

Cambridge International Examinations Cambridge International General Certificate of Secondary Education

MATHEMATICS

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Paper 4 (Extended) MARK SCHEME Maximum Mark: 130

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Abbreviations

| cao | correct answer only |
|------|----------------------------|
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working |
| | . 1. 1 |

soi seen or implied

| Question | Answer | Marks | Part marks |
|-----------|----------------------------|-------|---|
| 1(a)(i) | 9550 | 1 | |
| 1(a)(ii) | 23 1 58 7 50 | 2FT | FT <i>their</i> (a)(i) × 2425 correctly evaluated M1 for <i>their</i> lower bound × 2425 |
| 1(a)(iii) | 23160000 | 1FT | FT their (a)(ii) rounded to 4 sf |
| 1(a)(iv) | 2.316×10^7 | 1FT | FT <i>their</i> (a)(iii) or <i>their</i> (a)(ii) rounded to 3sf or more and in standard form |
| 1(b) | 520 nfww | 3 | M2 for $546 \times \frac{100}{(100+5)}$ oe or M1 for 105[%] associated with 546 oe |
| 1(c) | 3380 or 3376 to 3377 | 2 | M1 for $3000 \times \left(1 + \frac{3}{100}\right)^4$ oe |
| 2(a) | 38 | 1 | |
| | 118 | 1 | |
| | 62 | 1FT | FT 180 – <i>their y</i> |
| 2(b) | 69 | 3 | B2 for $ACB = 42$ or B1 for $ADB = 42$ If zero scored, SC1 for $ACB = their ADB$ |
| 2(c) | 107 | 2 | B1 for <i>QPS</i> = 73 or [reflex] <i>QOS</i> = 214 |
| 3(a) | 0 2.25 2 1.25 | 4 | B1 for each |
| 3(b) | Fully correct smooth curve | 4 | B3 FT for 7 or 8 points or B2 FT for 5 or 6 points or B1 FT for 3 or 4 points |

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| Question | Answer | Marks | Part marks |
|----------|------------------------------------|---------|---|
| 3(c) | 1 | 1 | |
| 3(d)(i) | [y =] x + 1 | 1 | |
| 3(d)(ii) | -2.2 to -2.1 | 1 | |
| | -0.45 to -0.4 | 1 | |
| | 0.51 to 0.6 | 1 | If zero scored, SC1 for <i>their</i> line in (d)(i) drawn. It must be of the form $y = mx + c$ ($m \neq 0$) and drawn 'fit for purpose' |
| 3(e) | -1.33 < k < 0 to 0.1 | 2FT | FT Strict ft of <i>their</i> max point and min point dep on cubic graph or accept correct answer from calculus B1 for each If zero scored, SC1 for two correct values reversed |
| 4(a)(i) | 17.5 or 17.46nfww | 6 | B3 for triangle height 3.46[4] or $\sqrt{12}$ oe or M2 for $\sqrt{4^2 - 2^2}$ or M1 for $h^2 + 2^2 = 4^2$ and M2 for $2 \times 7 + \frac{1}{2} \times 2 \times their h$ oe |
| | | | or M1 for $\frac{1}{2} \times 2 \times their h$ |
| 4(a)(ii) | 140 or 139.6 to 139.7 | 1FT | FT their (a) $\times 8$ |
| 4(b)(i) | 2.62 or 2.618 | 3 | M2 for $[r^2 =] \frac{280}{13\pi}$ oe or M1 for $280 = \pi \times r^2 \times 13$ |
| 4(b)(ii) | 10.2 or 10.20 or $10\frac{10}{49}$ | 3 | M2 for $\frac{280}{14^3}$ [×100] oe |
| | | | or B1 for 2744 or 14^3 seen |
| 5(a)(i) | 80 33 20 | 1, 1, 1 | |
| 5(a)(ii) | 17.3 nfww | 4 | M1 for 5, 15, 22.5, 27.5, 40 soi |
| | | | M1 for $\sum fx$ with <i>their</i> f 's and x in correct interval including both boundaries |
| | | | M1 (dep on 2nd M1) for $\sum fx \div 200$ |

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| Question | Answer | Marks | Part marks |
|----------|--|-------|--|
| 5(b)(i) | $\frac{30}{210}$ oe | 2 | M1 for $\frac{6}{15} \times \frac{5}{14}$ If zero scored, SC1 for answer $\frac{36}{225}$ oe |
| 5(b)(ii) | 108/210 oe | 3 | M2 for $\frac{6}{15} \times \frac{9}{14} + \frac{9}{15} \times \frac{6}{14}$ oe or $1 - \frac{9}{15} \times \frac{8}{14} - \frac{6}{15} \times \frac{5}{14}$ or M1 for $\frac{6}{15} \times \frac{9}{14}$ or $\frac{9}{15} \times \frac{6}{14}$ or $\frac{9}{15} \times \frac{8}{14} + \frac{6}{15} \times \frac{5}{14}$ If zero scored, SC1 for answer $\frac{108}{225}$ oe |
| 5(c) | 150 | 1 | |
| 6(a)(i) | Translation | 1 | |
| | $\begin{pmatrix} 3\\ -13 \end{pmatrix}$ oe | 1 | |
| 6(a)(ii) | Enlargement | 1 | |
| | $[sf] - \frac{1}{2}$ oe | 1 | |
| | (0, -4) | 1 | |
| 6(b) | Image at (0,0)(0,6)(-4,6)(-4,2) | 2 | B1 for rotation of 90° anticlockwise about the wrong centre or 90° clockwise about $(3, -1)$ or 4 points correct but not joined. |
| 6(c) | Image at (4,0)(10,0)(10,-4)(6,-4) | 2 | B1 for reflection in $y = k$ or in $x = 1$ or 4 points correct but not joined |
| 6(d) | Enlargement | 1 | |
| | [sf]3 | 1 | |
| | Origin oe | 1 | |

