



# Cambridge O Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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**ADDITIONAL MATHEMATICS**

**4037/14**

Paper 1

**May/June 2021**

**2 hours**

You must answer on the question paper.

No additional materials are needed.

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages.

**Mathematical Formulae****1. ALGEBRA***Quadratic Equation*

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

*Binomial Theorem*

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where  $n$  is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

*Arithmetic series*      $u_n = a + (n-1)d$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

*Geometric series*      $u_n = ar^{n-1}$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_\infty = \frac{a}{1-r} \quad (|r| < 1)$$

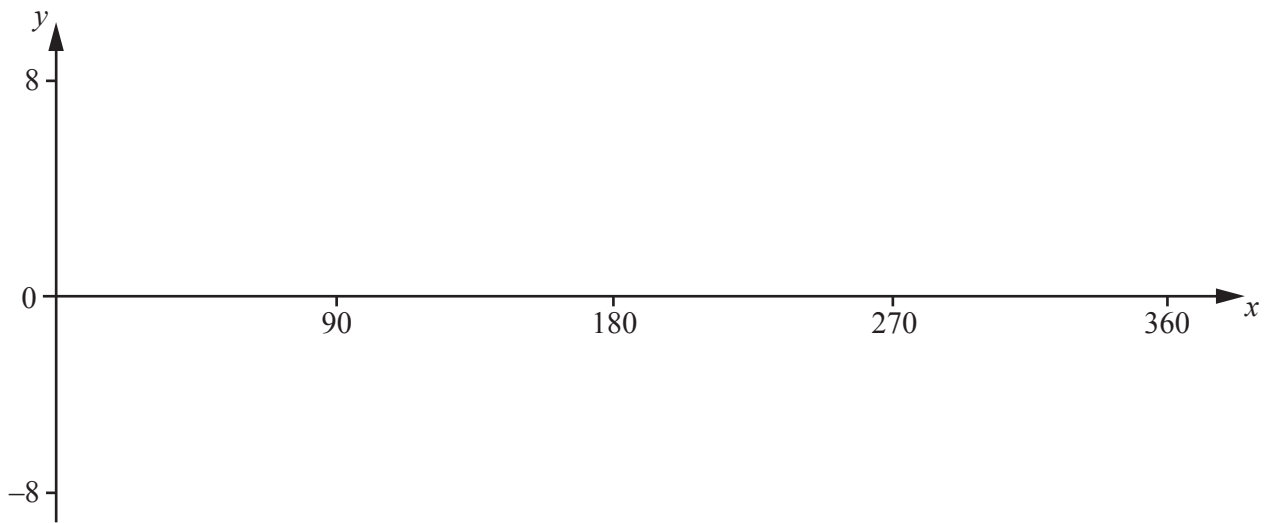
**2. TRIGONOMETRY***Identities*

$$\begin{aligned} \sin^2 A + \cos^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \operatorname{cosec}^2 A &= 1 + \cot^2 A \end{aligned}$$

*Formulae for  $\triangle ABC$* 

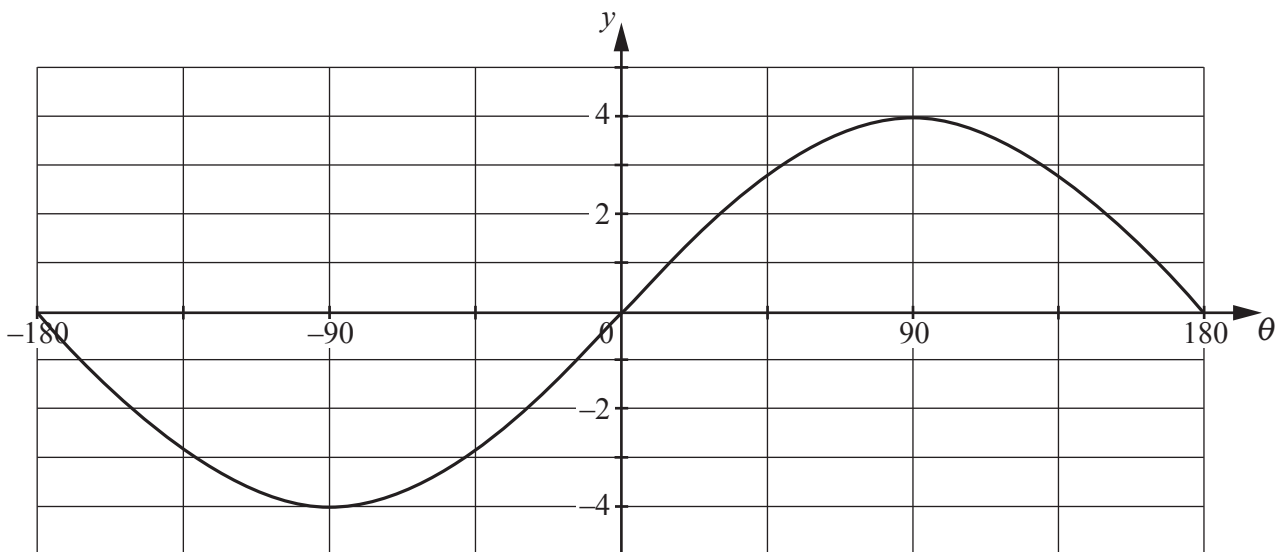
$$\begin{aligned} \frac{a}{\sin A} &= \frac{b}{\sin B} = \frac{c}{\sin C} \\ a^2 &= b^2 + c^2 - 2bc \cos A \\ \Delta &= \frac{1}{2}bc \sin A \end{aligned}$$

