

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

General Certificate of Education Ordinary Level

MARK SCHEME for the June 2004 question papers

4024 MATHEMATICS (Syllabus D)

4024/01	Paper 1, maximum raw mark 80
4024/02	Paper 2, maximum raw mark 100

These mark schemes are published as an aid to teachers and students, to indicate the requirements of the examination. They show the basis on which Examiners were initially instructed to award marks. They do not indicate the details of the discussions that took place at an Examiners' meeting before marking began. Any substantial changes to the mark scheme that arose from these discussions will be recorded in the published *Report on the Examination*.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the *Report on the Examination*.

- CIE will not enter into discussion or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the June 2004 question papers for most IGCSE and GCE Advanced Level syllabuses.

TYPES OF MARK

Most of the marks (those without prefixes, and 'B' marks) are given for accurate results, drawings or statements.

- **M** marks are given for a correct method.
- **B** marks are given for a correct statement or step.
- **A** marks are given for an accurate answer following a correct method.

ABBREVIATIONS

a.r.t.	Anything rounding to
b.o.d.	Benefit of the doubt has been given to the candidate
c.a.o.	Correct answer only (i.e. no 'follow through')
e.e.o.	Each error or omission
f.t.	Follow through
o.e.	Or equivalent
SC	Special case
s.o.i.	Seen or implied
ww	Without working
www	Without wrong working
*	Indicates that it is necessary to look in the working following a wrong answer



June 2004

GCE ORDINARY LEVEL

MARKING SCHEME

MAXIMUM MARK: 80

SYLLABUS/COMPONENT: 4024/01

MATHEMATICS (Syllabus D)
Paper 1



Page 1	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	1

1	(a) (0).07 cao (b) 8(.00....) (%)	1 1			2	
2	(a) $\frac{2}{3}$ cao (b) $\frac{19k}{21k}$ cao	1 1	Allow decimal in range (0).904 to (0).905		2	
3	(a) 70 cao (b) $1 + 72 + (4 \times 2) = 10$	1 1	(Not 70/1) Both brackets needed. Ignore extra <u>pairs</u> if not wrong		2	
4	(a) $9x^6$ (b) 4	1 1	Accept ± 4 , but not - 4 or $16^{\frac{1}{2}}$	2		
5	(a) 64 (b) 58	1 1			2	
6	(a) 10 (b) $\frac{1}{\text{their (a)}} \begin{pmatrix} 2 & 1 \\ -4 & 3 \end{pmatrix}$ or correct answer	1 1	Accept equivalents Both brackets essential		2	12
7	11 Accept 10.99 (from $\pi = 3.14$)	2	11/2 , $5\frac{1}{2}$ or 5.5 or Figs $\left(\frac{3+3}{360} \times 2 \times \pi \times 105\right)$ seen	C1 M1	2	
8	Condone missing outside brackets and Final answer $\frac{x+7}{(x-3)(x+2)}$ or $\frac{x+7}{x^2-x-6}$	2	use of wrong letter if clear Correct num, but brackets missing in denom or $\frac{2(x+2)-(x-3)}{(x-3)(x+2)}$ oe soi [Condone all missing brackets] [Only available if some working seen]	C1 M1	2	

Page 2	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	1

9 (a)	10	1				
(b)	8	1			2	
10(a)	2.173×10^4 cao	1	Accept . for x Do not accept calculator form	C1	3	
(b)	0.031×10^5 , 217.3×10^2 , 22.6×10^3 , 2.5×10^4 or equivalents	2	Order reversed or Least or greatest identified Condone minor slips if intention clear	C1 C1		
11(a)	2	1		C1	3	
(b)	(c =) 3 (x) (d =) - 5	1 1	One correct or ($f^{-1} : x \rightarrow$) $3x - 5$ seen in working	C1 M1		
12(a)	-8(.0)	1		M1	3	15
(b)	$22\frac{1}{2}$ or 22.5 cao	2	$\frac{6}{t} = \frac{4}{15}$ oe or better seen (not just in ratio form)			
13(a)	Ruled straight line through (0, 0) and (157.5, 40 000)	1	Allow tolerance of $\frac{1}{2}$ small square at points			
(b)	(i) 8500 to 9000	1				
	(ii) $\frac{1}{8}$ or (0).125 cao	1	Condone 1: 8		3	
14(a)	$2\frac{1}{2}$, 2.5 or $\frac{5}{2}$	1	Ignore reference to y coordinate if it is -1	C1	3	
(b)	$y > -1$, $y < x + 3$ and $y + 2x < 4$ oe Accept \geq for $>$ etc throughout	2	All inequalities reversed or Two inequalities correct	C1 C1		
15(a)	(0)68 ⁽⁰⁾	1	Ignore embellishments (eg N 68 E)	C1	3	9
(b)	199 to 201 ⁽⁰⁾	2	Ignore embellishments such as S 199 W Other value in range 196 to 204 or (BAC =) 109 to 111 or (BCA =) 47 to 49 or (ACS =) 19 to 21 or for S 19 to 21 W seen or implied, possibly on diagram	M1		

