



1. Simplify

(a)  $(2\sqrt{5})^2$  (1)

(b)  $\frac{\sqrt{2}}{2\sqrt{5} - 3\sqrt{2}}$  giving your answer in the form  $a + \sqrt{b}$ , where  $a$  and  $b$  are integers. (4)

Handwriting lines for the answer.





2. Solve the simultaneous equations

$$y - 2x - 4 = 0$$

$$4x^2 + y^2 + 20x = 0$$

(7)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---









4. (i) A sequence  $U_1, U_2, U_3, \dots$  is defined by

$$U_{n+2} = 2U_{n+1} - U_n, \quad n \geq 1$$

$$U_1 = 4 \text{ and } U_2 = 4$$

Find the value of

(a)  $U_3$

(1)

(b)  $\sum_{n=1}^{20} U_n$

(2)

- (ii) Another sequence  $V_1, V_2, V_3, \dots$  is defined by

$$V_{n+2} = 2V_{n+1} - V_n, \quad n \geq 1$$

$$V_1 = k \text{ and } V_2 = 2k, \text{ where } k \text{ is a constant}$$

- (a) Find  $V_3$  and  $V_4$  in terms of  $k$ .

(2)

Given that  $\sum_{n=1}^5 V_n = 165,$

- (b) find the value of  $k$ .

(3)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---























































