

2. A circle C with centre at the point $(2, -1)$ passes through the point A at $(4, -5)$.

(a) Find an equation for the circle C . (3)

(b) Find an equation of the tangent to the circle C at the point A , giving your answer in the form $ax + by + c = 0$, where a , b and c are integers. (4)



4.

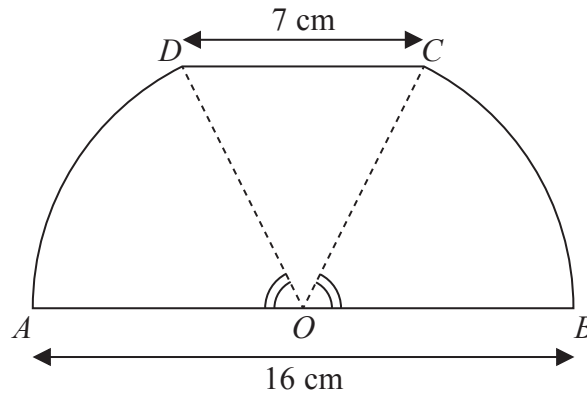


Figure 1

Figure 1 shows a sketch of a design for a scraper blade. The blade *AOBCDA* consists of an isosceles triangle *COD* joined along its equal sides to sectors *OBC* and *ODA* of a circle with centre *O* and radius 8 cm. Angles *AOD* and *BOC* are equal. *AOB* is a straight line and is parallel to the line *DC*. *DC* has length 7 cm.

- (a) Show that the angle *COD* is 0.906 radians, correct to 3 significant figures. (2)
- (b) Find the perimeter of *AOBCDA*, giving your answer to 3 significant figures. (3)
- (c) Find the area of *AOBCDA*, giving your answer to 3 significant figures. (3)



Question 5 continued

Lined writing area for the answer to Question 5.



P 4 3 1 7 8 A 0 1 5 3 2

6. (a) Find

$$\int 10x(x^{\frac{1}{2}} - 2)dx$$

giving each term in its simplest form.

(4)

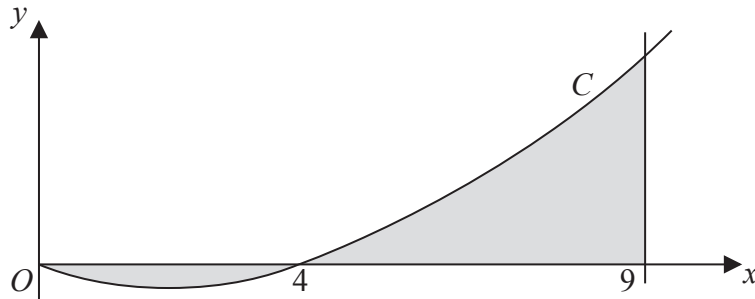


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = 10x(x^{\frac{1}{2}} - 2), \quad x \geq 0$$

The curve C starts at the origin and crosses the x -axis at the point $(4, 0)$.

The area, shown shaded in Figure 2, consists of two finite regions and is bounded by the curve C , the x -axis and the line $x = 9$

(b) Use your answer from part (a) to find the total area of the shaded regions.

(5)



Question 6 continued

Lined writing area for the answer to Question 6.



P 4 3 1 7 8 A 0 1 9 3 2

Question 6 continued



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Question 6 continued

Lined area for writing the answer to Question 6.

(Total 9 marks)

Q6



P 4 3 1 7 8 A 0 2 1 3 2

- 7. (i) Use logarithms to solve the equation $8^{2x+1} = 24$, giving your answer to 3 decimal places.

(3)

- (ii) Find the values of y such that

$$\log_2(11y - 3) - \log_2 3 - 2 \log_2 y = 1, \quad y > \frac{3}{11}$$

(6)



Question 7 continued

A large vertical rectangular area containing horizontal ruling lines for writing. The lines are evenly spaced and extend across most of the width of the page.



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Question 7 continued

Lined area for writing the answer to Question 7.

(Total 9 marks)

Q7



8. (i) Solve, for $0 \leq \theta < \pi$, the equation

$$\sin 3\theta - \sqrt{3} \cos 3\theta = 0$$

giving your answers in terms of π .

(3)

- (ii) Given that

$$4\sin^2 x + \cos x = 4 - k, \quad 0 \leq k \leq 3$$

- (a) find $\cos x$ in terms of k .

(3)

- (b) When $k = 3$, find the values of x in the range $0 \leq x < 360^\circ$

(3)



9. A solid glass cylinder, which is used in an expensive laser amplifier, has a volume of $75\pi\text{ cm}^3$.

The cost of polishing the surface area of this glass cylinder is £2 per cm^2 for the curved surface area and £3 per cm^2 for the circular top and base areas.

Given that the radius of the cylinder is r cm,

- (a) show that the cost of the polishing, £ C , is given by

$$C = 6\pi r^2 + \frac{300\pi}{r} \quad (4)$$

- (b) Use calculus to find the minimum cost of the polishing, giving your answer to the nearest pound. (5)

- (c) Justify that the answer that you have obtained in part (b) is a minimum. (1)



