

Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} .$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$.

2. TRIGONOMETRY*Identities*

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

Formulae for ΔABC

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

- 1 Show that $\sec x - \cos x = \sin x \tan x$. [3]
- 2 A 4-digit number is formed by using four of the seven digits 2, 3, 4, 5, 6, 7 and 8. No digit can be used more than once in any one number. Find how many different 4-digit numbers can be formed if
- (i) there are no restrictions, [2]
- (ii) the number is even. [2]
- 3 The line $y = mx + 2$ is a tangent to the curve $y = x^2 + 12x + 18$. Find the possible values of m . [4]
- 4 The remainder when the expression $x^3 + kx^2 - 5x - 3$ is divided by $x - 2$ is 5 times the remainder when the expression is divided by $x + 1$. Find the value of k . [4]
- 5 Solve the simultaneous equations
- $$\log_3 a = 2 \log_3 b,$$
- $$\log_3 (2a - b) = 1. \quad [5]$$
- 6 Solve the equation $3x^3 + 7x^2 - 22x - 8 = 0$. [6]
- 7 (i) Sketch the graph of $y = |3x - 5|$, for $-2 \leq x \leq 3$, showing the coordinates of the points where the graph meets the axes. [3]
- (ii) On the same diagram, sketch the graph of $y = 8x$. [1]
- (iii) Solve the equation $8x = |3x - 5|$. [3]
- 8 (a) A function f is defined, for $x \in \mathbb{R}$, by
- $$f(x) = x^2 + 4x - 6.$$
- (i) Find the least value of $f(x)$ and the value of x for which it occurs. [2]
- (ii) Hence write down a suitable domain for $f(x)$ in order that $f^{-1}(x)$ exists. [1]
- (b) Functions g and h are defined, for $x \in \mathbb{R}$, by
- $$g(x) = \frac{x}{2} - 1,$$
- $$h(x) = x^2 - x.$$
- (i) Find $g^{-1}(x)$. [2]
- (ii) Solve $gh(x) = g^{-1}(x)$. [3]

9 (a) Find $\int \left(x^{\frac{1}{3}} - 3\right)^2 dx$. [3]

(b) (i) Given that $y = x \sqrt{x^2 + 6}$, find $\frac{dy}{dx}$. [3]

(ii) Hence find $\int \frac{x^2 + 3}{\sqrt{x^2 + 6}} dx$. [2]

10 A particle travels in a straight line so that, t s after passing through a fixed point O , its displacement s m from O is given by $s = \ln(t^2 + 1)$.

(i) Find the value of t when $s = 5$. [2]

(ii) Find the distance travelled by the particle during the third second. [2]

(iii) Show that, when $t = 2$, the velocity of the particle is 0.8 ms^{-1} . [2]

(iv) Find the acceleration of the particle when $t = 2$. [3]

11 Solve the equation

(i) $3 \sin x - 4 \cos x = 0$, for $0^\circ \leq x \leq 360^\circ$, [3]

(ii) $11 \sin y + 1 = 4 \cos^2 y$, for $0^\circ \leq y \leq 360^\circ$, [4]

(iii) $\sec\left(2z + \frac{\pi}{3}\right) = -2$, for $0 \leq z \leq \pi$ radians. [4]

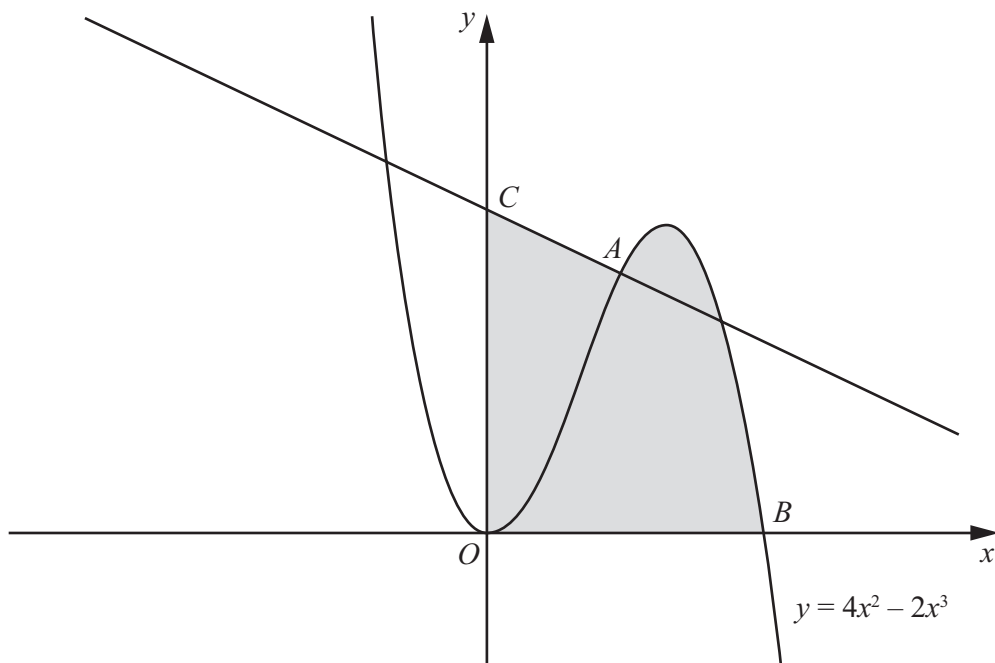
12 Answer only **one** of the following two alternatives.

EITHER

A curve has the equation $y = A \sin 2x + B \cos 3x$. The curve passes through the point with coordinates $\left(\frac{\pi}{12}, 3\right)$ and has a gradient of -4 when $x = \frac{\pi}{3}$.

- (i) Show that $A = 4$ and find the value of B . [6]
- (ii) Given that, for $0 \leq x \leq \frac{\pi}{3}$, the curve lies above the x -axis, find the area of the region enclosed by the curve, the y -axis and the line $x = \frac{\pi}{3}$. [5]

OR



The diagram shows the curve $y = 4x^2 - 2x^3$. The point A lies on the curve and the x -coordinate of A is 1. The curve crosses the x -axis at the point B. The normal to the curve at the point A crosses the y -axis at the point C.

- (i) Show that the coordinates of C are $(0, 2.5)$. [5]
- (ii) Find the area of the shaded region. [6]

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