-s^2) \rightarrow 4x^2+7x-2=0$	B1	Use of $s^2+c^2=1$. Answer given.
		[1]	
	(ii) $4s^4 + 7s^2 - 2 = 0$		
	$\rightarrow s^2 = \frac{1}{4}$ or $s^2 = -2$	M1	Recognition of quadratic in s ²
	$\rightarrow \sin\theta = \pm \frac{1}{2}$	A 1 A 1 a	Co. For 1808 "his walve"
	$\rightarrow \theta = 30^{\circ} \text{ and } 150^{\circ}$	A1A1√	Co. For 180° - "his value"
	and $\theta = 210^{\circ}$ and 330°	A1√	For other 2 answers from "his value",
		[4]	providing no extra answers in the range or
			answers from $s^2 = -1$
3	(a) $a=60$, $n=48$, $S_n=3726$		
	S_n formula used	M1	Correct formula (M0 if nth term used)
	\rightarrow d = \$0.75	A1	Co
	3^{rd} term = a+2d = \$61.50	A1√	Use of $a+2d$ with his d. 61.5 ok.
		[3]	
	(h) $a=6$ $a=4$ $i=2/$	M1	a, ar correct, and r evaluated
	(b) $a=6 \text{ ar } =4$ $\therefore r=\frac{2}{3}$		
	$S_{\infty} = a/(1-r) = 18$	M1A1	Correct formula used, but needs $r < 1$ for
		[3]	M mark
		D0 1 0	a
4	(i) $y = x^3 - 2x^2 + x$ (+c)	B2,1,0	Co - unsimplified ok.
	(1,5) used to give c= 5	B1√	Must have integrated + use of $x=1$ and $y=5$
		[3]	for c
	(ii) $3x^2 - 4x + 1 > 0$	M1	Set to 0 and attempt to solve.
	\rightarrow end values of 1 and $\frac{1}{3}$	A1	Co for end values – even if <,>,=,etc
	5	Al	Co (allow \leq and \geq). Allow $1 < x < \frac{1}{3}$
	\rightarrow x< $\frac{1}{3}$ and x>1	[3]	$CO(allow \leq alld \leq)$. Allow $1 < x < \frac{1}{3}$
		[3]	
5	(i) m of BC = $\frac{1}{2}$	B1	Со
3		1	
ለግ	Eqn BC y-6= $\frac{1}{2}(x-4)$	M1A1√	Correct form of eqn. $\sqrt{\text{ on m}}="1/2"$."
	m of CD = -2	M1	Use of $m_1m_2=-1$
B	eqn CD y-5=-2(x-12)	A1√	$\sqrt{10}$ on his "1/2" but needs both M marks.
	20	[5]	
	(125)		
A	(2.0)		
0			
	(ii) Sim eqns 2y=x+8 and y+2x=29	M1	Method for solving
	\rightarrow C (10,9)	A1	Co
		[2]	Diagram only for (ii), allow B1 for (10,9)
L		<u> </u>	

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6 (i) $20 = 2r + r\theta$ $\rightarrow \theta = (20 / r) - 2$ (ii) $A = \frac{1}{2}r^{2}\theta$ $\rightarrow A = 10r - r^{2}$	M1 A1 [2] M1 A1 [2]	Eqn formed + use of $r\theta$ + at least one r Answer given. Appropriate use of $\frac{1}{2}r^2\theta$ Co – but ok unsimplified –eg $\frac{1}{2}r^2(20/r)-2)$
(iii) Cos rule $PQ^2 = 8^2 + 8^2 - 2.8.8\cos 0.5$ Or trig $PQ = 2 \times 8\sin 0.25$ $\rightarrow PQ = 3.96$ (allow 3.95).	M1 A1 A1 [3]	Recognition of "chord" +any attempt at trigonometry in triangle. Correct expression for PQ or PQ ² . Co
7 (i) Height = 4 (ii) MC = $3i-6j-4k$ MN = $6j-4k$ (iii) MC.MN = $-36+16 = -20$ MC.MN = $\sqrt{61}\sqrt{52}\cos\theta$ $\rightarrow \theta = 111^{\circ}$	B1 [1] B2,1 $$ B1 $$ [3] M1A1 $$ M1 A1 [4]	 Pythagoras or guess – anywhere, 4k ok. √ for "4". Special case B1 for –3i+6j+4k √ on "4". Accept column vectors. (nb if (ii) incorrect, but answers are correct in (iii) allow feedback). Use of x₁y₁+x₂y₂+x₃y₃. √ on MC and MN Product of two moduli and cos θ. Co. Nb If both MC and MN "reversed", allow 111° for full marks.
8 (i) y = $72 \div (2x^2)$ or $36 \div x^2$ A = $4x^2 + 6xy$ $\rightarrow A = 4x^2 + 216 \div x$ (ii) dA/dx = $8x - 216 \div x^2$ = 0 when $8x^3 = 216$	B1 M1 A1 [3] M1 DM1	Co from volume = lbh . Attempts most of the faces(4 or more) Co – answer was given. Reasonable attempt at differentiation. Sets his differential to 0 and uses.
$\rightarrow x = 3$ (iii) Stationary value = 108 cm ² $\frac{d^{2}A/dx^{2}=8+432 \div x^{3}}{\rightarrow Positive when x=3}$ Minimum.	A1 [3] A1√ M1 A1 [3]	Co. (answer = ± 3 loses last A mark) For putting his x into his A. Allow in (ii). Correct method – could be signs of dA/dx A mark needs d ² A/dx ² correct algebraically, + x=3 + minimum. It does not need "24".

