

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level

MARK SCHEME for the June 2005 question paper

9709 MATHEMATICS

9709/02

Paper 2, maximum raw mark 50

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which Examiners were initially instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began. Any substantial changes to the mark scheme that arose from these discussions will be recorded in the published *Report on the Examination*.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the *Report on the Examination*.

- CIE will not enter into discussion or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the June 2005 question papers for most IGCSE and GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Grade thresholds taken for Syllabus 9709 (Mathematics) in the June 2005 examination.

	maximum mark available	minimum mark required for grade:		
		A	B	E
Component 2	50	38	34	19

The thresholds (minimum marks) for Grades C and D are normally set by dividing the mark range between the B and the E thresholds into three. For example, if the difference between the B and the E threshold is 24 marks, the C threshold is set 8 marks below the B threshold and the D threshold is set another 8 marks down. If dividing the interval by three results in a fraction of a mark, then the threshold is normally rounded down.

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
 - A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
 - B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - The symbol \surd implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
 - Note: B2 or A2 means that the candidate can earn 2 or 0.
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking g equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR -1	A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
PA -1	This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

June 2005

GCE AS LEVEL

MARK SCHEME

MAXIMUM MARK: 50

SYLLABUS/COMPONENT: 9709/02

MATHEMATICS
Paper 2 (Pure Mathematics 2)

Page 1	Mark Scheme	Syllabus	Paper
	GCE AS LEVEL – JUNE 2005	9709	2

1	EITHER	State or imply non-modular inequality $x^2 > (3x - 2)^2$, or corresponding equation	M1	
		Expand and make reasonable solution attempt at 2- or 3-term quadratic, or equivalent	M1	
		Obtain critical values $\frac{1}{2}$ and 1	A1	
		State correct answer $\frac{1}{2} < x < 1$	A1	
OR		State one correct linear equation for a critical value	M1	
		State two equations separately	A1	
		Obtain critical values $\frac{1}{2}$ and 1	A1	
		State correct answer $\frac{1}{2} < x < 1$	A1	
OR		State one critical value from a graphical method or inspection or by solving a linear inequality	B1	
		State the other critical value correctly	B2	
		State correct answer $\frac{1}{2} < x < 1$	B1	4
2	(a)	Obtain a linear equation, e.g. $x \log 3 = \log 8$	B1	
		Obtain final answer 1.89	B1	2
(b)		Use $2 \ln y = \ln(y^2)$	M1	
		Use law for addition or subtraction of logarithms	M1	
		Obtain answer $z = \frac{y+2}{y^2}$	A1	3
3	(i)	Use the given iterative formula correctly at least once	M1	
		Obtain final answer $\alpha = 1.68$	A1	
		Show sufficient iterations to justify the answer to 2 dp	B1	3
(ii)		State equation, e.g. $x = \frac{3}{4}x + \frac{2}{x^3}$, in any correct form	B1	
		Derive the exact answer α (or x) = $\sqrt[4]{8}$, or equivalent	B1	2
4	(i)	Substitute $x = -1$ and equate to zero obtaining e.g. $(-1)^3 - (-1)^2 + a(-1) + b = 0$	B1	
		Substitute $x = 2$ and equate to 12	M1	
		Obtain a correct 3-term equation	A1	
		Solve a relevant pair of equations for a or b	M1	
		Obtain $a = 2$ and $b = 4$	A1	5
(ii)		Attempt division by $x + 1$ reaching a partial quotient of $x^2 + kx$, or similar stage by inspection	M1	
		Obtain quadratic factor $x^2 - 2x = 4$	A1	2
		[Ignore failure to repeat that $x + 1$ is a factor]		
5	(i)	Differentiate using chain or quotient rule	M1	
		Obtain derivative in any correct form	A1	
		Obtain given answer correctly	A1	3
(ii)		State $\frac{dx}{d\theta} = \sec^2 \theta$, or equivalent	B1	
		Use $\frac{dy}{dx} = \frac{dy}{d\theta} \div \frac{dx}{d\theta}$	M1	
		Obtain given answer correctly	A1	3

Page 2	Mark Scheme	Syllabus	Paper
	GCE AS LEVEL – JUNE 2005	9709	2

	(iii) State that $\theta = \frac{\pi}{6}$	B1	
	Obtain x-coordinate $1 + \frac{1}{\sqrt{3}}$, or equivalent	B1	
	Obtain y-coordinate $\frac{2}{\sqrt{3}}$, or equivalent	B1	3
6	(i) State coordinates (1, 0)	B1	1
	(ii) Use quotient or product rule	M1	
	Obtain correct derivative, e.g. $\frac{-\ln x}{x^2} + \frac{1}{x^2}$	A1	
	Equate derivative to zero and solve for x	M1	
	Obtain $x = e$	A1	
	Obtain $y = \frac{1}{e}$	A1	5
	(iii) Show or imply correct coordinates 0, 0.34657..., 0.36620..., 0.34657,,,	B1	
	Use correct formula, or equivalent, with $h = 1$ and four ordinates	A1	
	Obtain answer 0.89 with no errors seen	A1	3
	(iv) Justify statement that the rule gives an under-estimate	B1	1
7	(i) Make relevant use of the $\sin(A + B)$ formula	B1	
	Make relevant use of $\sin 2A$ and $\cos 2A$ formulae	M1	
	Obtain a correct expression in terms of $\sin x$ and $\cos x$	A1	
	Use $\cos^2 x = 1 - \sin^2 x$ to obtain an expression in terms of $\sin x$	M1(dep*)	
	Obtain given answer correctly	A1	5
	(ii) Replace integrand by $\frac{3}{4} \sin x - \frac{1}{4} \sin 3x$, or equivalent	B1	
	Integrate, obtaining $-\frac{3}{4} \cos x + \frac{1}{12} \cos 3x$, or equivalent	B1√ + B1√	
	Use limits correctly	M1	
	Obtain given answer correctly	A1	5