CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Ordinary Level

## MARK SCHEME for the May/June 2014 series

## **4037 ADDITIONAL MATHEMATICS**

4037/22 Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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F	Page 2	Mark Scheme		Syllabus	Paper
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1	ratio	police the denominator to get			
I	$\frac{1}{2}$	$\frac{(2+\sqrt{5})^2(\sqrt{5}+1)}{5-1}$ or better		or squaring to get	$\frac{4+4\sqrt{5}+5}{\sqrt{5}-1}$ or
	squar	squaring to get			
	(4+)	$\frac{(4+4\sqrt{5}+5)(\sqrt{5}+1)}{their4}$ or better		or rationalising the get $\sqrt{2}$	the denominator to $\overline{(1,1)}$
	$\frac{29}{4}$ +	$\frac{13}{4}\sqrt{5}$ oe isw	A1 + A1	$\frac{their(9+4\sqrt{5})\sqrt{5}}{5-1}$ correct simplifica	$\frac{(5+1)}{(5+1)}$ or better
				Allow $\frac{29+13\sqrt{5}}{4}$	- etc.
2	Corre	ectly eliminate y	M1	$-kx+2=2x^2-9$	9x + 4 oe
	$2x^{2}$ -	+(k-9)x+2[=0]oe	A1	allow even if x te condone $\dots = y$ p implies it should	erms not collected; rovided later work be 0
	Use	$b^2 - 4ac$ oe	M1	must be applie quadratic express as a coefficient; c	d to a 3 term sion containing $k$ condone < 0 etc.
	Reac	h $their(k-9=\pm 4)$ or			
	solve	s $their(k^2 - 18k + 65) = 0$	M1	condone $9-k =$ inequality at this	= ±4 ; condone an stage
	<i>k</i> = 5	and 13 cao	A1	mark final answer A0 if inequalities	r, do not isw; for final answers

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ĺ	Page	3	Mark Scheme		Śyllabus	Paper	
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3	; (i)	3(-1) to <i>d</i> =	$r^{3} - 14(-1)^{2} - 7(-1) + d = 0$ with completion = 10	B1	at least $-3 - 14 + d = 10$ ; N.B. = 0 implied by = d be seen in follow or convincingly s $3(-1)^3 - 14(-1)^2$ at least -3 - 14 + 7 + 10 or correct synthe as far as -1 3 - 14 -3	7 + d = 0, must be seen or d or = -d, may ing step. showing -7(-1)+10 = 0; = 0 tic division at least -7 = 10 17 = -10	
	(ii)	$3x^2 -$	-17x + 10 isw or $a = 3, b = -17, c = 10$ isw	B2, 1, 0	-1 each error; must be seen or referenced in (ii) even if found in (i) or (iii)		
	(iii)	(x+1)	(x-5)(3x-2)	M1	for factorising quadratic <b>ft</b> correct; condone omission of $(x+1)$ or for <b>ft</b> correct use of formula or <b>ft</b> correct completing the square		
		-1, 5,	$,\frac{2}{3}$	A1	If <b>M0</b> then <b>SC1</b> for all three root stated without working or verified/found by trials		

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		1			1		
4	(i)	12(x	$\left(-\frac{1}{4}\right)^{2} + \frac{17}{4}$ isw	<b>B3</b> , 2, 1,0	one mark for each of $p$ , $q$ , $r$ correct in a correctly formatted expression allow correct equivalent values;		
					If <b>B0</b> then <b>SC2</b> f	for $12\left(x - \frac{1}{4}\right) + \frac{17}{4}$	
					SC1 for correct 3 incorrect format $12\left(x - \frac{1}{x}\right) + \frac{17}{x}$	3 values seen in e.g.	
					$ \begin{pmatrix} 4 \\ 12 \\ x^2 - \frac{1}{4} \\ + \frac{17}{4} \\ \text{or for a correct c} \end{pmatrix} $	ompleted square	
					form of the original expression in a different but correct format. e.g.		
					$3\left(2x-\frac{1}{2}\right)^{2}+\frac{17}{4}$		
	(ii)	their	$\frac{4}{17}$ or <i>their</i> 0.235	B1ft	strict <b>ft</b> ; <i>their</i> $\frac{4}{17}$ fraction or decimination of the figs or more or the figs of the	- must be a proper al rounded to 3sig runcated to 4 figs	
		their	$x = \frac{1}{4}$ oe	B1ft	strict <b>ft</b> ; <i>x</i> must be correctly attributed		
5	(i)	1-20	$0x + 160x^2$	B2, 1, 0	-1 each error		
					if <b>B0</b> then <b>M1</b> for seen; may be unservice $1, 5(-4x), \frac{5 \times 2}{2}$	r 3 correct terms simplified e.g. $\frac{4}{4}(-4x)^2$	
	(ii)	a+(t)	heir - 20) = -23 soi	M1	condone sign err <i>their</i> –20 from (i	ors only; must be )	
		a = -	3	A1	validly obtained		
		b + (t	heir - 20)a + (their 160) = 222 soi	M1	condone sign err their -20 and the their a if used	ors only ; must be <i>rir</i> 160 from (i) and	
		<i>b</i> = 2		A1	validly obtained		