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·			
9	(i) $dy/dx = -24/(3x+2)^2$	M1A1	Use of fn of fn. Needs $\times 3$ for M mark. Co.
AVESTAL	Eqn of tangent y-1=- $\frac{3}{8}$ (x-2) Cuts y=0 when x= $\frac{4^2}{3}$	M1A1√	Use of line form with dy/dx. Must use calculus. $$ on his dy/dx. Normal M0.
	Area of Q = $\frac{1}{2} \times 2^{\frac{2}{3}} \times 1 = \frac{4}{3}$	M1A1 [6]	Needs y=0 and ½bh for M mark. (beware fortuitous answers)
= Limit	$\pi \int y^2 dx = \pi \int 64(3x+2)^{-2} dx$ $\pi [-64(3x+2)^{-1} \div 3]$ as from 0 to 2 $\Rightarrow 8\pi$	M1 A1A1 DM1 A1 [5]	Uses $\int y^2 + \text{ some integration} \rightarrow (3x+2)^k$. A1 without the ÷3. A1 for ÷3 and π Correct use of 0 and 2. DMO if 0 ignored. Co. Beware fortuitous answers.
10			
	= g first, then f = $8/(2-x) - 5 = 7$	M1 DM1	Correct order - g first, then into f. Correct method of solution of fg=7.
	$\rightarrow x = 1\frac{1}{3}$	A1	Co. (nb gf gets $0/3$)
(or f(A)=7, A =	$(3) = 6, g(x) = 6, \rightarrow x = 1\frac{1}{3})$	[3]	(M1 for 6. M1 for g(x)=6. A1)
(ii) $f^1 = \frac{1}{2}$ Make $\rightarrow g^2$	$\frac{1}{2}(x+5)$ es y the subject $y = 4 \div (2-x)$ $x^{-1} = 2 - (4 \div x)$	B1 M1 A1 [3]	Anywhere in the question. For changing the subject. Co – any correct answer. (A0 if f(y).)
\rightarrow x Use c	$x = \frac{1}{2} (x+5)$ $x^{2}+x+8=0$ of b ² -4ac \rightarrow Negative value to roots.	M1 M1 A1 [3]	Algebra leading to a quadratic. Quadratic=0 + use of b ² -4ac. Correct deduction from correct quadratic.
(iv) 5,2	Y a line wax	B1 B1 B1 [3]	Sketch of f Sketch of f ⁻¹ Evidence of symmetry about y=x.



GCE AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/02

MATHEMATICS Pure Mathematics : Paper Two



	Page 1	WWW.dyı Mark Scheme	namicpap Syllabus	ers.com Paper
	raye i	A AND AS LEVEL – NOVEMBER 2003	9709	2
1	EITHER:	State or imply non-modular inequality e.g. $-2 < 8-3x < 2$, or corresponding equation or pair of equations	or $(8-3x)^2 < 2$	² , M1
		Obtain critical values 2 and $3\frac{1}{3}$		Al
		State correct answer $2 < x < 3\frac{1}{3}$		Al
	OR:	State one critical value (probably $x = 2$), from a graphical	method or by	
		inspection or by solving a linear equality or equation State the other critical value correctly		B1 B1
		State correct answer $2 < x < 3\frac{1}{3}$		B1
				[3]
2		State or imply at any stage $\ln y = \ln k - x \ln a$		B1
		Equate estimate of $\ln y$ - intercept to $\ln k$ Obtain value for k in the range 9.97 ± 0.51		M1 A1
		Calculate gradient of the line of data points		MI
		Obtain value for <i>a</i> in the range 2.12 ± 0.11		Al
				[5]
3 (1	i) <i>EITHER</i> :	*		M1
		Obtain answer <i>a</i> =6		Al
	OR:	Carry out complete division and equate remainder to zero		M1
		Obtain answer <i>a</i> =6		A1
				[2]
(i	i)	Substitute 6 for <i>a</i> and either show $f(x) = 0$ or divide by (<i>x</i>	– 2) obtainin	-
		remainder of zero		B1
	EITHER:	State or imply $(x + 1)(x - 2) = x^2 - x - 2$ Attempt to find another quadratic factor by division or ins	nation	B1 M1
		State factor $(x^2 + x - 3)$	pection	Al
	OR:	Obtain $x^3 + 2x^2 - 2x - 3$ after division by $x + 1$, or $x^3 - x^2 - 3x^2 -$	-5x+6	
		after division by $x - 2$ Attempt to find a quadratic factor by further division by re-	alevant divis	B1
		or by inspection		M1
		State factor $(x^2 + x - 3)$		Al
				[4]
4 (i	i)	State answer $R = 2$		B1
`	e	Use trig formula to find α		M1
		Obtain answer $\alpha = \frac{1}{3}\pi$		Al
		3		
				[3]

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l age 2	A AND AS LEVEL – NOVEMBER 2003 9709	2
(ii)	Carry out, or indicate need for, evaluation of $\cos^{-1}(\sqrt{2}/2)$	M1*
	Obtain, or verify, the solution $\theta = \frac{7}{12}\pi$	A1
	Attempt correct method for the other solution in range	
	i.e. $-\cos^{-1}(\sqrt{2}/2) + \alpha$. M1(dep*)
	Obtain solution $\theta = \frac{1}{12}\pi$: [M1A0 for $\frac{25\pi}{12}$]	A1
	12 12	[4]
5 (i)	Make recognisable sketch of $y = 2^x$ or $y = x^2$, for $x < 0$	B1
	Sketch the other graph correctly	B1
		[2]
(ii)	Consider sign of $2^x - x^2$ at $x = -1$ and $x = -0.5$, or equivalent	M1
()	Complete the argument correctly with appropriate calculations	A1
		[2]
(iii)	Use the iterative form correctly	M1
()	Obtain final answer –0.77	A1
	Show sufficient iterations to justify its accuracy to 2 s.f., or show there is a sign change in the interval $(-0.775, -0.765)$	A1
		[3]
6 (i)	State <i>A</i> is (4, 0)	B1
	State B is $(0, 4)$	B1
		[2]
(ii)	Use the product rule to obtain the first derivative	M1(dep)
	Obtain derivative $(4 - x)e^x - e^x$, or equivalent Equate derivative to zero and solve for x	A1 M1 (dep)
	Obtain answer $x = 3$ only	A1
		[4]
(iii)	Attempt to form an equation in p e.g. by equating gradients of OP	
	and the tangent at P , or by substituting $(0, 0)$ in the equation of the	N/1
	tangent at P Obtain a section in a section $4-p$	M1
	Obtain equation in any correct form e.g. $\frac{4-p}{p} = 3-p$	A1
	Obtain 3-term quadratic $p^2 - 4p + 4 = 0$, or equivalent Attempt to solve a quadratic equation in p	A1 M1
	Obtain answer $p = 2$ only	A1
		[5]
7 (i)	Attempt to differentiate using the quotient, product or chain rule	M1
	Obtain derivative in any correct form	A1
	Obtain the given answer correctly	A1 [3]

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(ii)	State or imply the indefinite integral is -cotx		В
	Substitute limits and obtain given answer correctly		В
			[2
(iii)	Use $\cot^2 x = \csc^2 x - 1$ and attempt to integrate both terms,		
	or equivalent		M
	Substitute limits where necessary and obtain a correct unsimplifie	ed	
	answer		A
	Obtain final answer $\sqrt{3} - \frac{1}{3}\pi$		А
	3		12
			[3
(iv)	Use $\cos 2A$ formula and reduce denominator to $2\sin^2 x$		В
	Use given result and obtain answer of the form $k\sqrt{3}$		М
	Obtain correct answer $\frac{1}{2}\sqrt{3}$		А
	-		[3



GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 75

SYLLABUS/COMPONENT: 9709/03, 8719/03

MATHEMATICS Mathematics and Higher Mathematics : Paper 3



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	A AND AS LEVEL – NOVEMBER 2003	9709/8719	3
EITHER:	State or imply non-modular inequality $-5 < 2^x - 8 < 5$, or	$\left(2^x - 8\right)^2 < 5$	² or correspon
	pair of linear equations or quadratic equation		
	Use correct method for solving an equation of the form 2	$a^{x} = a$	
	Obtain critical values 1.58 and 3.70, or exact equivalents		
	State correct answer $1.58 < x < 3.70$		
OR:	Use correct method for solving an equation of the form 2	$a^{x} = a$	
	Obtain one critical value (probably 3.70), or exact equival	lent	
	Obtain the other critical value, or exact equivalent		
	State correct answer $1.58 < x < 3.70$		
terms of ln c	ad 3.7. Condone \leq for $<$. Allow final answers given separate or logarithms to base 10.] given as logarithms to base 2 can only earn M1 and B1 of		
EITHER:	Obtain correct unsimplified version of the x^2 or x^4 term of x^2	of the expansi	ion of
	$(1+\frac{1}{2}x^2)^{-2}$ or $(2+x^2)^{-2}$		

State correct first term $\frac{1}{4}$ Obtain next two terms $-\frac{1}{4}x^2 + \frac{3}{16}x^4$ A1+A1

[The M mark is not earned by versions with unexpanded binomial coefficients such as $\begin{pmatrix} -2 \\ 1 \end{pmatrix}$.]

[SR: Answers given as $\frac{1}{4}(1-x^2+\frac{3}{4}x^4)$ earn M1B1A1.]

[SR: Solutions involving $k(1+\frac{1}{2}x^2)^{-2}$, where k = 2, 4 or $\frac{1}{2}$ can earn M1 and A1 for a correct simplified term in x^2 or x^4 .]

OR:	Differentiate expression and evaluate $f(0)$ and $f'(0)$, where $f'(x) = kx(2 + x^2)^{-1}$	⁻³ M1
	State correct first term $\frac{1}{4}$	B1
	Obtain next two terms $-\frac{1}{4}x^2 + \frac{3}{16}x^4$	A1+A1

[Allow exact decimal equivalents as coefficients.]

[4] 3 Use correct cos 2A formula, or equivalent pair of correct formulas, to obtain an equation in $\cos \theta$ M1 Obtain 3-term quadratic $6\cos^2\theta + \cos\theta - 5 = 0$, or equivalent A1 Attempt to solve quadratic and reach $\theta = \cos^{-1}(a)$ M1 Obtain answer 33.6° (or 33.5°) or 0.586 (or 0.585) radians A1 Obtain answer 180° or π (or 3.14) radians and no others in range A1

[The answer $\theta = 180^{\circ}$ found by inspection can earn B1.] [Ignore answers outside the given range.]

[5]

B1

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4(i) EITHER	Obtain terms $\frac{1}{2\sqrt{x}}$ and $\frac{1}{2\sqrt{y}} \frac{dy}{dx}$, or equivalent	B1+B1
	Obtain answer in any correct form, e.g. $\frac{dy}{dx} = -\sqrt{\frac{y}{x}}$	B1
OR:	Using chain or product rule, differentiate $(\sqrt{a} - \sqrt{x})^2$	M1
	Obtain derivative in any correct form	A1
	Express $\frac{dy}{dx}$ in terms of x and y only in any correct form	A1
OR:	Expand $(\sqrt{a} - \sqrt{x})^2$, differentiate and obtain term $-2 \cdot \frac{\sqrt{a}}{2\sqrt{x}}$, or equivalent	B1
	Obtain term 1 by differentiating an expansion of the form $a + x \pm 2\sqrt{a}\sqrt{x}$	B1
	Express $\frac{dy}{dx}$ in terms of x and y only in any correct form	B1
		[3]
(ii)	State or imply coordinates of P are $(\frac{1}{4}a, \frac{1}{4}a)$	B1
()	Form equation of the tangent at P	M1
	Obtain 3 term answer $x + y = \frac{1}{2}a$ correctly, or equivalent	Al
		[3]
5 (i)	Make recognizable sketch of $y = \sec x$ or $y = 3 - x^2$, for $0 < x < \frac{1}{2}\pi$	B1
- (-)	Sketch the other graph correctly and justify the given statement	B1
	satisfier and start graph contoolly and justify the group statement	
		[2]

[Award B1 for a sketch with positive *y*-intercept and correct concavity. A correct sketch of $y = \cos x$ can only earn B1 in the presence of $1/(3-x^2)$. Allow a correct single graph and its intersection with y = 0 to earn full marks.]

(ii)	State or imply equation $\alpha = \cos^{-1}(1/(3-\alpha^2)) \operatorname{or} \cos \alpha = 1/(3-\alpha^2)$	B1
	Rearrange this in the form given in part (i) i.e. sec $\alpha = 3 - \alpha^2$	B1

[Or work vice versa.]

Use the iterative formula with $0 \le x_1 \le \sqrt{2}$	M1
Obtain final answer 1.03	A1
Show sufficient iterations to justify its accuracy to 2d.p. or show there is a sign change in the interval (1.025, 1.035)	A1
	Obtain final answer 1.03 Show sufficient iterations to justify its accuracy to 2d.p. or show there is a sign

[3]

[2]

