

Cambridge IGCSE[™]

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MATHEMATICS 0580/43

Paper 4 (Extended)

October/November 2022

2 hours 30 minutes

You must answer on the question paper.

You will need: Geometrical instruments

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For π , use either your calculator value or 3.142.

INFORMATION

- The total mark for this paper is 130.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages. Any blank pages are indicated.

(a) Here are the ingredients needed to make a pasta bake to serve 12 people.

1

		250 g butter 600 g pasta 460 g mushrooms 280 g cheese 800 ml milk	
(i)	Find the mass of the chee	ese as a percentage of the ma	ass of the mushrooms.
(ii)	Find the mass of butter n	eeded to make a pasta bake	to serve 18 people.
			g [2]
(iii)	Monica has 2.2 litres of r	milk and 1.5 kg of each other	r ingredient.
	Calculate the greatest number of the calculate the calculate the greatest number of the calculate the greatest number of the calculate the calculate the greatest number of the calculate	mber of people she can serve	
			[3]

(b)		2019, a packet of pasta cost \$2.40. is was an increase of 25% of the cost of a packet in 2018.	
	(i)	Work out the cost in 2018.	
		\$	[2]
	(ii)	In 2020, the cost of a packet increased by 15% from the cost in 2	2019.
		Work out the total percentage increase in the cost of a packet fro	om 2018 to 2020.
			% [3]
(c)		width	
			NOT TO SCALE
			SCIEL
		sta is sold in packets with width 11.5 cm, correct to the nearest 0.5 chop places these packets in a single line on a shelf of length 2 m, c	
		nd the maximum number of these packets that will fit along this should be a second to the second the second that will be a second to the second that will be a second to the second to the second that will be a second to the sec	elf.
	You	u must show all your working.	

•		a. 1.c	C 11
2	(a)	Simplify	fully.

(i) $p^3 \times p^{11}$

.....[1]

(ii) $\frac{18m^6}{3m^2}$

.....[2]

(iii) $\left(\frac{27x^9y^{27}}{64}\right)^{-\frac{1}{3}}$

.....[3]

(b) A sequence has nth term $3n^2$.

Write down the first 3 terms of this sequence.

- (c) Find the *n*th term for each of these sequences.
 - (i) 13, 16, 19, 22, 25, ...

.....[2]

(ii) 3, 17, 55, 129, 251, ...

.....[2]

(d) Solve.

$$\frac{3x - 22}{4} = 23$$

x	=	 [3]
		F - 1

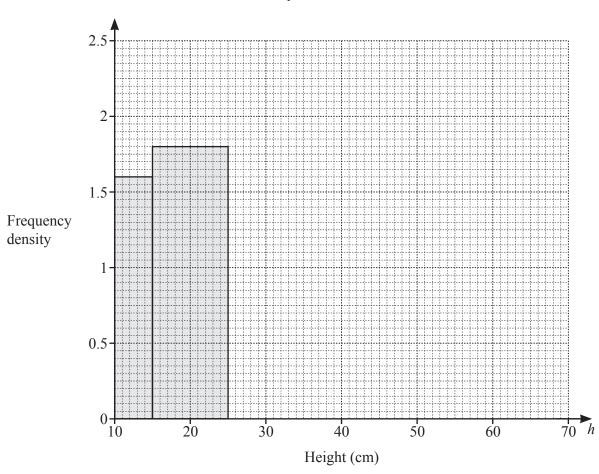
(e) Use the quadratic formula to solve $3x^2 + 8x - 20 = 0$. Show all your working and give your answers correct to 2 decimal places.

$$x = \dots, x = \dots$$
 [4]

3 The height, $h \, \text{cm}$, of each of 100 plants is recorded. The table shows information about the heights of these plants.

Height (h cm)	$10 < h \le 15$	15 < h ≤ 25	$25 < h \leqslant 40$	$40 < h \leqslant 60$	$60 < h \leqslant 70$
Frequency	8	18	28	33	13

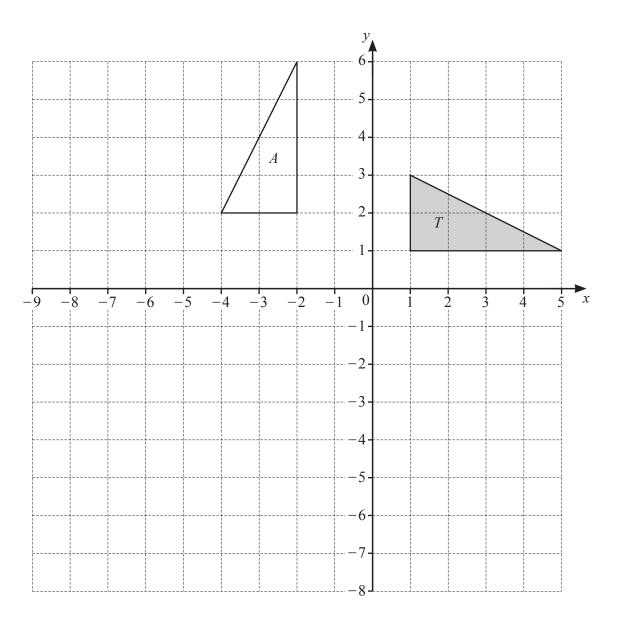
(a) Complete the histogram to show this information. The first two blocks have been drawn for you.