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	Page	5	Mark Scheme	Syllabus	Paper			
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6	(a) (i)	1		B1				
	(ii)	x = -	1 or -2	B1 + B1	as final answers			
	(b)	$\frac{\log_3 1}{\log_3 0}$	$\frac{5}{a}$ seen or implied	B1*	may be implied b $2\log_3 15 - \log_3 5$	у		
		2 log	$_{3}15 = \log_{3}15^{2}$ seen or implied	B1				
		log <sub>3</sub> 1	$15^2 - \log_3 5 = \log_3\left(\frac{15^2}{5}\right)$	B1dep*	not from wrong w	vorking		
		100.4	45 cao	R1	must be 45 not e	$\frac{225}{2}$ .		
		1053		DI	must be 45 not e.	<sup>g.</sup> 5 '		
					with no wrong wo	orking seen		
7	(i)	$x^4(3e$	$(e^{3x}) + 4x^3 e^{3x}$ isw	B1 + B1	each term of the s be a sum of two t	sum correct; must erms		
	(ii)	$\frac{1}{2+c}$	$\frac{1}{\cos x} \times (-\sin x)$ isw	B2	or <b>B1</b> for $\frac{1}{2 + \cos k}$ and <i>k</i> a constant	$\frac{1}{x} \times (k \pm \sin x)$		
	(iii)	$\frac{\mathrm{d}}{\mathrm{d}x}(\mathrm{s})$	$(in x) = \cos x soi$	B1				
		$\frac{\mathrm{d}}{\mathrm{d}x}(1)$	$(+\sqrt{x}) = \frac{1}{2} x^{-\frac{1}{2}}$ soi	B1				
			$\frac{\sqrt{x}}{their\cos x - \left(their\frac{1}{2}x^{-\frac{1}{2}}\right)\sin x}{\left(1 + \sqrt{x}\right)^2}$ isw	B1ft	for correct form of their $\cos x$ and the	of quotient rule <b>ft</b> eir $\frac{1}{2}x^{-\frac{1}{2}}$ ;		
					allow correct use chain rules to obtain $x\left(-\left(1+\sqrt{x}\right)^{-2}\right)$ $\cos x\left(1+\sqrt{x}\right)^{-1}$ or	of product and ain $\times \frac{1}{2} x^{\frac{1}{2}} +$		

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	Page	6	Mark Scheme	Syllabus	Paper	
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				1	1	
8		Subst equat	itution of either $x - 5$ or $y + 5$ into ion of curve and brackets expanded	M1	condone one sign equation of curve brackets; condon BUT $x - 5$ or $y +$	error in either or expansion of e omission of $= 0$ , 5 must be correct
		$2x^{2}$ -	$-8x - 10[= 0]$ or $2y^2 + 12y[= 0]$ obtained	A1		
		Solvi	ng their quadratic	M1	dep on a valid su	bstitution attempt
		(-1, -	-6) oe and (5, 0) oe isw	A1*+A1*	or A1 for correct coordinates or co coordinates	pair of <i>x</i> rrect pair of <i>y</i>
	$\sqrt{72}$		or $6\sqrt{2}$ cao isw	B1dep*		
9	(i)	[ <i>y</i> =]	$\frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} (+c)$ oe	B2	or <b>B1</b> for $(2x + 1)$	1/2+1
		10 =	$\frac{2}{6}(2(4)+1)^{\frac{3}{2}}+c$ oe	M1	for valid attempt slips e.g. omissio error	to find <i>c</i> ; condone n of power or sign
		$y = \frac{1}{2}$	$\frac{2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} + c \text{ seen and } c = 1 \text{ or}$	A1	must have $y = \dots$ $f(x) = \dots$	.; condone
	y =		$\frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} + 1$ isw			
		$\int \left(\frac{1}{3}\right)$	$(2x+1)^{\frac{3}{2}}+1$ $dx = \frac{1}{15}(2x+1)^{\frac{5}{2}} + x(+const)$	B1 + B1	<b>B1</b> for $(2x+1)^{\frac{3}{2}+1}$	) <del>2</del> ,
		$\left[\frac{1}{2}\right]$	$(2r+1)^{\frac{5}{2}} + r^{1.5} =$	B1ft	<b>B1</b> for $\frac{1}{15}(2x+1)$ <b>B1</b> ft <i>their</i> c from $c \neq 0$	) <sup>2</sup> 1 ( <b>i)</b> provided
		$\begin{bmatrix} 15 \\ 1\\ 15 \end{bmatrix}$	$2(1.5)+1)^{\frac{5}{2}}+(1.5)\left]-\left[\frac{1}{15}(2(0)+1)^{\frac{5}{2}}+0\right]$	M1	for a genuine atter – F(0) in an atten <i>their y</i> ; if their F( least their F(1.5)-	The second seco
		$\frac{107}{30}$	be isw	A1	as long as their <i>c</i> if decimal 3.57 or e.g. 3.566	is <b>not</b> numerical. r more accurate