| Question | Answer | Marks | Part marks |
|----------|--|-------|--|
| 7(a) | [x =] -5 | 4 | M1 for correctly equating one set of coefficients |
| | [y =] 7 with correct working | | M1 for correct method to eliminate one variable |
| | | | OR |
| | | | M1 for correctly rearranging one equation |
| | | | M1 for correct method to eliminate one variable |
| | | | A1 $x = -5$ A1 $y = 7$ both dep on M2 |
| | | | If zero scored, SC1 for 2 values satisfying one of the original equations |
| | | | SC1 if no correct working shown, but 2 correct answers given |
| 7(b) | [<i>a</i> =] 36 | 3 | B2 for either correct |
| | [b =] -6 | | or M1 for $a = b^2$ or for $x^2 + bx + bx + b^2$ or |
| | | | better or for $(x - 6)^2$ seen and M1 for $2b = -12$ soi |
| 7(c) | $\frac{7x^2 - 12x - 10}{(2x - 5)(x - 1)}$ of final answer nfww | 4 | B1 for common denom $(2x-5)(x-1)$ seen oe isw |
| | | | M1 for $x(x-1)+(3x+2)(2x-5)$ soi isw |
| | | | B1 for $6x^2 - 15x + 4x - 10$ soi |
| 8(a)(i) | 4 points correctly plotted | 2 | B1 for 2 or 3 points correctly plotted |
| 8(a)(ii) | Positive | 1 | |
| 8(b) | mean 3.1 | 3 | M2 for $\frac{\text{sum of products}}{30}$ |
| | | | or M1 for at least 4 correct products soi |
| | median 3 | 2 | M1 for 15.5 oe indicated |
| | mode 5 | 1 | |
| | range 5 | 1 | |
| 8(c) | 24 nfww | 3 | M1 for $\frac{x \times 52 + 45 \times 75 + 11 \times 91}{x + 45 + 11}$ [= 70.3] |
| | | | x + 45 + 11 M1 for clearing <i>their</i> fraction |

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| Question | Answer | Marks | Part marks |
|-----------|--|-------|---|
| 9(a) | 1120 or 1121 | 4 | M2 for $[AC^2 =]$ $525^2 + 872^2 - 2 \times 525 \times 872 \times \cos 104$ or M1 for implicit version A1 for 1257000 to 1258000 |
| 9(b) | $[QB \text{ or } x =] 872 \times \tan 1 \text{ seen}$ | M2 | M1 for $\tan 1 = \frac{QB}{872}$ |
| | $\tan = their \ QB \div 525$ | M1 | |
| | 1.7 or 1.660 to 1.661 nfww | A1 | dep on M3 |
| 9(c)(i) | 222 000 or 222 100 or 222 101 | 2 | M1 for $\frac{1}{2} \times 525 \times 872 \times \sin 104$ |
| 9(c)(ii) | 5.55 or 5.550 to 5.553 nfww | 2FT | FT their (c)(i) $\times 100^2 \div 20000^2$ M1 for their (c)(i) $\times 100^2 \div 20000^2$ or restart |
| 10(a) | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 4 | All 8 regions correct M3 for 6 or 7 regions correct M2 for 4 or 5 regions correct M1 for 3 regions correct |
| 10(b)(i) | ∉ | 1 | |
| 10(b)(ii) | Ø | 1 | |
| 10(c) | 21, 23, 24, 29 | 2FT | Correct or FT SC1 for 1 omission or 4 correct and 1 extra |
| 10(d)(i) | 5 | 1FT | Correct or FT if less than 10 |
| 10(d)(ii) | 9 | 1FT | Correct or FT if less than 10 |
| 10(e) | \subset or \subseteq | 1 | |

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| Question | Answer | Marks | Part marks |
|----------|---|--------|--|
| 11 | 64 $(n+3)^2$ oe final answer | 1, 2 | M1 for a quadratic expression seen or second differences 2 |
| | 17 $3n+2$ oe final answer | 1, 2 | B1 for $3n + k$ (any k) or $kn + 2$ ($k \neq 0$) |
| | 47 $(n+3)^2 - (3n+2)$ oe isw | 1, 2FT | FT <i>their</i> difference expressions $A - B$ M1 for expression $an^2 + bn + c$ seen or second differences 2 |
| | $\frac{7}{6} = \frac{n+2}{n+1}$ of final answer | 1, 2 | B1 for $\frac{n+k+1}{n+k}$ seen |