(b) Calculate an estimate of the mean height.

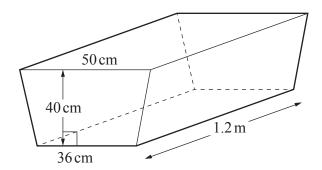
.....cm [4]

[3]



- (a) Draw the reflection of triangle T in the line y = -2. [2]
- **(b)** Draw the enlargement of triangle T with scale factor $\frac{1}{2}$ and centre of enlargement (-5, -3). [2]
- (c) Describe fully the **single** transformation that maps triangle T onto triangle A.

.....[3



NOT TO SCALE

The diagram shows a water trough in the shape of a prism.

The prism has a cross-section in the shape of an isosceles trapezium.

The trough is completely filled with water.

(a) Show that the volume of water in the trough is 206.4 litres.

[3]

(b) The water from the trough is emptied at a rate of 600 ml per second.

Calculate the time taken, in minutes and seconds, for the trough to be emptied.

..... minutes seconds [3]

- (c) All the water from the trough is emptied into a vertical cylindrical tank. The depth of the water in the tank is 84 cm.
 - (i) Calculate the radius of the tank.



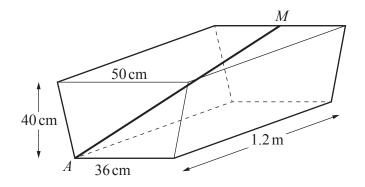
.....cm [3]

(ii) The tank is 60% full.

Calculate the height of the tank.

..... cm [2]

(d)



NOT TO SCALE

A steel rod AM is placed inside the empty water trough as shown in the diagram. A is a vertex at the base of the isosceles trapezium and M is the midpoint of the top edge on the opposite face.

Calculate the length of the steel rod, AM.

		2
6	(a)	$P = 5k^2 - 7$

(i) Find the value of P when k = 3.

$$P = \dots$$
 [2]

(ii) Rearrange the formula to make k the subject.

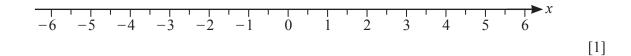
$$k = \dots [3]$$

(b) (i) Solve.

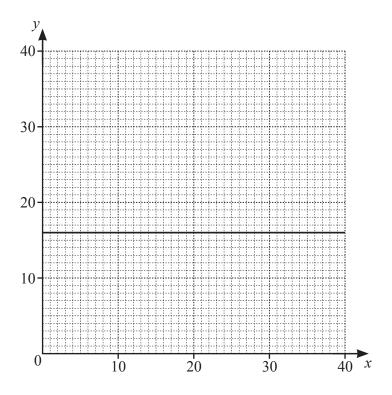
$$x - 3 \le 5x + 7$$

.....[2]

(ii) Show your answer to part (b)(i) on the number line.



(c) The line y = 16 is drawn on the grid.



The region R satisfies the following inequalities.

$$y \ge 16 \qquad x > 2 \qquad 2x + 3y \ge 72 \qquad y \le 32 - x$$

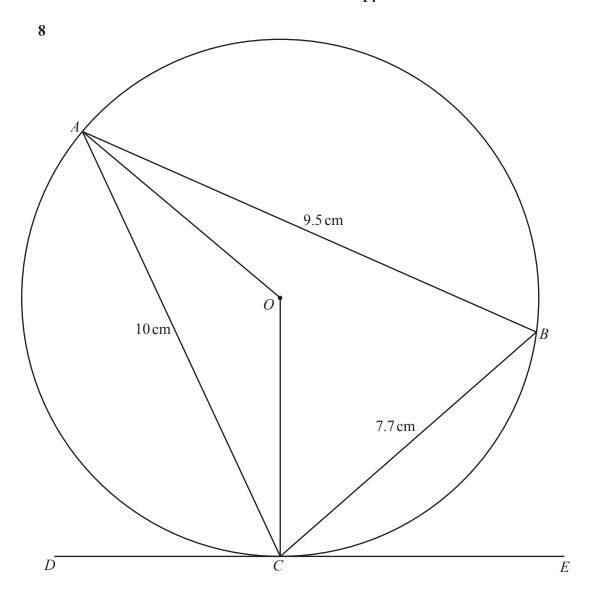
- (i) By drawing three more lines and shading the region **not required**, find and label region R. [6]
- (ii) Find the integer coordinates (x, y) in the region R that give the maximum value of 2x + y.

