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1. (a) Write down the value of $8^{\frac{1}{3}}$. (1)

(b) Find the value of $8^{-\frac{2}{3}}$. (2)

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(Total 3 marks)

Q1



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Question 2 continued

(Total 5 marks)Leave
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3.
$$x^2 - 8x - 29 \equiv (x + a)^2 + b,$$

where a and b are constants.

(a) Find the value of a and the value of b . **(3)**

(b) Hence, or otherwise, show that the roots of

$$x^2 - 8x - 29 = 0$$

are $c \pm d\sqrt{5}$, where c and d are integers to be found. **(3)**



4.

Figure 1

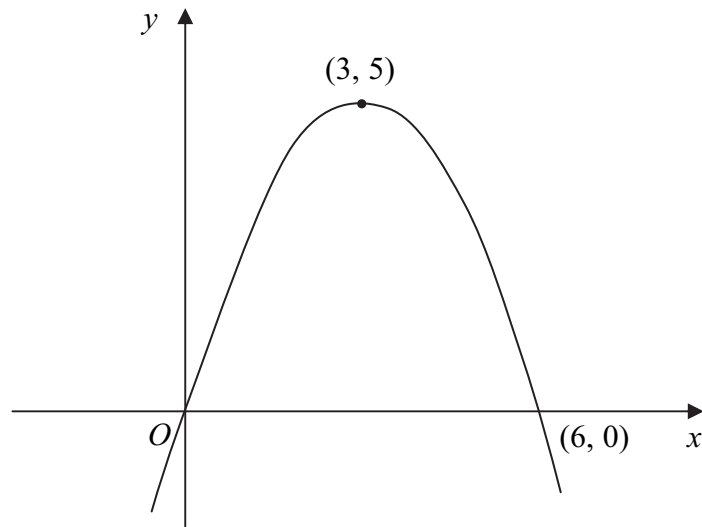


Figure 1 shows a sketch of the curve with equation $y = f(x)$. The curve passes through the origin O and through the point $(6, 0)$. The maximum point on the curve is $(3, 5)$.

On separate diagrams, sketch the curve with equation

(a) $y = 3f(x)$, (2)

(b) $y = f(x + 2)$. (3)

On each diagram, show clearly the coordinates of the maximum point and of each point at which the curve crosses the x -axis.



Question 4 continued

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Q4

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5. Solve the simultaneous equations

$$x - 2y = 1,$$

$$x^2 + y^2 = 29.$$

(6)

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6. Find the set of values of x for which

(a) $3(2x + 1) > 5 - 2x,$

(2)

(b) $2x^2 - 7x + 3 > 0,$

(4)

(c) **both** $3(2x + 1) > 5 - 2x$ **and** $2x^2 - 7x + 3 > 0.$

(2)



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Question 8 continued

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(Total 10 marks)

Q8



9. An arithmetic series has first term a and common difference d .

(a) Prove that the sum of the first n terms of the series is

$$\frac{1}{2}n[2a + (n-1)d]. \quad (4)$$

Sean repays a loan over a period of n months. His monthly repayments form an arithmetic sequence.

He repays £149 in the first month, £147 in the second month, £145 in the third month, and so on. He makes his final repayment in the n th month, where $n > 21$.

(b) Find the amount Sean repays in the 21st month.

(2)

Over the n months, he repays a total of £5000.

(c) Form an equation in n , and show that your equation may be written as

$$n^2 - 150n + 5000 = 0. \quad (3)$$

(d) Solve the equation in part (c).

(3)

(e) State, with a reason, which of the solutions to the equation in part (c) is **not** a sensible solution to the repayment problem.

(1)



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10. The curve C has equation $y = \frac{1}{3}x^3 - 4x^2 + 8x + 3$.

The point P has coordinates $(3, 0)$.

(a) Show that P lies on C .

(1)

(b) Find the equation of the tangent to C at P , giving your answer in the form $y = mx + c$, where m and c are constants.

(5)

Another point Q also lies on C . The tangent to C at Q is parallel to the tangent to C at P .

(c) Find the coordinates of Q .

(5)



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Question 10 continued

Lined area for writing the answer to Question 10.

Q10

(Total 11 marks)

TOTAL FOR PAPER: 75 MARKS

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