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raye J	A AND AS LEVEL – NOVEMBER 2003 9709/8719 3
(i)	Use product or quotient rule to find derivative
()	Obtain derivative in any correct form
	Equate derivative to zero and solve a linear equation in x
	Obtain answer $3\frac{1}{2}$ only
(ii)	State first step of the form $\pm \frac{1}{2}(3-x)e^{-2x} \pm \frac{1}{2}\int e^{-2x} dx$, with or without 3
	State correct first step e.g. $-\frac{1}{2}(3-x)e^{-2x} - \frac{1}{2}\int e^{-2x} dx$, or equivalent, with or
	without 3
	Complete the integration correctly obtaining $-\frac{1}{2}(3-x)e^{-2x} + \frac{1}{4}e^{-2x}$, or equivalent
	Substitute limits $x = 0$ and $x = 3$ correctly in the complete integral
	Obtain answer $\frac{1}{4}(5+e^{-6})$, or exact equivalent (allow e^0 in place of 1)
(\mathbf{i}) FITHE	R: Attempt multiplication of numerator and denominator by $3 + 2i$,
	or equivalent
	Simplify denominator to 13 or numerator to $13 + 26i$
	Obtain answer $u = 1 + 2i$
OR:	Using correct processes, find the modulus and argument of u
	Obtain modulus $\sqrt{5}$ (or 2.24) or argument tan ⁻¹ 2 (or 63.4° or 1.11 radians)
	Obtain answer $u = 1 + 2i$
(ii)	Show the point U on an Argand diagram in a relatively correct position
(11)	Show a circle with centre U
	Show a circle with radius consistent with 2
f.t. on the va	lue of <i>u</i> .]
(iii)	State or imply relevance of the appropriate tangent from O to the circle
	Carry out a complete strategy for finding max arg z
	Obtain final answer 126.9° (2.21 radians)
Drawing the	appropriate tangent is sufficient for $B1\sqrt{.}$]
	ver obtained by measurement earns M1 only.]

Page 4	Mark Scheme	dynamicpa	Paper
	A AND AS LEVEL – NOVEMBER 2003	9709/8719	3
(i) FITHER.	Divide by denominator and obtain a quadratic remainder		
(\mathbf{I}) EITHER.	Obtain $A = 1$		
	Use any relevant method to obtain <i>B</i> , <i>C</i> or <i>D</i>		
	Obtain one correct answer		
	Obtain $B = -1, C = 2, D = 0$		
OR:	Reduce <i>RHS</i> to a single fraction and identify numerator v	with that of f(x	<i>z</i>)
	Obtain A = 1		
	Use any relevant method to obtain <i>B</i> , <i>C</i> or <i>D</i> Obtain one correct answer		
	Obtain one correct answer Obtain $B = -1$, $C = 2$, $D = 0$		
	00mm D 1, C 2, D 0		
(ii)	Integrate and obtain terms $x - \ln (x - 1)$, or equivalent		
	Obtain third term $\ln(x^2 + 1)$, or equivalent		
	Substitute correct limits correctly in the complete integra	1	
	Obtain given answer following full and exact working		
	first B1 $$ is not available.] mitted in part (i), treat as if $A = 0$. Thus only M1M1 and E	$D_{1}/D_{1}/M_{1}$ or	a availabla
$[SK: \Pi A] S C$			e avallable
9 (i)	Separate variables and attempt to integrate $\frac{1}{\sqrt{(P-A)}}$		
	Obtain term $2\sqrt{(P-A)}$		
	Obtain term $-kt$		
	Obtain term $-kT$		
(ii)	Use limits $P = 5A$, $t = 0$ and attempt to find constant c		
()	Obtain $c = 4\sqrt{A}$, or equivalent		
	Use limits $P = 2A$, $t = 2$ and attempt to find k		
	Obtain given answer $k = \sqrt{A}$ correctly		
(iii)	Substitute $P = A$ and attempt to calculate t Obtain answer $t = 4$		
	Obtain answer $t - 4$		
(iv)	Using answers to part (ii), attempt to rearrange solution t	o give <i>P</i> in ter	ms of
	A and t	-	
	Obtain $P = \frac{1}{4}A(4 + (4 - t)^2)$, or equivalent, having square	$d\sqrt{A}$	

[For the M1, $\sqrt{(P-A)}$ must be treated correctly.]

	www.dynamicpapers.com			m
Page 5	Mark Scheme Syllabus Paper			
	A AND AS LEVEL – NOVEMBER 2003	9709/8719	3	
10 (i)	Express general point of <i>l</i> or <i>m</i> in component form e.g. (1 (6 + t , -5 - 2 t , 4 + t) Equate at least two corresponding pairs of components and for <i>s</i> or <i>t</i> Obtain $s = 1$ or $t = -3$ Verify that all three component equations are satisfied Obtain position vector $3\mathbf{i} + \mathbf{j} + \mathbf{k}$ of intersection point, or e	d attempt to		B1 M A1 A1
				[5]
(ii) EITHER:	Use scalar product to obtain $2a + b + 3c = 0$ and $a - 2b + c$ Solve and find one ratio e.g. $a : b$ State one correct ratio Obtain answer $a : b : c = 7 : 1 : -5$, or equivalent Substitute coordinates of a relevant point and values of a ,		eneral	B1 M A1 A1
	equation of plane and calculate d Obtain answer $7x + y - 5z = 17$, or equivalent			M A
OR:	Using two points on <i>l</i> and one on <i>m</i> (or <i>vice versa</i>) state three simultaneous equations in <i>a</i> , <i>b</i> , <i>c</i> and <i>d</i> e.g. $3a + b + c = d$, $a - 2c = d$ and $6a - 5b + 4c = d$ Solve and find one ratio e.g. <i>a</i> : <i>b</i> State one correct ratio Obtain a ratio of three unknowns e.g. <i>a</i> : <i>b</i> : <i>c</i> = 7 : 1 : - 5, or equivalent Use coordinates of a relevant point and found ratio to find fourth unknown e.g. <i>d</i> Obtain answer $7x + y - 5z = 17$, or equivalent		B M A A M A	
OR:	Form a correct 2-parameter equation for the plane, e.g. $\mathbf{r} = \mathbf{i} - 2\mathbf{k} + \lambda(2\mathbf{i}+\mathbf{j}+3\mathbf{k}) + \mu(\mathbf{i}-2\mathbf{j}+\mathbf{k})$ State 3 equations in <i>x</i> , <i>y</i> , <i>z</i> , λ and μ State 3 correct equations Eliminate λ and μ Obtain equation in any correct unsimplified form Obtain $7x + y - 5z = 17$, or equivalent		B1 M A1 A1 A1	
OR:	Attempt to calculate vector product of vectors parallel to <i>l</i> Obtain two correct components of the product Obtain correct product, e.g. $7\mathbf{i} + \mathbf{j} - 5\mathbf{z}$ State that the plane has equation of the form $7x + y - 5z = 3$ Substitute coordinates of a relevant point and calculate <i>d</i> Obtain answer $7x + y - 5z = 17$, or equivalent			M A A M A
[T] C. 11 41.	rough is an $2\mathbf{i} + \mathbf{i} + \mathbf{k}$ only]			[6]

[The follow through is on 3i + j + k only.]



GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/04

MATHEMATICS Paper 4 (Mechanics 1)



Pa	age 1	www.dynan Je 1 Mark Scheme Sylla		Paper	
		A AND AS LEVEL – NOVEMBER 2003	9709	4	
l	(i)	The force is 320 N	B1	1	
	(ii)	For using Newton's second law (3 terms needed)	M1		
		$320 - R = 100 \times 0.5$	A1 √		
		Resistance is 270 N	A1	3	
2	(i)	Speed is 20 ms ⁻¹	B1	1	
	(ii)	For using $s = \frac{1}{2} gt^2$ $45 = \frac{1}{2} 10t^2$	M1		
		Time taken is 3 s	A1	2	
	(iii)	For using $v^2 = u^2 + 2gs$ $(40^2 = 30^2 + 2 \times 10s)$	M1		
		Distance fallen is 35 m	A1	2	
3	(i)	For using the idea of work as a force times a distance $(25 \times 2\cos 15^{\circ})$	M1		
		Work done is 48.3 J	A1	2	
	(ii)	For resolving forces vertically (3 terms needed)	M1		
		$N + 25 \sin 15^\circ = 3 \times 10$ ($\sqrt{\cos instead}$ of sin following sin instead of cos in (i))	A1 √		
		Component is 23.5 N	A1	3	
ŀ	(i)	KE (gain) = $\frac{1}{2} 0.15 \times 8^2$	B1		
		For using PE loss = KE gain	M1		
		Height is 3.2 m	A1	3	
	(ii)	For using WD is difference in PE loss and KE gain	M1		
		WD = $0.15 \times 10 \times 4 - \frac{1}{2} 0.15 \times 6^2$	A1		
		Work Done is 3.3 J	A1	3	
	(implied in (in (in (in (in (in (in (in (in (in	by candidates who treat <i>AB</i> as if it is straight and vertical icitly or otherwise) Max 2 out of 6 marks. $8^2 \div (2 \times 10) = 3.2$ B1 $= 6^2 \div (2 \times 4) = 4.5$ and $R = 0.15 \times 10 - 0.15 \times 4.5 = 0.825$ and $= 4 \times 0.825 = 3.3$ B1	I		

Ρ	age 2	Mark Scheme	ynamicpa Syllabus	Paper
		A AND AS LEVEL – NOVEMBER 2003	9709	4
	(i)	For applying Newton's second law to <i>A</i> or to <i>B</i> (3 terms needed)	M1	
		T - 0.6 = 0.4a or $0.1g - T = 0.1a$	A1	
		For a second of the above 2 equations or for 0.1g - 0.6 = 0.5a [Can be scored in part (ii)] (Sign of <i>a</i> must be consistent with that in first equation)	B1	
		Tension is 0.92 N	A1	4
	(ii)	<i>a</i> = 0.8	B1	
		For using $v = at$	M1	
		Speed = 1.2 ms^{-1}	A1	3
	(i)	$T_{\rm BM} = T_{\rm AM}$ or $T_{\rm BM} \cos 30^\circ = T_{\rm AM} \cos 30^\circ$	B1	
		For resolving forces at <i>M</i> horizontally $(2T \sin 30^\circ = 5)$ or for using the sine rule in the triangle of forces $(T \div \sin 60^\circ = 5 \div \sin 60^\circ)$ or for using Lami's theorem $(T \div \sin 120^\circ = 5 \div \sin 120^\circ)$ Tension is 5 N A.G.	M1 A1	3
	(ii)	For resolving forces on <i>B</i> horizontally $(N = T \sin 30^{\circ})$ or from symmetry $(N = 5/2)$ or for using Lami's theorem $(N \div \sin 150^{\circ} = 5 \div \sin 90^{\circ})$ For resolving forces on <i>B</i> vertically (3 terms needed) or for using Lami's theorem	M1	
		$0.2 \times 10 + F = T \cos 30^{\circ}$ or $(0.2g + F) \div \sin 120^{\circ} = T \div \sin 90^{\circ}$ For using $F = \mu R$ (2.33 = 2.5 μ	A1	
		Coefficient is 0.932	A1	5
	(iii)	$(0.2 + m)g - 2.33 = 5\cos 30^{\circ}$ or $mg = 2(2.33)$ m = 0.466	B1 √ B1	2
	(i)	For using the idea that area represents the distance travelled	d. M1	
		For any two of $\frac{1}{2} \times 100 \times 4.8$, $\frac{1}{2} \times 200(4.8 + 7.2)$, $\frac{1}{2} \times 200 \times 7.2$ (240, 1200, 720)	A1	
		Distance is 2160 m	A1	3

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Page 3	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – NOVEMBER 2003	9709	4
(ii)	For using the idea that the initial acceleration is the gradier the first line segment or for using $v = at$ (4.8 = 100 <i>a</i>) $v^2 = 2as$ (4.8 ² = 2 <i>a</i> ×240)		
	Acceleration is 0.048 ms ⁻²	A1	2
(iii)	a = 0.06 - 0.00024t	B1	
	Acceleration is greater by 0.012 ms ⁻² [$\sqrt{\text{ for } 0.06 - \text{ ans}(ii)}$ (must be +ve) and/or wrong coefficient of <i>t</i> in <i>a</i> (<i>t</i>)] [Accept 'acceleration is 1.25 times greater']	B1 √	2
(iv)	<i>B</i> 's velocity is a maximum when $0.06 - 0.00024t = 0$ [$\sqrt{\text{wrong coefficient of } t \text{ in } a(t)$]	B1 √	
	For the method of finding the area representing $s_A(250)$	M1	
	$240 + \frac{1}{2} (4.8 + 6.6) 150 \text{or} 240 + (4.8 \times 150 + \frac{1}{2} \ 0.012 \times 150^2) $ (1095)	A1	
	For using the idea that s_B is obtained from integration	M1	
	$0.03t^2 - 0.00004t^3$	A1	
	Required distance is 155 m $(\sqrt{\text{dependent on both M marks}})$	A1√	6



GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/05, 8719/05

MATHEMATICS AND HIGHER MATHEMATICS Paper 5 (Mechanics 2)