1 (a) On the axes below, sketch the graph of  $y = 6 \cos 2x - 1$  for  $0^\circ \leq x \leq 360^\circ$ .



[3]

(b) The graph of  $y = a + b \sin c\theta$  for  $-180^\circ \leq \theta \leq 180^\circ$  is shown below.

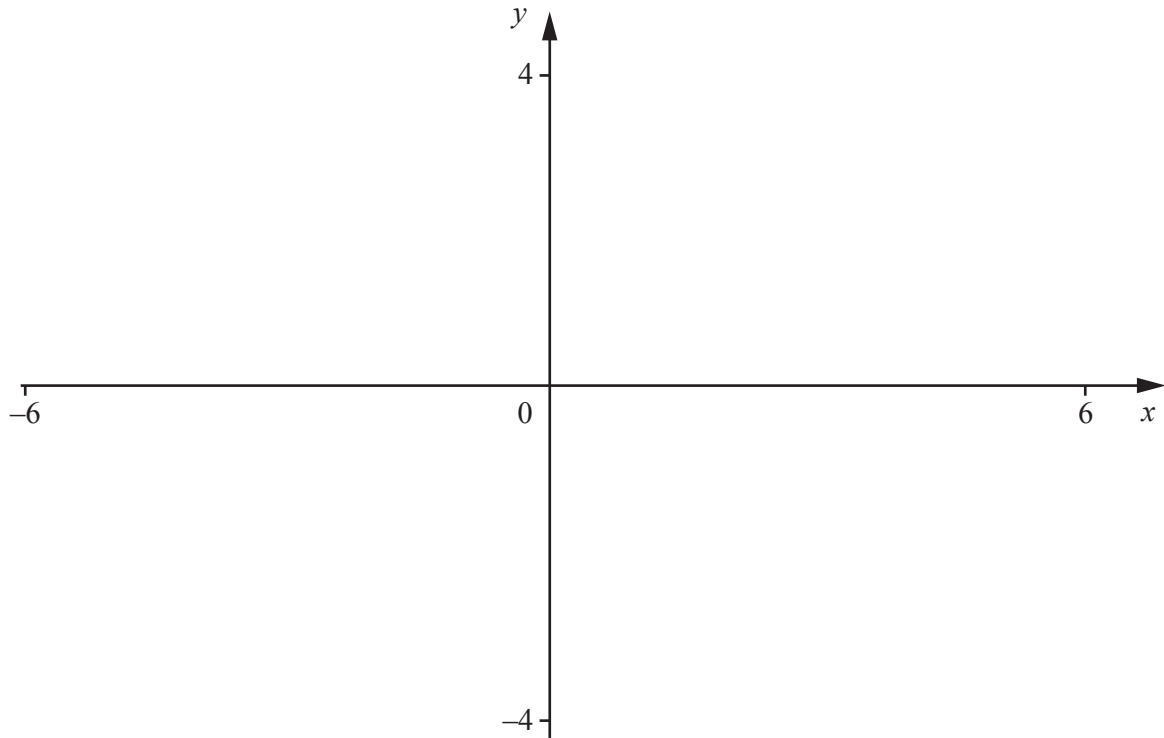


Write down the value of each of the constants  $a$ ,  $b$  and  $c$ .