Page 3	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	1

16(a)	1.515 m oe	1	Unit essential in this case			
(b)	3.96	2	Figs 396 or Figs $\frac{2 \times 0.55 \times 60 \times 60}{1000}$	C1 M1	3	
17	Both 3 and -5	3	$3 \times 4 = x^2 + 3x - x \pm 3$ or better seen and $(x + 5)(x - 3)$ oe seen, condoning missing outside brackets or $\frac{-2 \pm \sqrt{64}}{2}$ obtained	M1 M1	3	
18	40	3	$7^2 = 3^2 + \ell^{(2)}$ seen or implied, eg by $\sqrt{40}$ or $7^2 = 3^2 + 3^2 + \ell^{(2)}$ soi eg by 31 or $\sqrt{31}$ or 6, 7 used correctly	M2 M1 M1	3	
19(a)	30 (%)	2	70 (%) or Figs $\left(\frac{400 - 280}{400} \times 100 \right)$	C1 M1		
(b)	(\$) 20	2	(\$) 520 or Figs $\left(\frac{500 \times 6 \times 8}{100 \times 12} \right)$ seen, if intention clear	C1 M1	4	13
20	Circular arc, centre B, radius 6.5 ± 0.5 cm One line parallel to one coast One arc of circle linking two of these Region clearly identified	1 1 1 1	Subtending at least 90° at B Parallel by eye, 2 ± 0.5 cm from coasts as long as relevant coast or till it cuts circle Dep on large circular arc and 3 parallel lines, but not lost for wrong measurements Ignore superfluous lines		4	
21(a)	(i) 2 cao (ii) 2.65 to 2.7(0)	1 1	Not 2/1 Ignore any attempt at $x = 0$			
(b)	(i) 0.5 (ii) 3	1 1	Do not accept $x < 2.65$ Condone intrusion of y value of about 6.4 Accept $\frac{1}{2}$		4	8

Page 4	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	1

22(a)	(i) 107(°)	1	Accept on diagram if necessary			
	(ii) 34(°)	1	Accept on diagram if necessary			
(b)	Completely correct solution	2	Any reference to angle at centre, 146 = 2 x 73 or CEA = 2 x CBA or reference to angles in same segment soi	1 1	4	
23(a)	Condone missing outside brackets, "=0", and use of wrong letter if clear If only "solutions" (even incorrect) in answer space, award marks in working space $5(a - 2)(a + 2)$ oe	2	Incomplete factorisation seen e.g. $5(a^2 - 4)$, $(5a - 10)(a + 2)$ etc	M1		
(b)	(i) - 8	1				
	(ii) $-\frac{k}{2k}$ or - (0).5 cao	1	No follow through. Not \pm .		4	8
24	31 (m)	4	30.6, 30.7, 30.65 or 30.8 or Appropriate diagram or attempt to add 1.8 and $50 \tan 30$ oe or 50×0.577 and Rounding finally to the nearest integer provided some rounding has taken place Accept a reasonable eye level used	C3 M1 M1 M1	4	
25(a)	(i) $2^4 \times 3^2 \times 7^2$ oe	2	Attempted division by same prime at least twice, soi	M1		
	(ii) $(\pm) 84$ cao	1	Not just - 84			
(b)	$(p =) (\pm) 9$, $(q =) (\pm) 4$	1	Any combination of + and - acceptable			
(c)	Any irrational, with no rationals given	1	= 3.142 does not score		5	9

Page 5	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	1

26(a)	(One way) stretch	dep	1	Ignore reference to invariant line			
	Factor 2		1	No other transformation to be stated			
	(b) (i) $\begin{pmatrix} 8 \\ 0 \end{pmatrix}$		1	Brackets essential. Not (8 , 0)			
	(ii)(a) A' at A, (4 , 0) C' at (-7 , -2)		1	Labels not essential if triangle drawn			
			1	Labels essential if triangle not drawn			
	(b) 4		1	Accept (good) freehand triangle			
				Indep		6	6