	Page 1		Paper
		A AND AS LEVEL – NOVEMBER 2003 9709/8719	5
		For using Newton's second law with $a = v^2/r$	Ν
		$F = 50\ 000\ \frac{25^2}{1250}$	А
		Magnitude of the force is 25 000 N	А
			[3
	(i)	For stating or implying that the centre of mass is vertically above the $-$	
		lowest point of the cone, and with $y = 5$	В
		For using $\tan \theta = \frac{10}{y}$ or equivalent	Ν
		$\theta = 63.4^{\circ}$	A
			[3
	(ii)	For using $F < \mu R$	Ν
		$mg\sin\theta < \mu mg\cos\theta$	А
		or the above 2 marks:	
		$\tan \phi$ where ϕ is the angle of friction e cone topples without sliding	N A
		Coefficient is greater than 2 (ft on $tan\theta$ in (i))	А
I.B	. Direct q	uotation of "topples if $\mu > \tan\theta$ " (scores B2); $\mu > 2$ (B1)	[3
	(i)	$T = \frac{88 \times 0.1}{2.4}$	В
	(i)	$T = \frac{88 \times 0.1}{0.4}$ For using Newton's second law (22 - 0.2 x 10 = 0.2a)	B
	(i)	$T = \frac{88 \times 0.1}{0.4}$ For using Newton's second law (22 - 0.2 x 10 = 0.2 <i>a</i>) (3 term equation needed) Initial acceleration is 100 ms ⁻²	
1	(i)	For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed)	Ν
		For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻²	M A [3
	(i) (ii)	For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻² For using EPE = $\frac{\lambda x^2}{2L}$ $(\frac{88 \times 0.1^2}{2 \times 0.4})$	M A [3 M
		For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻²	M A [3 M A
	(ii)	For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻² For using EPE = $\frac{\lambda x^2}{2L}$ $(\frac{88 \times 0.1^2}{2 \times 0.4})$ Initial elastic energy is 1.1 J	M [3 [4 [4
		For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻² For using EPE = $\frac{\lambda x^2}{2L}$ $(\frac{88 \times 0.1^2}{2 \times 0.4})$	M A [3 M A
	(ii)	For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻² For using EPE = $\frac{\lambda x^2}{2L}$ $(\frac{88 \times 0.1^2}{2 \times 0.4})$ Initial elastic energy is 1.1 J	M [3 [4 [4
	(ii)	For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻² For using EPE = $\frac{\lambda x^2}{2L}$ $(\frac{88 \times 0.1^2}{2 \times 0.4})$ Initial elastic energy is 1.1 J Change in GPE = 0.2 x 10 x 0.1 For using the principle of conservation of energy (KE, EPE and GPE must all be represented)	M [4 [4 [4 [4] [4]]
	(ii)	For using Newton's second law $(22 - 0.2 \times 10 = 0.2a)$ (3 term equation needed) Initial acceleration is 100 ms ⁻² For using EPE = $\frac{\lambda x^2}{2L}$ $(\frac{88 \times 0.1^2}{2 \times 0.4})$ Initial elastic energy is 1.1 J Change in GPE = 0.2 x 10 x 0.1 For using the principle of conservation of energy (KE, EPE and GPE	М [4 [4 [4 [4] В

Page 2	WWW.dy Mark Scheme	Syllabus	Paper	Ĵ.
Fage 2		9709/8719	<u>- raper</u> 5	
(i)	e.g. For taking moments about BC			М
	Distance of centre of mass of triangular portion is			
	$9.5 + \frac{1}{3} \ge 6 (= 11.5)$			B1
	$8 \times 9.5 \times 4.75 + \frac{1}{2} \times 8 \times 6 \times 11.5 = (8 \times 9.5 + \frac{1}{2} \times 8 \times 6)$	$\overline{5}$) \overline{x}		A1
	Distance is 6.37 cm			A1
N.B.	Alternative method			м
	e.g. Moments about axis through A perpendicular to AB			M
	Distance of C.O.M. of triangular piece removed is 2			B1
	$(8 \times 15.5) \times 7.75 - (\frac{1}{2} \times 8 \times 6) \times 2 = (124 - 20) \overline{x}_1$			A
	$(\bar{x}_1 = 9.13)$ therefore distance is 6.37 cm			A1
				[4]
(ii)	For taking moments about A For LHS of $80(15.5 - 6.37) = T \times 15.5 \sin 30^{\circ}$ For RHS of above equation Tension is 94.2 N			M A1 A1 A1
				[4]
				•
(iii)	For resolving forces on the lamina vertically (3 term equ ($V = 80 - 94.2 \times 0.5$) or taking moments about B	ation)		М
	$(15.5V = 8 \times 10 \times 6.37)$ Magnitude of vertical component is 32.9 N			A
				[2]

	WWW.	dynamicp	apers.cc	Sm
Page 3	Mark Scheme	Syllabus	Paper	
	A AND AS LEVEL – NOVEMBER 2003	9709/8719	5	

(i) For using
$$\dot{y} = \dot{y}_0 - gt$$
 with $\dot{y} = 0$ $(t = 2\sin\alpha)$ M1

5

For using
$$y = \dot{y}_0 t - \frac{1}{2}gt^2$$
 with *t* as found and $y = 7.2$, or show M1
 $t = 1.2$ as in (ii)

Alternatively for using
$$y_{max} = \frac{V^2 \sin^2 \alpha}{2g}$$
 with $y_{max} = 7.2$ and $V = 20$
or $\dot{y}^2 = \dot{y}_0^2 - 2gy$ with $\dot{y} = 0$ M2

$$7.2 = \frac{400\sin^2\alpha}{20}$$
A1

[4]

Speed on hitting the wall is 20×0.8 (use of ball rebounding at 10 ms⁻¹ scores B0) (ii) B1ft For using $y = 0 - \frac{1}{2}gt^2$ $(-7.2 = -\frac{1}{2}10t^2)$ or $0 = \dot{y} - gt \quad (0 = 12 - 10t)$ M1

Distance is 9.6 m (No ft if rebound velocity =
$$10 \text{ ms}^{-1}$$
) A1ft

Alternative – speed on hitting the wall is
$$20 \times 0.8$$
B1ftUse trajectory equation, with $\theta = 0^{\circ}$ M1

$$-7.2 = x \tan 0^{\circ} - \frac{gx^2}{2.8^2 \cos^2 0^{\circ}}$$
 (allow ft with halving attempt including 10) A1ft
x = 9.6 m A1

[4]

(iii)
$$\dot{y} = \mp 10 \text{ x } 1.2$$
 B1ft

$$\theta = \tan^{-1}(\mp)\frac{\dot{y}}{\dot{x}}$$
 (\dot{x} must have halving attempt. Allow $\dot{x} = 10$) M1