[2]

$a = \dots\dots\dots$        $b = \dots\dots\dots$        $c = \dots\dots\dots$

- 2 (a) On the axes below, sketch the graphs of  $y = |x - 3|$  and  $y = \left|\frac{2}{5}x\right|$ , giving the coordinates of the points where the graphs meet the axes. [3]



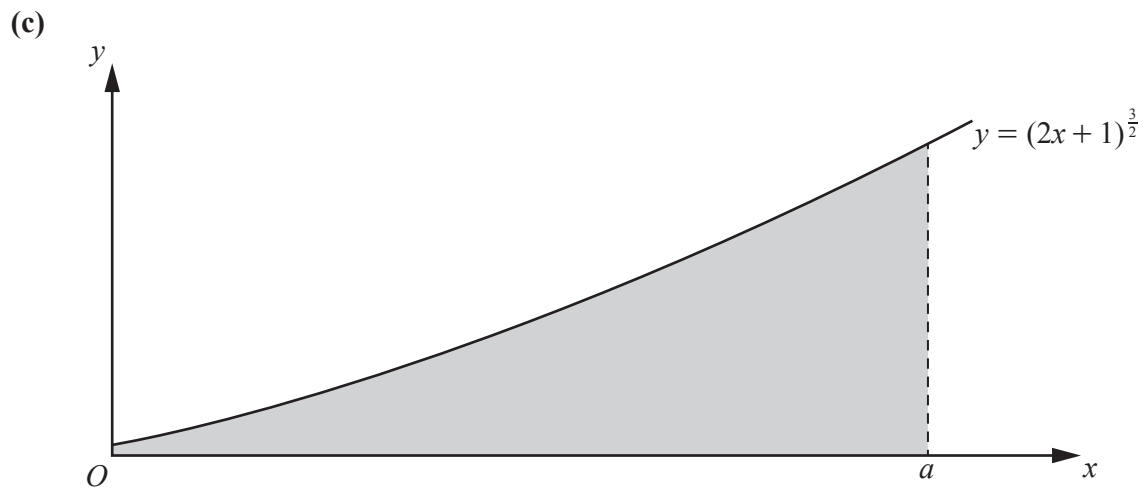
- (b) Solve the equation  $\left|\frac{2}{5}x\right| = |x - 3|$ . [2]

- 3 (a) Find the first 3 terms in the expansion, in ascending powers of  $x$ , of  $(a-3x)^{10}$ , where  $a$  is a constant. [3]

- (b) Given that  $a$  is positive and that the three terms found in **part (a)** can also be written as  $p + qx + \frac{405}{256}x^2$ , find the value of each of the constants  $a$ ,  $p$  and  $q$ . [3]

4 (a) Find  $\frac{d}{dx}(2x+1)^{\frac{5}{2}}$ . [2]

(b) Hence find  $\int (2x+1)^{\frac{3}{2}} dx$ . [2]



The diagram shows the graph of the curve  $y = (2x + 1)^{\frac{3}{2}}$  for  $x \geq 0$ . The shaded region enclosed by the curve, the axes and the line  $x = a$  is equal to 48.4 square units. Find the value of  $a$ , showing all your working. [3]

- 5 (a)** A 5-digit number is to be formed from the digits 2, 5, 6, 7 and 9. Each digit may only be used once.
- (i)** Find the number of different 5-digit numbers that can be formed. [1]
- (ii)** Find the percentage of these numbers that are odd. [2]
- (b)** 12 people are placed at random in 3 groups of 4 people each. Find the number of ways that this can be done. [3]



6 (a) Solve the simultaneous equations

$$\log_a(x+y) = 0,$$

$$\log_a(x+1) = 2\log_a y.$$

[4]

(b) Given that  $\log_p q^2 \times \log_q p^3 = A$ , find the value of the constant  $A$ .

[3]

- 7 A curve is such that  $\frac{d^2y}{dx^2} = 8 \sin 2x$ . The curve has a gradient of 6 at the point  $\left(\frac{\pi}{2}, 4\pi\right)$ .