June 2004

GCE ORDINARY LEVEL

MARKING SCHEME

MAXIMUM MARK: 100

SYLLABUS/COMPONENT: 4024/02

MATHEMATICS (Syllabus D)
Paper 2



Page 1	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	2

1	(a)	(i)	(a) 360 (m) (b) 4800 (m)	B1 B1	2	f.t. 5160 – their 360	
		(ii)	$\frac{6000 \times 3}{10}$ o.e. M1 = 1800 (m)	A1	2	sc1 for 4200 or 600s or 10min seen.	
		(iii)	$\frac{6000}{7}$ (s) M1 = 14m 17s	A1	2	Allow M1 if 857. ...seen	
	(b)	(i)	1 : 250000	B1	1	Allow $n = 250000$	
		(ii)	$2 \times \frac{6}{5}$ (figs) o.e. M1 = 2.4 cm	A1	2	e.g. $\frac{6000 \times 100}{250000}$ Accept 0.024m NB: figs 24→M1 immediately	
					9		
2	(a)		$(t - 5)(2v + 1)$ o.e.	B2	2	sc1 for any factor e.g. $2(tv - 5v)$ or if solution given.	
	(b)		$\frac{h}{k} = 9$ or $\sqrt{h} = 3\sqrt{k}$ M1 → $k = \frac{h}{9}$	A1	2	sc1 for any of: $k = \frac{\sqrt{h}}{3}, k = \frac{h}{\sqrt{3}}, k = \frac{h}{3^2}$	
	(c)		For numerical $\frac{p \pm (or + or -)\sqrt{q}}{r}$ $p = 23$ and $r = 2$ $q = 205$ or $\sqrt{q} = 14.3$ $x = 18.66$ 4.34	B1 B1 B1 B1	4	as final answer or $\left(x - \frac{23}{2}\right)^2$ B1, 51.25 B1	
	(d)		$\begin{pmatrix} 8 & 4 \\ -6 & 0 \end{pmatrix}$ Accept $a = 8, b = 4$ etc	B2	2	sc1 for 18.6→18.7 and 4.3→4.35 or for any two answers given to 2 dec. places. sc1 for 3 elements correct or $3Y = 2\begin{pmatrix} 12 & 6 \\ -9 & 0 \end{pmatrix}$	
						10	
3	(a)	(i)	30 (cm ²)	B1	1	Possible GRAD answers (a)(iii) 59.0...	
		(ii)	$\frac{1}{2} \times 5h + \frac{1}{2} \times 6 \times 4 =$ their 30 or 9 sin their $\hat{DAB} \rightarrow 7.18 \rightarrow 7.2$	M1 A1	2		
		(iii)	$\tan DAB = \frac{4}{3}$ (or $\sin DAB = \frac{7.2}{9}$ etc.) $\rightarrow 53 \rightarrow 53.14$	M1 A1	2		
	(b)	(i)	$\cos 51 = \frac{RS}{8}$ o.e. M1 → 5 → 5.04	A1	2		(b)(i) 5.56...
		(ii)	$\frac{\sin Q}{8} = \frac{\sin 95}{8.5}$ M1 → $\frac{8 \sin 95}{8.5}$ M1 (dep) $\rightarrow 69.6 \rightarrow 70$	A1	3		(b)(ii) 77.5...
		(iii)	(a) No: $PQR \neq 90$ or equiv (b) Mid pt of PR	B1 B1	2	Ignore superfluous reasoning.	
						12	

Page 2	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	2

4	(a)	$180 - \frac{360}{5}$ or $\frac{5-2}{5} \times 180$ o.e.	M1			
		$\rightarrow 108^\circ$	A1	2	AG	
			B1			
	(b) (i)	2 lines of symmetry Rot. sym. of order 2	B1	2		
	(ii)	Rhombus	B1		Accept diamond.	
	(iii)	252°	B1			
	(iv)	36°	B1	3		
	(c) (i)	40°	B1			
	(ii)	100°	B1			
	(iii)	120°		3		
				10	f.t. 220 – their 100	f.t.
5	(a)	$n(S \cup F)'$ or $n(S' \cap F')$ or $n(\quad) - n(S \cup F)$	B1	1		
	(b)	$y + 80 + 35 - x = 100$ o.e.	M1 $\rightarrow x - 15$ A1	2		
	(c) (i)	$x_{\min} = 15$	B1			
	(ii)	$y_{\max} = 20$	B1	2		
				5		
6	(a)	$p = 14$ $q = 27$	B1	1	<u>both</u>	
	(b)	$k = 2$	B1	1	Accept $3n + 2$	
	(c)	$7n$ -1	B1 B1	2	Accept unsimplified	
	(d)	$R = 41$ $B = 20$ 9 fences with either $\frac{400}{41}$ or $\frac{200}{20}$	B1 B1	2 6	NB: 9 fences without working sc1	