Required angle is 56.3°

A1

Page 4	Mark Scheme Syllabus F	Paper
	A AND AS LEVEL – NOVEMBER 2003 9709/8719	5
(i)	For using Newton's second low	M1
(i)	For using Newton's second law	IVI
	$120 - 8v - 80 \times 10 \times 0.1 = 80a$	A1
	$\frac{1}{5-v} \frac{dv}{dt} = \frac{1}{10}$ from correct working	A1
		[3]
(ii)	For separating the variables and attempting to integrate	M
	$-\ln(5-v) = \frac{1}{10}t + (C)$	Al
	For using $v(0) = 0$ to find C (or equivalent by using limits) (C = -ln5)	M
	For converting the equation from logarithmic to exponential form (allow even if + <i>C</i> omitted) $(5 \div (5 - v) = e^{t/10})$	М
	$v = 5(1 - e^{-t/10})$ from correct working	Al
		[5]
(iii)	For using $v = \frac{dx}{dt}$ and attempting to integrate	М
	$x = 5(t + 10e^{-t/10}) + (C)$	Al
	For using $x(0) = 0$ to find (<i>C</i>) (= -50), then substituting $t = 20$ (or equivalent using limits)	М
	Length is 56.8 m	Al
	OR du	
	For using Newton's second law with $a = v \frac{dv}{dx}$, separating the variables as	nd

attempting to integrate dx (M1 $-v - 5\ln(5 - v) = \frac{x}{10} + C$ A1 For using v = 0 when x = 0 to find C (= -5ln5), then substituting t = 20 into v(t) $(v(20) = 5(1 - e^{-2}) = 4.3233),$

 $(v(20) = 5(1 - e^{-2}) = 4.3233),$ And finally substituting v(20) into the above equation $(x = -50(1 - e^{-2}) + 50 \times 2 = 50 + 50e^{-2})$ M1

Length is 56.8m

A1

[4]

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November 2003

GCE A AND AS LEVEL AICE

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/06, 0390/06

MATHEMATICS Paper 6 (Probability and Statistics 1)



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Page 1	Mark Scher AICE AND A AND AS LEVEL			Syllabus Paper BER 2003 9709/0390 6
	AICE AND A AND AS LEVEL	- 140 4		BER 2003 9703/0390 0
$ \begin{array}{c} 1 \\ x \\ freq \\ OR \end{array} $	0 2 23 17	M1		For reasonable attempt at the mean using freqs or probs but not using prob=0.5
P(0) = 23/40, P(2) = 17/40 Mean = 34/40 = 0.850 Variance = (4×17)/40-(0.85) ² = 0.978 (exact answer 0.9775) (391/400)		A1 M1 A1ft	4	For correct mean For correct variance formula For correct answer
-	7, 6, 3, 1 ies: 3, 7, 3, 1.5, 0.5 4, 0.006, 0.003, 0.001	M1		For frequencies and attempt at scaling, accept cw/freq but not cw × freq , not cw/mid point
scaled f		A1		For correct heights from their scaled frequencies seen on the graph
5		B1		For correct widths of bars, uniform horiz scale, no halves or gaps or less-than-or-equal tos
0 500 1000	2000 3000 4000 area, m ²	B1	4	Both axes labelled, fd and area or m ² . Not class width
$35 - \mu = 1.2$	496σ (accept 0.495 or in between) 282 σ (accept 1.281 or in between, not 1.28)	M1 A1 A	1	For any equation with μ and σ and a reasonable z value not a prob. Allow cc, $\sqrt{\sigma}$, σ^2 , or – and give M1 A0A1ft for these four cases For 2 correct equations
$\sigma = 8.91$ $\mu = 23.6$	(accept 8.89 to 8.92 incl)	M1 A1 A1	6	For solving their two equations by elim 1 variable sensibly For correct answer For correct answer
4 (i) $(0.95)^5$ = 0.774		M1 A1	2	For 0.95 seen, can be implied For correct final answer
(ii) (0.95) ⁴ ×	$(0.05)^1 \times {}_5C_1$	M1		For any binomial calculation with 3 terms, powers summing to 5
= 0.204		A1	2	For correct answer
(iii) (0.95) ² ×	a (0.05)	M1		For no Ps, no Cs, and only 3 terms of type $p^2(1-p)$
= 0.0451((361/8000)	A1	2	For correct answer

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Page 2 Mark Sche			Syllabus	Paper	_
AICE AND A AND AS LEVEL		BER 2003	9709/0390	6	
5 <i>C</i>	M1	For correc	t shape ie <i>M</i> a	nd F first	
0.54 0.95 NC	A1		t, ie labels and nly for (implie		
0.46 0.02 C F 0.98 NC	M1 A1		g P(<i>M</i> and <i>C</i>) and <i>C</i>) and <i>C</i> are a constrained of <i>C</i> are a constrained of <i>C</i> and <i>C</i> are a constrained of <i>C</i> and <i>C</i> are a constrained of <i>C</i>		.d <i>C</i>)
$P(M C) = \frac{0.54 \times 0.05}{0.54 \times 0.05 + 0.46 \times 0.02}$ $= 0.746 (135/181)$	M1 B1 M1 A1 6	For correc	t conditional p t numerator ng two two-fact t answer	-	
6 (a) (i) 18564 (ii) ${}_{17}C_5$ or ${}_{6}/18 \times$ their (i) or ${}_{18}C_6 - {}_{17}C_6$ = 6188	B1 1 M1 A1 2		t final answer 17 and 5 as a p t answer	perm or co	mb
(b) (i) 40320 (ii) $5! \times 3! \times {}_{4}C_{1}$ = 2880	B1 1 B1 1 B1 1 B1 1 B1 1	For $5!$ or ${}_5P_5$ For $3!$ For ${}_4C_1$, ma	t final answer used in a prod or ny be implied by	v 4!	a term≠5!
	B1 4		et final answer		21
7 (i) $z = \pm 1.143$ P(7.8 <t<11)=<math>\Phi(1.143) - 0.5 = 0.8735 - 0.5</t<11)=<math>	M1 A1 M1	accept √σ For seeing	C.		σ cc, no σ^2 but where $p_2 > p_1$
= 0.3735 (accept ans rounded to 0.37 to 0.374)	A1 4	For correc	t answer		
(ii) $(0.1265)^2 \times (0.8735) \times {}_3C_2$ = 0.0419	M1 A1ft 2	with powe	ree term binon rs summing to t answer ft on	3	-
(iii) Not symmetric so not normal Does not agree with the hospital's figures	B1 B1dep 2	For any va For stating	llid reason it does not agree	e, with no in	nvalid reasons
8 (i) $18c = 1$	M1	For $\sum p_i$	=1		
c = 1/18 = 0.0556	A1 2	For correc	t answer		
(ii) $E(X) = 2.78 (= 25/9)(= 50c)$ Var $(X) = 1.17 (= 95/81) (=160c - 2500 \ c^2)$	M1 A1ft M1 A1ft 4	For correc For correc	rect formula for t expectation, t variance form t answer ft on	ft on their nula	с
(iii) $P(X > 2.78) = 11c$ = 0.611 (= 11/18)	M1 A1 2	For using the For correct	neir correct num t answer	iber of disci	rete values of X



GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/07, 8719/07

MATHEMATICS AND HIGHER MATHEMATICS Paper 7 (Probability and Statistics 2)



 $\begin{array}{l} U \\ NIVERSITY \textit{ of } C \\ A \\ MBRIDGE \\ Local Examinations \\ Syndicate \end{array}$

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	Page 1 Mark Scl A AND AS LEVEL – I		Syllabus Paper ER 2003 9709/8719 7
			· · · · · · · · · · · · · · · · · · ·
1	$\frac{1.9}{\sqrt{n}} \times 1.96 < 1$ n > 13.9 (13.87) n = 14	M1 A1 M1 A1 [4]	For equality or inequality involving width or equivalent and term in $1/\sqrt{n}$ and a z-value For correct inequality For solving a relevant equation For correct answer cwo
2	$\lambda = 4.5$ P(X = 2, 3, 4) = e ^{-4.5} $\left(\frac{4.5^2}{2!} + \frac{4.5^3}{3!} + \frac{4.5^4}{4!} \right)$ = 0.471	M1 B1 M1 A1 A1 [5]	For using Poisson approximation any mean For correct mean used For calculating P(2, 3, 4) their mean For correct numerical expression For correct answer NB Use of Normal can score B1 M1 SR Correct Bin scores M1 A1 A1 only
3	SU ~ N(19,12) P(T-SU > 0) or P(T-S > 5) = $1 - \Phi\left(\frac{0-1}{\sqrt{21}}\right)$ = $\Phi(0.2182)$ = 0.586	B1 M1 M1 A1 [5]	For correct mean and variance. Can be implied if using $P(T-S>5)$ in next part For consideration of $P(T - SU > 0)$ For summing their two variances For normalising and finding correct area from their values For correct answer
4	(i) $\lambda = \frac{20}{80} = 0.25$	B1	For $\lambda = 0.25$
	$P(X \ge 3) = 1 - P(X \le 2)$	M1	For calculating a relevant Poisson prob(any λ)
	$= 1 - e^{-0.25} (1 + 0.25 + \frac{0.25^2}{2})$	M1	For calculating expression for P ($X \ge 3$) their λ
	= 0.00216	A1	For correct answer
		[4]	
	(ii) $e^{\frac{-k}{80}} = 0.9$ $\frac{-k}{80} = -0.10536$	M1 M1 M1	For using $\lambda = -t/80$ in an expression for P(0) For equating their expression to 0.9 For solving the associated equation
	<i>k</i> = 8.43	A1 [4]	For correct answer cwo
5	(i) $P(\overline{X} > 1800) = 1 - \Phi\left(\frac{1800 - 1850}{117 / \sqrt{26}}\right)$	B1	For $117/\sqrt{26}$ (or equiv)
	$= \Phi(2.179)$	M1	For standardising and use of tables
	= 0.985	A1	For correct answer cwo
		[3]	

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(II) II 1050	D1	
(ii) $H_0: \mu = 1850$	B1	Both hypotheses correct
$H_1: \mu \neq 1850$		
Test statistic = $\frac{1833 - 1850}{117/\sqrt{26}}$	M1	Standardising attempt including standard error
= -0.7409	A1	Correct test statistic (+/-)
Critical value $z = \pm 1.645$	M1	Comparing with $z = \pm 1.645$, + with + or – with – (or equiv area comparison) ft 1 tail test z=1.282
Accept H ₀ , no significant change	A1ft	For correct conclusion on their test statistic and their <i>z</i> . No contradictions.
	[5]	
6 (i) (a) Rejecting H_0 when it is true	B1	Or equivalent
(b) Accepting H_0 when it is false	B1	
	[2]	
(ii) (a) $\mathbf{P}(\mathbf{N} \mathbf{N} \mathbf{N} \mathbf{N})$ up dop $\mathbf{H} = (0, 0.4)^5$	M1*	For evoluting D (NINININI) under H
(ii) (a) P(NNNNN) under $H_0 = (0.94)^5$ = 0.7339	A1	For evaluating P(NNNNN) under H ₀ For correct answer (could be implied)
P(Type I error) = 1 - 0.7339	M1*	For identifying the Type I error outcome
= 0.266	Alft	For correct final answer
	dep*	SR If M0M0 allow B1 for Bin(5,0.94)used
	[4]	
(b) P(NNNNN) under $H_1 = (0.7)^5$	M1	For Bin(5,0.7) used
= 0.168	M1	For P(NNNN) under H_1
P(Type II) error = 0.168	Al	For correct final answer
	[3]	
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~		
7 (i) $\int_{0}^{\infty} k e^{-3x} dx = 1$	M1	For attempting to integrate from 0 to $\infty$ and putting the integral = 1
$0 - \frac{-k}{3} = 1 \Longrightarrow k = 3$	A1	For obtaining given answer correctly
	[2]	
(ii) $\int_{1}^{q_1} 3e^{-3x} dx = 0.25$	M1	For equating $\int 3e^{-3x} dx$ to 0.25 (no limits
0	1711	5
		needed)
$\left[-e^{-3x}\right]_{0}^{q_{1}}=0.25$	M1	For attempting to integrate and substituting
$-e^{-3q_1} + 1 = 0.25$		(sensible) limits and rearranging
$0.75 = e^{-3q1}$	A 1	
$q_1 = 0.0959$	A1	For correct answer
	[3]	
		1

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Page 3	Mark Sche	eme		Syllabus	Paper
	A AND AS LEVEL – NO	OVEMB	ER 2003	9709/8719	7
$=\left[\frac{e}{e}\right]$	$e^{-3x} dx$ $e^{-3x} xe^{-3x} \Big]_{0}^{\infty} - \int_{0}^{\infty} -e^{-3x} dx$ $\left[\frac{e^{-3x}}{-3}\right]_{0}^{\infty}$ 333 or 1/3	B1 M1 A1 M1 A1 A1 <b>[6]</b>	For correct state For attempting to needed) For $-xe^{-3x}$ or $-$ For attempt $\int -$ For 0+ $\left[\frac{e^{-3x}}{-3}\right]$ For correct ans	to integrate $3xe^{-3x}/3$ $e^{-3x} dx$ (their $\infty$	- ^{3x} (no limits