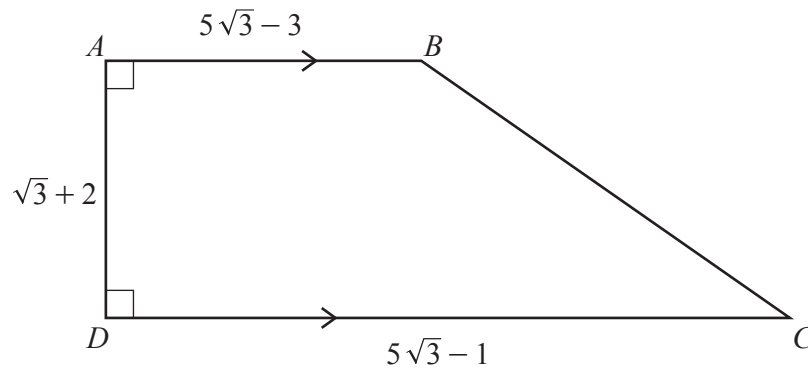
Find the equation of the curve.

[8]

- 8 The polynomial  $p(x)$  is  $ax^3 + bx^2 + 7x + 1$ , where  $a$  and  $b$  are integers. It is given that  $2x + 1$  is a factor of  $p(x)$  and that when  $p(x)$  is divided by  $x - 3$  there is a remainder of 175.
- (a) Find the value of  $a$  and of  $b$ . [5]

- (b) Using your values of  $a$  and  $b$  from **part (a)**, find the remainder when  $p'(x)$  is divided by  $x - 1$ . [3]

- 9 In this question all lengths are in centimetres.  
**Do not use a calculator in this question.**



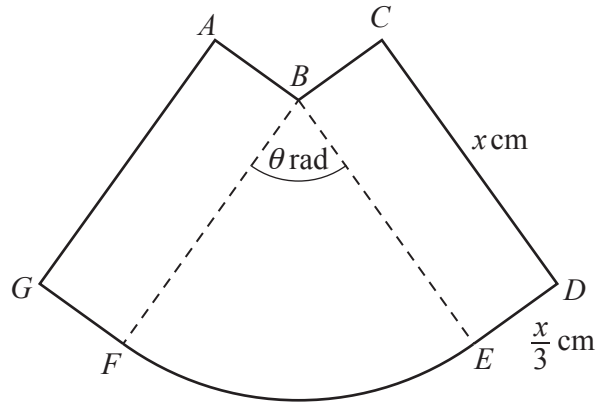
The diagram shows the trapezium  $ABCD$ , where  $AB = 5\sqrt{3} - 3$ ,  $DC = 5\sqrt{3} - 1$  and  $AD = \sqrt{3} + 2$ .

- (a) Find the area of  $ABCD$ , giving your answer in the form  $a + b\sqrt{3}$ , where  $a$  and  $b$  are integers. [3]

- (b) Given that angle  $BCD = \theta$  radians, find the value of  $\cot \theta$  in the form  $c + d\sqrt{3}$ , where  $c$  and  $d$  are integers. [3]

- (c) Using your answer to **part (b)**, find the value of  $\operatorname{cosec}^2 \theta$  in the form  $e + f\sqrt{3}$ , where  $e$  and  $f$  are integers. [2]

10



The diagram shows the figure  $ABCDEFG$ , where  $ABFG$  and  $BCDE$  are rectangles of length  $x$  cm and width  $\frac{x}{3}$  cm. The sector  $BFE$  of the circle, centre  $B$ , radius  $x$  cm, has an angle of  $\theta$  radians. It is given that the area of  $BFE$  is  $2$  cm<sup>2</sup>.

- (a) Show that the perimeter,  $P$  cm, of the figure  $ABCDEFG$  is given by  $P = \frac{10x}{3} + \frac{4}{x}$ . [5]

- (b) Given that  $x$  can vary, find the minimum value of  $P$  in the form  $q\sqrt{30}$ , where  $q$  is a rational number. [4]

- (c) Verify that  $P$  is a minimum. [1]

**Question 11 is printed on the next page.**

- 11 The tangent at the point where  $x = 1$  on the curve  $y = 6x \ln(x^2 + 1)$  intersects the  $y$ -axis at the point  $P$ . This tangent also intersects the line  $x = 2$  at the point  $Q$ . A line through  $P$ , parallel to the  $x$ -axis, meets the line  $x = 2$  at the point  $R$ . Find the exact area of triangle  $PQR$ . [10]

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