Page 3	Mark Scheme	Syllabus	Paper
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7	(a)	$2 \times 3^2 (56.5..)$ $+ 3^2 (28.2..)$ $= 84.8 - 84.834$	M1 M1 A1	3	
	(b)	$I = \sqrt{16^2 + 4^2} (16.5)$ $\rightarrow \text{CSA} = \pi \times 4 \times 16.5$ $= 207 - 207.5$	M1 M1 A1	3	
	(c) (i)	$\frac{r}{d} = \frac{4}{16} \text{ or } r = \frac{4d}{16}$	B1	1	A.G Alternatively: 4 <u>and</u> 16 with mention of shape or similarity o.e.
	(ii)	$V = \frac{1}{3} \times \pi \times 4^2 \times 16$ $= 267.9 \rightarrow 268.2$	M1 A1	2	
	(iii)	$\frac{1}{3} \pi r^2 d = \frac{268}{2}$ $\frac{1}{3} \pi \frac{d^3}{16} = \frac{268}{2} \text{ o.e.}$ $\rightarrow d = 12.69 - 12.7 \text{ (cm)}$	M1 M1	3	
				12	
8	(a)	Scales All 8 points correctly plotted (within 1 mm) Smooth curve through pts (allow marginally incorrect pts)	S1 P1 C1	3	Lost for st. lines, incomplete, grossly thick.
	(b) (i)	116 – 117	V1		Accept (4.5 , 116)
	(ii)	1.1 – 1.2 <u>and</u> 5.2 to 5.3	V1	2	DiHo Accept (1.1 , 128) , (5.2 , 128)
	(c)	suitable tangent 22 – 40	T1 T1	2	
	(d)	98	K1	1	(2.5 , 98) not accepted
	(e) (i)	$100 = \frac{A}{2} + 2B \rightarrow 200 = A + 4B$	E1		AG
	(ii)	$140 = A + B \text{ or } 100 = \frac{A}{3} + 3B \text{ etc.}$ $A = 120 \quad B = 20$	E1 B2	4	sc1 for attempt to solve $200 = A + 4B$ and 2 nd equation in A and B
				12	

Page 4	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	2

9	(a)	$(BC^2) = 7^2 + 8^2 - (or +) (2).7.8.\cos 120$ (or 60) $BC^2 = 7^2 + 8^2 - 2.7.8 \cos 120 \rightarrow BC = 13$	B1 B1	2	AG Possible GRAD answers (a) 12.4... (AG) (b) 26.62...
	(b)	Area = $\frac{1}{2} \cdot 7.8 \cdot \sin 120$ $= 24.2 - 24.25 \text{ (cm}^2\text{)}$	M1 A1	2	
	(c) (i)	$\frac{1}{2} \cdot 13 \cdot r$	B1		
	(ii)	$\frac{+1.7 \cdot r}{2} + \frac{1.8 \cdot r}{2}$ M1 = 14r	A1		
	(iii)	$14r = 24.2$ $r = 1.728 \rightarrow 1.733$	M1 A1	5	
	(d)	$24.2 - x \cdot 1.73^2$ M1 24.2 $= 61 - 61.2 \text{ (%)}$	M1 A1	3 12	
10	(a)	Widths 2, 1, 1, 2, 2, 3 Heights $3\frac{1}{2}$, 8, 6, 5, $1\frac{1}{2}$, 2 All correct (inc. given scales)	M1 M1 A1	3	Allow any clear indication. $fx = 63 + 84 + 69 + 130 + 45 + 105 = 496$ Allow 1 omission or 2 incorr mid pts not $\frac{0}{40}$ isw
	(b)	$11 < x \leq 12$	B1	1	
	(c)	fx (496) M1 f (40) M1 = 12.4 indep	A1	3	
	(d)	26	B1	1	
	(e) (i)	0	B1		
	(ii)	$\frac{6}{40}$	B1		
	(f)	$(2x) \frac{6}{40} \times \frac{34}{39}$ M1 = $\frac{17}{65}$	A1	4 12	

Page 5	Mark Scheme	Syllabus	Paper
	MATHEMATICS (Syllabus D) – JUNE 2004	4024	2

11	(a)	(i)	Number of events	B1		
		(ii)	(a) $\begin{pmatrix} 44 \\ 46 \end{pmatrix}$	B1 + B1		sc1 for (44, 46)
			(b) School scores, totals, no of points o.e.	B1 indep of (a)		
		(iii)	$\begin{pmatrix} 55 \\ 55 \end{pmatrix} \rightarrow \text{Yes, (tie)}$	B1	5	
(b)	(i)		$\overline{PX} = -\frac{1}{3}p + \frac{1}{3}q$ o.e	B1		Accept unsimplified answers
	(ii)		$\overline{OX} = \frac{2}{3}p + \frac{1}{3}q$ o.e	B1		Accept unsimplified answers
	(iii)		$\overline{QY} = p + (k-1)q$ o.e	B1	3	Accept unsimplified answers
	(iv)		$\lambda \overline{OX} = \overline{QY}$ M1 $k = \frac{3}{2}$	A1	2	
	(v)		$\overline{PZ} = \frac{1}{2}q$	B2	2	Accept unsimplified answers
					12	