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	1		1	1	
10 (i)	Taking logs of both sides		M1	any base; must b correct statement	e an explicitly t
	$\log y = \log A + x \log b$		A1	correct form; any from incorrect m	y base; no recovery tethod steps
(ii)	<i>b</i> : aw	rt 3 to one sf isw or awrt 4 to one sf isw	B2	or <b>M1</b> for $b = e^{t}$ their gradient mu evaluated as rise.	<sup>their gradient</sup> soi; ust be correctly /run
	<i>A</i> : aw	rt 0.5 to one sf	B2	or <b>B1</b> for $A = e^{-0.6}$	
				or <b>SC1</b> for $A = e$ an awrt 0.7)	$e^{-0.3} = 0.7$ (giving
(iii)	Evide	ence of graph used at $\ln y = 5.4$ soi	M1	or $\frac{220}{their 0.5} = (th)$	eir4) <sup>x</sup>
				or 5.39= <i>their</i>	(1.4)x + their - 0.6
				or $\ln(220) = x \ln(th)$	eir4) + ln( $their0.5$ )
	awrt -	4.4 to two sf	A1		

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	1			I	
11 (i)	f(x)	$> 3 \text{ or } [f(x) \in ](3,\infty)$	<b>B</b> 1	condone $y > 3$	
(ii)	<i>x</i> + 1	$=2^{y}$	M1	or $y + 1 = 2^x$	
	$f^{-1}(x) = \log_2(x+1)$		A1	mark final answe	er
				or $\log_2(y+1) = x$	x and
				$f^{-1}(x) = \log_2(x +$	- 1)
				or for $f^{-1}(x) = \frac{lo}{dx}$	$\frac{\log(x+1)}{\log 2}$ (any base
				for this form)	5
	Domain $x > 3$		B1ft	<b>ft</b> their <b>range</b> of mathematically winterval	f provided valid inequality or
	Range	e $f^{-1}(x) > 2$	<b>B</b> 1	condone $f(x) > 2$	or $y > 2$
(iii)	$2^{x}(2^{x})$	(-1) oe isw	<b>B</b> 1	e.g. $(2^x - 1)^2 + (2x - 1)$	
				or $2^{2x} - 2 \times 2^{x} +$	$1 + 2^{x} - 1$
	$2^{x}(2^{x})$	$(-1)=0$ leading to $2^x = 0$ , impossible or	B1	or $2^x = 0$ which of gf	is outside domain
	$2^{x} = 1$	$1 \Longrightarrow x = 0$	M1	or	
				$\begin{bmatrix} 2^{x}(2^{x}-1)=2^{2x}\\ 2^{2x}=2^{x}\end{bmatrix} \Rightarrow x=$	$-2^{x} = 0$ 0
	0 is n soluti	ot in the domain (and so $gf(x) = 0$ has no ons)	A1		

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Page 9		Mark Scheme	Syllabus	Paper	
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	1				
12 (i)	$\frac{\mathrm{d}y}{\mathrm{d}x} =$	$3x^2 - 18x + 24$	<b>B</b> 1		
	Solvi	ng their $3x^2 - 18x + 24 \ge 0$			
	by fac comp	ctorising or quadratic formula or leting the square	M1	attempt at differentiation resulting in quadratic expression with two terms correct; allow = or $\leq$ or $<$ o $>$ or $\geq$ 0 omitted here.	
	<u> </u>		4.1		
	Critic	al values 2 and 4 $\sim 2$		A0 if courious of	tampt to combine
	$x \le 2, x \ge 4$		AI	mark final answe	er
(ii)	Evalu	hating their $\frac{dy}{dx}$ at $x = 3$	M1		
	Use o	of $m_1m_2 = -1$ to get $m_{normal} = -\frac{1}{their(-3)}$	M1	must be explicit s gradient of norms equation	statement of al ; may be seen in
	y = 13	3 soi	B1		
	y-th	heir 18 = $\left(their\frac{1}{3}\right)(x-3)$ or			
	y = t	<i>heir</i> $\frac{1}{3}x + c$ and $c = their 17$ isw	A1ft	<b>ft</b> <i>their m</i> provide attempt at $m_{normal}$ m = their m.	ed a genuine ; no <b>ft</b> if
				tangent	
	P(0, 1)	17) cao	<b>B</b> 1		