(.....) [2]

7	Reg	an is	playin	ng a ga	ame w	ith the	ese six	numb	er card	S.					
		-	-3		_2	2		2		3		5		7	
	(a)	She		two c	cards a	at rand	lom, w	vithout	replac	ement,	and m	ultiplies	the two	o number	rs to give a
		Fine	d the p	robab	ility th	nat									
		(i)	the sc	core is	s 35										
													•••••		[3]
		(ii)	the sc	core is	s a pos	itive n	number	r.							
															[3]

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(D)	three numbers to give a total.	tne
	Find the probability that her total is 5.	
		[4]



NOT TO SCALE

A, B and C are points on the circle, centre O. DE is a tangent to the circle at C. AC = 10 cm, AB = 9.5 cm and BC = 7.7 cm.

(a) Show that angle $ABC = 70.2^{\circ}$, correct to 1 decimal place.

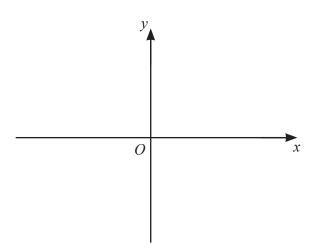
[4]

.....% [4]

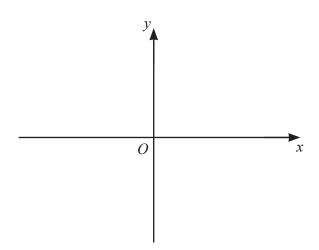
(b) Find(i) angle AOC	
(ii) angle ACO	Angle <i>AOC</i> = [1]
(iii) angle ACD.	Angle <i>ACO</i> = [1]
(c) Calculate the radius, <i>OC</i> , of the circle.	Angle <i>ACD</i> = [1]
(d) Calculate the area of triangle <i>ABC</i> as a percent	OC =

9 (a) Sketch the following graphs.
On each sketch, indicate any intercepts with the axes.

(i)
$$3x - 4y = 12$$

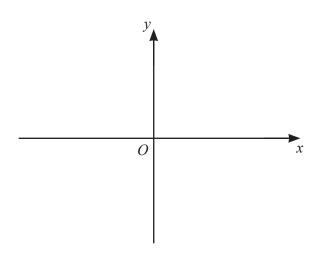


(ii)
$$y = x^2 - 3x - 4$$



[4]

(iii)
$$y = 6^x$$



[2]

(b)	(i)	Find the derivative,	$\frac{\mathrm{d}y}{\mathrm{d}x}$, of	y = 5 + 8x -	$\frac{4}{3}x^3$
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.....[2]

(ii) Find the gradient of $y = 5 + 8x - \frac{4}{3}x^3$ at x = -1.

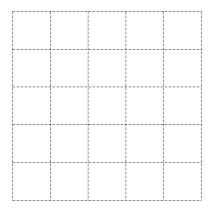
.....[2]

(iii) A tangent is drawn to the graph of $y = 5 + 8x - \frac{4}{3}x^3$. The gradient of the tangent is -28.

Find the coordinates of the two possible points where this tangent meets the graph.

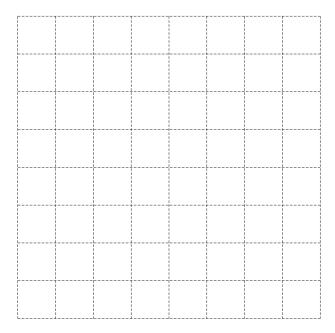
10 (a)
$$\mathbf{a} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$
 $\mathbf{b} = \begin{pmatrix} -3 \\ 5 \end{pmatrix}$

(i) On the grid, draw and label vector 2a.



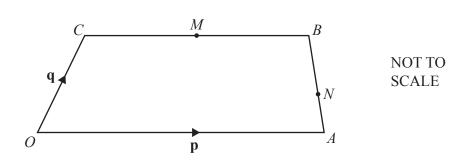
[1]

(ii) On the grid, draw and label vector $(\mathbf{a} - \mathbf{b})$.



[2]

(b)



OABC is a trapezium with *OA* parallel to *CB*.

M is the midpoint of CB and N is the point on AB such that AN : NB = 1 : 2.

O is the origin, $\overrightarrow{OA} = \mathbf{p}$, $\overrightarrow{OC} = \mathbf{q}$ and $\overrightarrow{CB} = \frac{3}{4}\mathbf{p}$.

- (i) Find, in terms of p and/or q, in its simplest form
 - (a) \overrightarrow{OB}

$\overrightarrow{OB} =$	 [1]
~ ~	L ^ J

(b) \overrightarrow{AB}

$$\overrightarrow{AB} = \dots$$
 [2]

(c) \overrightarrow{MN} .

$$\overrightarrow{MN} = \dots$$
 [3]

(ii) OA and MN are extended to meet at G.

Find the position vector of G in terms of \mathbf{p} .

.....[2

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