

Question Number	Scheme	Marks
8. (a)	Let $y = 3 - 2e^{-x}$, then $2e^{-x} = 3 - y$	M1
	$-x = \ln \frac{3-y}{2} \text{ and } x =$ $x = -\ln \frac{3-y}{2}$	M1
	$f^{-1}(x) = \ln \frac{2}{3-x} \text{ or } -\ln \frac{3-x}{2} \text{ o.e.}$	A1
	Domain is $x < 3$	B1 (5)
(b)	$\ln \frac{2}{3-x} = \ln x \rightarrow 2 = (3-x)x$	M1
	$x^2 - 3x + 2 = 0$ $x = 2 \text{ or } x = 1$	A1 M1 A1 (4)
(c)	$3 - 2e^{-t} = ke^t \rightarrow ke^{2t} - 3e^t + 2 = 0$ or $\rightarrow ke^{2t} - 3e^t = -2$ o.e. (isw)	M1 A1
	Use " $b^2 - 4ac = 0$ " or " $b^2 = 4ac$ " or attempts $e^t = \frac{3 \pm \sqrt{9-8k}}{2k}$	dM1
	So $k = 1.125$ o.e. e.g. $\frac{9}{8}$ or $1\frac{1}{8}$	A1 (4)
[13]		

Notes

(a) **M1**: Puts $y = f(x)$ and makes e^{-x} term subject of formula so $2e^{-x} = 3 - y$ or $e^{-x} = \frac{3-y}{2}$ or even

$-2e^{-x} = y - 3$ or $-e^{-x} = \frac{y-3}{2}$ - allow sign slips. Allow $f(x)$ instead of y in expression for both Ms

M1: Uses \ln to get $x =$ (This mark is for knowing that $\ln x$ is inverse of e^x so allow sign errors and weak log work. These errors will be penalised in the A mark.)

A1: completely correct log work giving a correct unsimplified answer for $x =$ (then isw for this mark)

A1: any correct answer - do not need to see LHS of equation but variable **must** be x not y

NB Possible answers include $\frac{\log \frac{2}{3-x}}{\log e}$, $-\ln(3-x) + \ln 2$, $-\ln(-\frac{1}{2}x + \frac{3}{2})$, or $\ln \frac{-2}{x-3}$ etc

If x and y interchanged at start - see alternative in scheme. Note this method gives A1A1 or A0A0

B1: For $x < 3$ (independent mark); allow $(-\infty, 3)$, but $x \leq 3$ is B0

(b) **M1**: Removes \ln correctly on both sides and multiplies across

A1: expands bracket to give three term quadratic equation, allow $x^2 - 3x = -2$

M1: Solves quadratic (may be implied by answers)

A1: Need both these correct answers

(c) **M1**: Sets $3 - 2e^{-t} = ke^t$ and attempts to multiply all terms by e^t or by e^{-t} (allow use of x instead of t)

A1: three term quadratic - allow x or t so $ke^{2x} - 3e^x + 2 = 0$ or $ke^{2x} - 3e^x = -2$ or $k = 3e^{-t} - 2e^{-2t}$ etc

dM1: Uses condition for equal roots to give expression in k - may not be simplified- or attempts to solve their quadratic equation in e^t using formula or completion of the square **A1**: See scheme

